Towards an Argument Game for Stable Semantics

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Abstract. In this paper, we present a discussion game for argumentation under stable semantics. Our work is inspired by Vreeswijk and Prakken, who have defined a similar game for preferred semantics. In the current paper, we restate Vreeswijk and Prakken's work using the approach of argument labellings and then show how it can be adjusted for stable semantics. The nature of the resulting argument game is somewhat unusual, since stable semantics does not satisfy the property of *relevance*.

1 Introduction

Stable semantics, a concept that goes back to [17] is one of the oldest semantics for argumentation and non-monotonic reasoning. Although Dung's landmark paper [10] was partially meant to argue against the use of it, stable semantics has remained an important concepts in fields like default logic [16] and logic programming [12, 13].

During recent years, several new semantics have been stated [2, 7, 11, 3]. What makes stable semantics unique, however, are two fundamental properties. First of all, there is the possible absence of stable extensions. When applying stable semantics in, for instance, answer set programming, this can in fact be a desirable property. If one encodes a problem such that the possible solutions correspond with the stable extensions, then the absence of stable extensions indicates the absence of solutions to the original problem. Secondly, stable semantics does not satisfy the property of relevance [7]. That is, it is possible for the status of an argument A to be influenced by a totally unrelated argument B. For instance, let (Ar, def) be an argumentation framework where the set of arguments Ar is $\{A, B\}$ and the defeat relation def is $\{(B, B)\}$. Then A and B are totally unrelated in the sense that there does not exist an (undirected) defeat-path between A and B. Yet, the existence of argument B causes argument A not to be credulously accepted.

The invalidity of the property of relevance has implications for the possibilities of defining an argument game. For instance, for grounded and preferred semantics, both of which do satisfy relevance, it is possible to define argument games in which each move is a response to a previous move [18, 15, 5]. For stable semantics, however, this is not possible. In the above example, argument B is the reason why argument A is not credulously accepted. Yet, it would be somewhat odd to reply to A with B, since no relation exists between these arguments.

In this paper, we propose an argument game that can deal with the unique characteristics of stable semantics. First, in Section 2, we briefly state some preliminaries on argument semantics and argument labellings. Then, in Section 3, we restate the approach of Vreeswijk and Prakken in terms of argument labellings. The discussion game for credulous acceptance under stable semantics is then given in Section 4, and an approach for sceptical acceptance under stable semantics is given in Section 5. Then, in Section 6, we finish with a discussion about some future research topics.

2 Argument Semantics and Argument Labellings

In this section, we briefly restate some preliminaries regarding argument semantics and argument-labellings.

Definition 1. An argumentation framework is a pair (Ar, def) where Ar is a finite set of arguments and $def \subseteq Ar \times Ar$.

We say that argument A defeats³ argument B iff $(A, B) \in def$.

An argumentation framework can be represented as a directed graph in which the arguments are represented as nodes and the defeat relation is represented as arrows. In several examples throughout this paper, we will use this graph representation.

Definition 2 (defense / conflict-free). Let (Ar, def) be an argumentation framework, $A \in Ar$ and $Args \subseteq Ar$. Args is conflict-free iff $\neg \exists A, B \in Args : A$ defeats B. Args defends argument A iff $\forall B \in Ar : (B \text{ defeats } A \supset \exists C \in Args : C \text{ defeats } B)$. Let $F(Args) = \{A \mid A \text{ is defended by } Args\}.$

In the definition below, definitions of grounded, preferred and stable semantics are described in terms of complete semantics, which has the advantage of making the proofs in the remainder of this paper more straightforward. These descriptions are not literally the same as the ones provided by Dung [10], but as is for instance stated in [6], these are in fact equivalent to Dung's original versions of grounded, preferred and stable semantics.

