

An Introduction to Formal Argumentation Theory



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Research Agenda:

Argumentation for Explainable Inference

- Formal Argumentation has its roots in Non Monotonic Reasoning (NMR)
- The idea is how to reason with “rules of thumb”
- Many formalisms for NMR can be captured by formal argumentation
- One of the aims of formal argumentation is to bridge the gap between human reasoning and automated inference

An Example [Prakken]

Paul: My car is very safe.

Olga: Why?

Paul: Since it has an airbag.

Olga: It is true that your car has an airbag, but I do not think that this makes your car safe, because airbags are unreliable: the newspapers had several reports on cases where airbags did not work.

Paul: I also read that report but a recent scientific study showed that cars with airbags are safer than cars without airbags, and scientific studies are more important than newspaper reports.

Arguments and attacks

Argument: expresses one or more reasons that lead to a proposition

$a, b, c \Rightarrow d$ or $a, b \Rightarrow c; c \Rightarrow d$

An argument can *attack* another argument

rebutting attack:

attack one of the *conclusions* of the other argument:

$e, f, g \Rightarrow \neg d$ against $a, b, c \Rightarrow d$

undercutting attack:

attack the *reasons* of the other argument

$e, f, g \Rightarrow [a, b, c \not\Rightarrow d]$ against $a, b, c \Rightarrow d$

Example

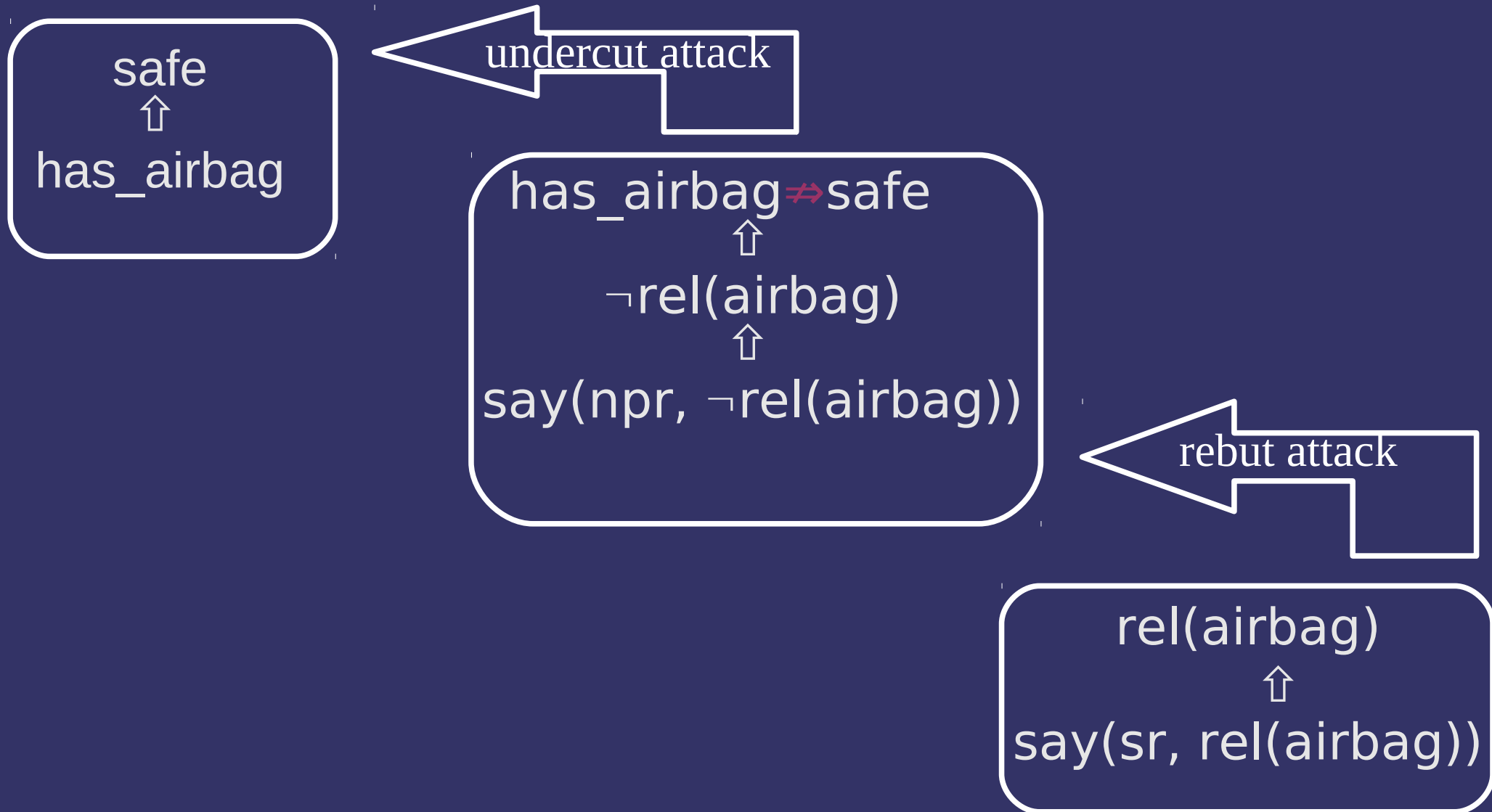
A: My car is very safe, since it has an airbag:
 $\text{has_airbag} \Rightarrow \text{safe}$