Definition 3 (acceptability semantics). Let (Ar, def) be an argumentation framework. A conflict-free set $Args \subseteq Ar$ is called

- an admissible set iff $Args \subseteq F(Args)$.
- a complete extension iff Args = F(Args).
- a grounded extension iff Args is the minimal complete extension.
- a preferred extension iff Args is a maximal complete extension.
- a stable extension iff Args is a complete extension that defeats every argument in $Ar \setminus Args$.
- a semi-stable extension iff Args is a complete extension where $Args \cup Args^+$ is maximal (w.r.t. set-inclusion)

The concepts of admissibility, as well as those of complete, grounded, preferred, stable or semi-stable semantics were originally stated in terms of sets of arguments. It is equally well possible, however, to express these concepts using *argument labellings*. This approach has been proposed by Pollock [14] and has recently been extended by Caminada [6]. The idea of a labelling is to associate

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 $^{^{3}}$ We follow the terminology of [1].

with each argument exactly one label, which can either be in, out or undec. The label in indicates that the argument is explicitly accepted, the label out indicates that the argument is explicitly rejected, and the label undec indicates that the status of the argument is undecided, meaning that one abstains from an explicit judgement whether the argument is in or out.

Definition 4. A labelling is a function \mathcal{L} : $Ar \longrightarrow \{in, out, undec\}.$

We write $in(\mathcal{L})$ for $\{A \mid \mathcal{L}(A) = in\}$, $out(\mathcal{L})$ for $\{A \mid \mathcal{L}(A) = out\}$ and $undec(\mathcal{L})$ for $\{A \mid \mathcal{L}(A) = undec\}$.

Since a labelling is a function, which is essentially a relation, it can be represented as a set of pairs. For instance, a labelling of the argumentation framework of Figure 1 would be $\{(A, in), (B, out), (C, undec), (D, undec), (E, undec)\}$.

Definition 5. Let \mathcal{L} be a labelling of argumentation framework (Ar, def) and $A \in Ar$. We say that:

- A is legally in iff L(A) = in and ∀B ∈ Ar : (B def A ⊃ L(B) = out)
 A is legally out iff L(A) = out
- and $\exists B \in Ar : (B \text{ def } A \land \mathcal{L}(B) = in).$ 3. A is legally under iff $\mathcal{L}(A) = under$
- and $\neg \forall B \in Ar : (B \text{ def } A \supset \mathcal{L}(B) = \texttt{out})$ and $\neg \exists B \in Ar : (B \text{ def } A \land \mathcal{L}(B) = \texttt{out})$

We say that an argument A is *illegally* in iff $\mathcal{L}(A) = \text{in but}$ A is not legally in. We say that an argument A is *illegally* out iff $\mathcal{L}(A) = \text{out but } A$ is not legally out. We say that an argument A is *illegally* undec iff $\mathcal{L}(A) = \text{out but } A$ is not legally undec.

Definition 6. An admissible labelling \mathcal{L} is a labelling where each argument that is labelled in is legally in and each argument that is labelled out is legally out.

A complete labelling is an admissible labelling where each argument that is labelled undec is legally undec.

A grounded labelling is a complete labelling \mathcal{L} where $in(\mathcal{L})$ is minimal (w.r.t. set inclusion).

A preferred labelling is a complete labelling \mathcal{L} where $in(\mathcal{L})$ is maximal (w.r.t. set inclusion).

A semi-stable labelling is a complete labelling \mathcal{L} where $undec(\mathcal{L})$ is minimal (w.r.t. set inclusion).

A stable labelling is a complete labelling \mathcal{L} where $undec(\mathcal{L}) = \emptyset$.

It can be proved that the various types of labellings correspond to the various kinds of argument semantics [6, 8].

Theorem 1. Let (Ar, def) be an argumentation framework and let $Args \subseteq Ar$.

Args is an admissible set iff

there exists an admissible labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}rgs$.

Args is a complete extension iff

there exists a complete labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}rgs$.

Args is the grounded extension iff

there exists a grounded labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}$ rgs.

Args is a preferred extension iff

there exists a preferred labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}rgs$.

Args is a semi-stable extension iff

there exists a semi-stable labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}$ rgs.

Args is a stable extension iff

there exists a stable labelling \mathcal{L} with $in(\mathcal{L}) = \mathcal{A}rgs$.

There are different ways to characterize a stable extension.

Proposition 1. Let (Ar, def) be an argumentation framework. The following statements, describing the concept of stable semantics, are equivalent:

- 1. Args defeats exactly the arguments in $Ar \setminus Args$
- 2. Args is a conflict-free set that defeats each argument in Ar\Args
- 3. Args is an admissible set that defeats each argument in Ar\Args
- 4. Args is a complete extension that defeats each argument in Ar\Args
- 5. Args is a preferred extension
- that defeats each argument in Ar\Args 6. Args is a semi-stable extension

that defeats each argument in $Ar \setminus Args$

3 Vreeswijk and Prakken's Argumentation Game for Preferred Semantics

In this section we treat a reformulated version of Vreeswijk and Prakken's argument game for preferred semantics [18]. Although there also exist other argument games for preferred semantics, like [9], we have chosen [18] for its relative simplicity and its easy adaptability to work with argument labellings. Our reformulation is aimed at slightly simplifying Vreeswijk and Prakken's approach, and also to allow for its easy adaptation to stable semantics, which will be treated in the next section.

In order to determine whether an argument (say A) is in an admissible set (say Args), one can examine whether there exists an admissible labelling (\mathcal{L}) with $\mathcal{L}(A) = in$ (Theorem 1). The discussion game is then aimed at providing this admissible labelling. The game can be described as follows:

- proponent (P) and opponent (O) take turns; P begins
- each move of O is a defeater of some (not necessarily the directly preceding) previous argument of P
- each move of P (except the first one) is a defeater of the directly preceding argument of O
- O is not allowed to repeat its own moves, but may repeat P's moves
- P is not allowed to repeat O's moves, but may repeat its own moves

The game is won by the proponent iff the opponent cannot move anymore. It is won by the opponent iff the proponent cannot move anymore, or if the opponent managed to repeat one of the proponent's moves.

One good way to view the discussion game is as the proponent trying to build the set of in-labelled arguments and the opponent trying to build the set of out-labelled arguments. As an example, consider the argumentation framework illustrated in Figure 1.

Here, the proponent can win the discussion game for argument D in the following way:

P: in(D) "I have an admissible labelling in which D is labelled in." O: out(C) "Then in your labelling it must also be the case that D's defeater C is labelled out (otherwise D would not be legally in). Based on which grounds?"

P: in(B) "C is labelled out because B is labelled in."

O: $\operatorname{out}(A)$ "Then in your labelling it must also be the case that B's defeater A is labelled out (otherwise B would not be legally in). Based on which grounds?"

P: in(B) "A is labelled out because B is labelled in."

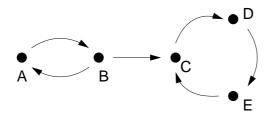


Figure 1. An argumentation framework

The above example illustrates the need for the proponent to be able to repeat its own arguments. At the same time, the proponent should not be allowed to repeat the opponent's arguments, since these have to be labelled out, so the proponent cannot claim them to be labelled in.

The argumentation framework of Figure 1 can also be used for an example of a game won by the opponent:

P: in(E) "I have an admissible labelling in which E is labelled in." O: out(D) "Then in your labelling it must be the case that E's defeater D is labelled out. Based on which grounds?"

P: in(C) "D is labelled out because C is labelled in."

O: out(E) "Then in your labelling it must be the case that C's defeater E is labelled out. This contradicts with your earlier claim that E is labelled in."

The correlation between the thus described discussion game and the concept of admissibility can be described as follows.

Theorem 2. Let (Ar, def) be an argumentation framework and $A \in Ar$. There exists an admissible labelling \mathcal{L} with $\mathcal{L}(A) = \operatorname{in}$ iff there exists an admissible discussion for A that is won by the proponent.

Since the concept of admissible labellings coincides with the concept of an admissible set (theorem 1) it holds that an argument is in an admissible set iff it is possible for the proponent to win the discussion for it. Moreover, it holds that an argument is in an admissible set iff it is in a preferred extension (or, alternatively, iff it is labelled in in a preferred labelling). Hence, the discussion game can be used as a basis for proof procedures for credulous preferred.

Vreeswijk and Prakken show that the discussion game can also be used as a basis for the decision problem of sceptical preferred semantics. This approach, however, only works for argumentation frameworks where every preferred extension is also a stable extension.

4 A Discussion Game for Credulous Stable Semantics

In the current section, we provide the main result of this paper, which is a discussion game for credulous stable semantics. Before doing so, it may be illustrative to see why the standard admissibility discussion game does not work for stable semantics. Consider again the argumentation framework of Figure 1. Even though A is in an admissible set and in a preferred extension ($\{A\}$), A is not in a stable extension. To see why A is in an admissible set, consider the following discusion:

P: in(A) "I have an admissible labelling where A is labelled in" O: out(B) "Then in your labelling, argument B must be labelled out. Based on which grounds?"

P: in(A) "B is labelled out because A is labelled in"

The point is, however, that once it has been committed that A is labelled in and B is labelled out, it is not possible anymore to label the remaining arguments such that final result will be a stable labelling. This can be seen as follows. Suppose C is labelled in. Then E must be labelled out, so D should be labelled in, which means that C would be labelled out. Contradiction. Similarly, suppose that C is labelled out. Then E must be labelled in, so D should be labelled in, so D should be labelled out, so C should be labelled in. Again, contradiction.

Proposition 1 shows that there are many ways to characterize a stable extension. For our purposes, the most useful characterization is that of an admissible set which defeats every argument that is not in it. When one translates this to labellings, one obtains an admissible labelling where each argument is labelled either in or out

It appears that a discussion game for stable semantics requires an additional type of move: question. By questioning an argument (question(A)), the opponent asks the proponent to give an explicit opinion on whether A should be labelled in or out. If the proponent thinks that A should be labelled in then it should respond with in(A). If the proponent thinks that A should be labelled out then it should respond with in(B) where B is a defeater of A. The discussion game for stable semantics can thus be described as follows:

- The proponent (P) and opponent (O) take turns. The proponent begins.
- Each move of the opponent is either of the form out(A), where A is a defeater of some (not necessarily the directly preceeding) move of the proponent, or of the form question(A), where A is an argument that has not been uttered in the discussion before (by either the proponent or the opponent). The opponent is only allowed to do a question move if it cannot do an out move.
- The first move of the proponent is of the form in(A), where A is the main argument of the discussion. The following moves of the proponent are also of the form in(A). If the directly preceeding move of the opponent is of the form out(B) then A is a defeater of B. If the directly preceeding move of the opponent is of the form question(B) then A is either equal to B or a defeater of B.
- The opponent may not repeat any of its out moves.
- The proponent is allowed to repeat its own moves, but may not do an in(A) move if the opponent has done some earlier out(A) move.

The opponent wins if it is able to do an out(A) move and the proponent has done an earlier in(A) move, or if the proponent cannot move anymore. The proponent wins if the opponent cannot move anymore.

To illustrate the use of the discussion game, consider the argumentation framework depicted in Figure 2.

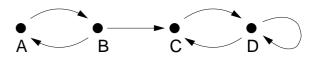


Figure 2. Another argumentation framework

Suppose the proponent would like to start a discussion about A. P: in(A) "I have a stable labelling in which A is labelled in." O: out(B) "Then in your labelling, A's defeater B must be labelled out. Based on which grounds?"

P: in(A) "B is labelled out because A is labelled in."

O: question(C) "What about C?"

 $\mathbf{P}: \mathtt{in}(C)$ "C is labelled in."

O: $\operatorname{out}(D)$ "Then C's defeater D must be labelled out. Based on which grounds?"

P: in(C) "D is labelled out because C is labelled in."

The proponent wins the discussion, since the opponent cannot move anymore.

The above example also shows that the outcome of a discussion may depend on P's response to a question move. For instance, if Pwould have replied to question(C) with in(D), then it would have lost the discussion, since O would then do out(D).

As an example of a game that cannot be won by the proponent, consider a game for argument B. This game has to be lost by the proponent since the argumentation framework of Figure 2 has only one stable extension: $\{A, C\}$, which does not include B.

P: in(B) "I have a stable labelling in which B is labelled in."

O: $\operatorname{out}(A)$ "Then in your labelling, B's defeater A must be labelled out. Based on which grounds?"

P: in(B) "A is labelled out because B is labelled in."

O: question(C) "What about C?"

P: in(D) "C is labelled out because its defeater D is labelled in." O: out(D) "Then D's defeater D (itself) must be labelled out. Contradiction."

The proponent would still not have won the discussion if it had responded to question(C) with in(C) instead of with in(D). This is because then the opponent would have reacted with out(B) and would therefore still have won the discussion.

Formally, the stable discussion game can be described as follows.

Definition 7. Let (Ar, def) be an argumentation framework. A stable discussion is a sequence of moves $[M_1, M_2, \ldots, M_n]$ $(n \ge 0)$ such that:

- each M_i $(1 \le i \le n)$ where *i* is odd (which is called a proponent move) is of the form in(A), where $A \in Ar$.
- each M_i $(1 \le i \le n)$ where i is even (which is called an opponent move) is of the form out(A) where $A \in Ar$, or of the form question(A) where $A \in Ar$.
- For each opponent move $M_i = \operatorname{out}(A)$ $(2 \le i \le n)$ there exists a proponent move $M_j = \operatorname{in}(B)$ (j < i) where A defeats B.
- For each proponent move $M_i = in(A)$ ($3 \le i \le n$) it either holds that (1) $M_{i-1} = out(B)$ where A defeats B, or (2) $M_{i-1} = question(B)$ where either A = B or A defeats B.
- For each opponent move M_i = out(A) (1 ≤ i ≤ n) there does not exist an opponent move M_j = out(A) with j < i.
- For each opponent move $M_i = \text{question}(A)$ $(1 \le i \le n)$ there does not exist any move M_j (j < i) of the form in(A), out(A) or question(A).
- For each proponent move $M_i = in(A)$ $(1 \le i \le n)$ there does not exist an opponent move $M_j = out(A)$ with j < i.

A stable discussion $[M_1, M_2, \ldots, M_n]$ is said to be finished iff there exists no M_{n+1} such that $[M_1, M_2, \ldots, M_n, M_{n+1}]$ is a stable discussion, or if M_n is an opponent move of the form out(A) for which there exists a proponent move M_i $(1 \le i \le n)$ of the form in(A). A finished discussion is won by the proponent if the last move is a proponent move, and is won by the opponent if the last move is an opponent move.

Theorem 3. Let (Ar, def) be an argumentation framework and $A \in Ar$. There exists a stable labelling \mathcal{L} with $\mathcal{L}(A) = \operatorname{in}$ iff there exists

a stable admissible discussion for A that is won by the proponent.

Proof. " \Longrightarrow " Suppose there exists a stable labelling \mathcal{L} with $\mathcal{L}(A) =$ in.

At the first step the proponent labels A with in. Trivially, it now holds that we have a game in which all in-labelled moves are also labelled in in the stable labelling \mathcal{L} .

We now prove that any unfinished discussion where the proponent does the last move and where all Proponent-moves are labelled in in \mathcal{L} can be extended to a discussion with an additional opponent move and an additional proponent-move such that the result will again be a discussion in which the proponent does the last move, and all proponent moves are labelled in in \mathcal{L} .

Let $[M_1, \ldots, M_n]$ be an unfinished discussion where M_n is a proponent move and all proponent moves are labelled in in \mathcal{L} . From the fact that the discussion is unfinished, it follows that the opponent can do a move M_{n+1} which is either of the form $\operatorname{out}(B)$, where B is a defeater of some earlier proponent move (say in(A)), or of the form $\operatorname{question}(B)$. In the first case $(\operatorname{out}(B))$, it holds that B is labelled out in \mathcal{L} , because A is labelled in in \mathcal{L} . It then follows that there exists an argument C which defeats B and is labelled in in \mathcal{L} , which makes it possible for the proponent to respond with in(C). In the second case (question(B)), the proponent can either respond with in(B) if B is labelled in in \mathcal{L} , or with in(C) if B is labelled out in \mathcal{L} , where C is a defeater of B. In any case, the resulting discussion will have a proponent move as the last move, and all proponent moves labelled in in \mathcal{L} .

From the facts that the argumentation framework is finite, the opponent cannot repeat its moves and every unfinished discussion game can always be extended to a discussion game in which the last move is still move by the proponent, it follows that the discussion game can ultimately be extended in such a way that it is won by the proponent.

" \Leftarrow " Suppose there exists a stable discussion game for argument A that is won by the proponent. Let Args be the set of the in labelled arguments. Args is confict-free, otherwise the opponent would have labelled an argument out that was labelled in by proponent earlier and would have won the game. Furthermore, Args defeats each argument that is not in Args. This can be seen as follows. Let $B \notin Args$. Then either (1)the opponent made a move out(B) which means the proponent labelled an argument C in such that C defeats B, or (2) the opponent made a move question(B) which followed by in(C) of proponent where C defeats B. In both cases, C is in Args, so Args defeats B.

Since Args is conflict-free and defeats each argument not in it, Args is a stable extension. From theorem 1, it follows that there exists a stable labelling with A is labelled in.

For the discussion game for preferred semantics, it is quite straightforward to convert the resulting game to an admissible labelling: $\mathcal{L} = \{(A, in) \mid \text{there exists a proponent-move } in(A)\} \cup \{(A, out) \mid \text{there exists an opponent-move } out(A)\} \cup \{(A, undec) \mid \text{there does not exist a proponent-move } in(A) and there does not exist an opponent-move out(A)}.$

For the discussion game for stable semantics, converting the moves of the game to a stable labelling is slightly different. $\mathcal{L} = \{(A, in) \mid \text{there exists a proponent-move } in(A)\} \cup \{(A, out) \mid \text{there exists an opponent-move } out(A)\} \cup \{(A, out) \mid \text{there exists an opponent-move } question(A) \text{ that was responded to with } in(B) where B is a defeater of } A\}.$

There are some possible optimizations for the above mentioned discussion game. As Vreeswijk and Prakken point out, the role of the opponent can also be seen as actually *helping* the proponent to find

what it is looking for. If one takes this perspective, then it is quite reasonable to require the opponent to do a question-move only when it has (temporarily) cannot do an out move anymore. There is, however, another way in which the opponent can help the proponent to construct a stable labelling. If the opponent has to do a questionmove, because it (temporarily) ran out of out-moves, then it makes sense for the opponent to try to do a question(A)-move such that (1) A is an argument that has a defeater that is in (that is, there exists an argument B such that B defeats A and the proponent did an in(B)-move in the past) or (2) A is an argument that has all its defeaters out (that is, for each argument B such that B defeats A, the opponent did either an out(B)-move or a question(B)-move at which the proponent did not respond with an in(B)-move). In both cases, it is clear how the proponent should respond. In case (1), the proponent should respond with in(B) (where B is a defeater of A that was already found to be in; basically, the proponent is repeating one of its earlier moves). In case (2), the proponent will respond with in(A). In general, the opponent could adapt a strategy of trying to select questions that are relatively easy to answer for the proponent. Such a strategy does not influence the correctness and completeness of the discussion game as a proof theory for stable semantics.

5 A Discussion Game for Sceptical Stable Semantics

In [18] Vreeswijk and Prakken provide a procedure for determining if an argument is an element of every preferred extension. Their procedure, however, only works for argumentation frameworks where each preferred extension is also a stable extension. The discussion procedure for sceptical stable semantics that is proposed in this section does not have this restriction.

The idea is that an argument is in each stable extension iff there is no stable extension that contains one of its defeaters.

So in order to examine whether an argument A is in each stable extension, one should examine the defeaters of A one by one. If one finds a defeater that is in a stable extension, then the question of whether A is in each stable extension can be answered with "no". If, however, it turns out that each defeater of A is not in any stable extension, then the answer is "yes". Therefore, one can simply apply the (credulous) stable discussion game for each defeater of A, to obtain the answer regarding sceptical stable.

6 Discussion and Further Research

In this paper, we have discussed a discussion game for stable semantics, based on the work of Vreeswijk and Prakken [18]. Our discussion game is not the only approach that can be based their work. The proof procedures of Dung, Mancarella and Toni for *ideal semantics* [11] can, for instance, also be described in terms of Vreeswijk and Prakken's argument game for preferred semantics. We recall that a set of arguments is *ideal* iff it is an admissible subset of each preferred extension. The *ideal extension* can then be defined as the (unique) maximal ideal set of arguments. It holds that an argument is in the ideal extension iff it is in an admissible set that is not defeated by any admissible set [11]. This means one can first perform the dialogue game for the argument itself, and then the dialogue game against each argument in the thus obtained admissible set to see whether the main argument is in the ideal extension.

The discussion game for stable semantics has so far been described in a rather informal way, similarly like was done in [18]. It would be interesting to provide a more formalized version of the dialogue game, like for instance was done by Bodenstaff, Prakken and Vreeswijk [4]. Their approach is to use event calculus to formalize the discussion game of [18]. For the stable discussion game, such a formalization would be a topic for future research.

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