B: The newspapers say that airbags are not reliable, so having an airbag is not a good reason why your car is safe

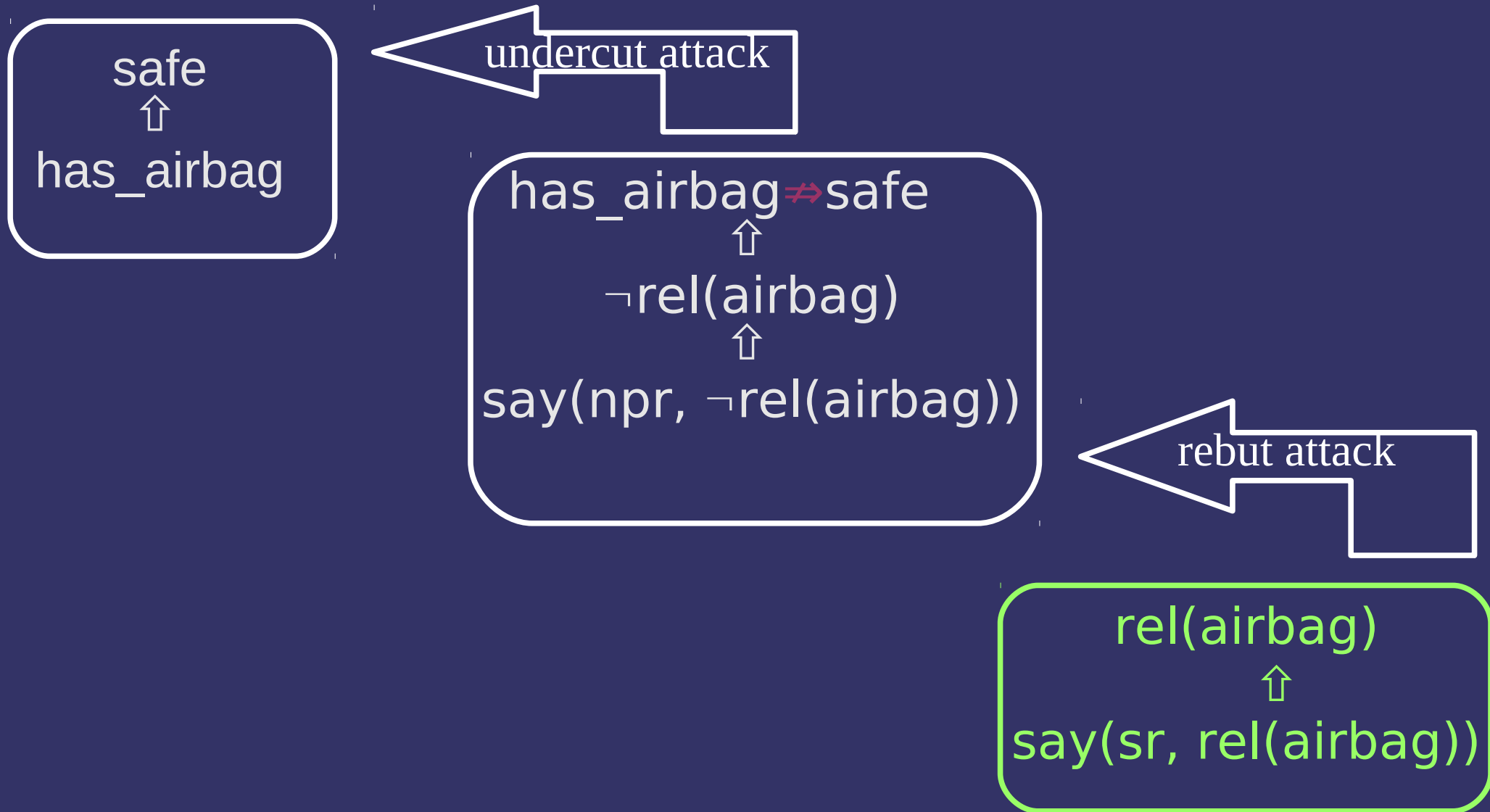
$\text{say}(\text{npr}, \neg \text{rel}(\text{airbag})) \Rightarrow \neg \text{rel}(\text{airbag})$
 $\neg \text{rel}(\text{airbag}) \Rightarrow [\text{has_airbag} \not\Rightarrow \text{safe}]$

C: Scientific reports say that airbags are reliable.
 $\text{say}(\text{sr}, \text{rel}(\text{airbag})) \Rightarrow \text{rel}(\text{airbag})$

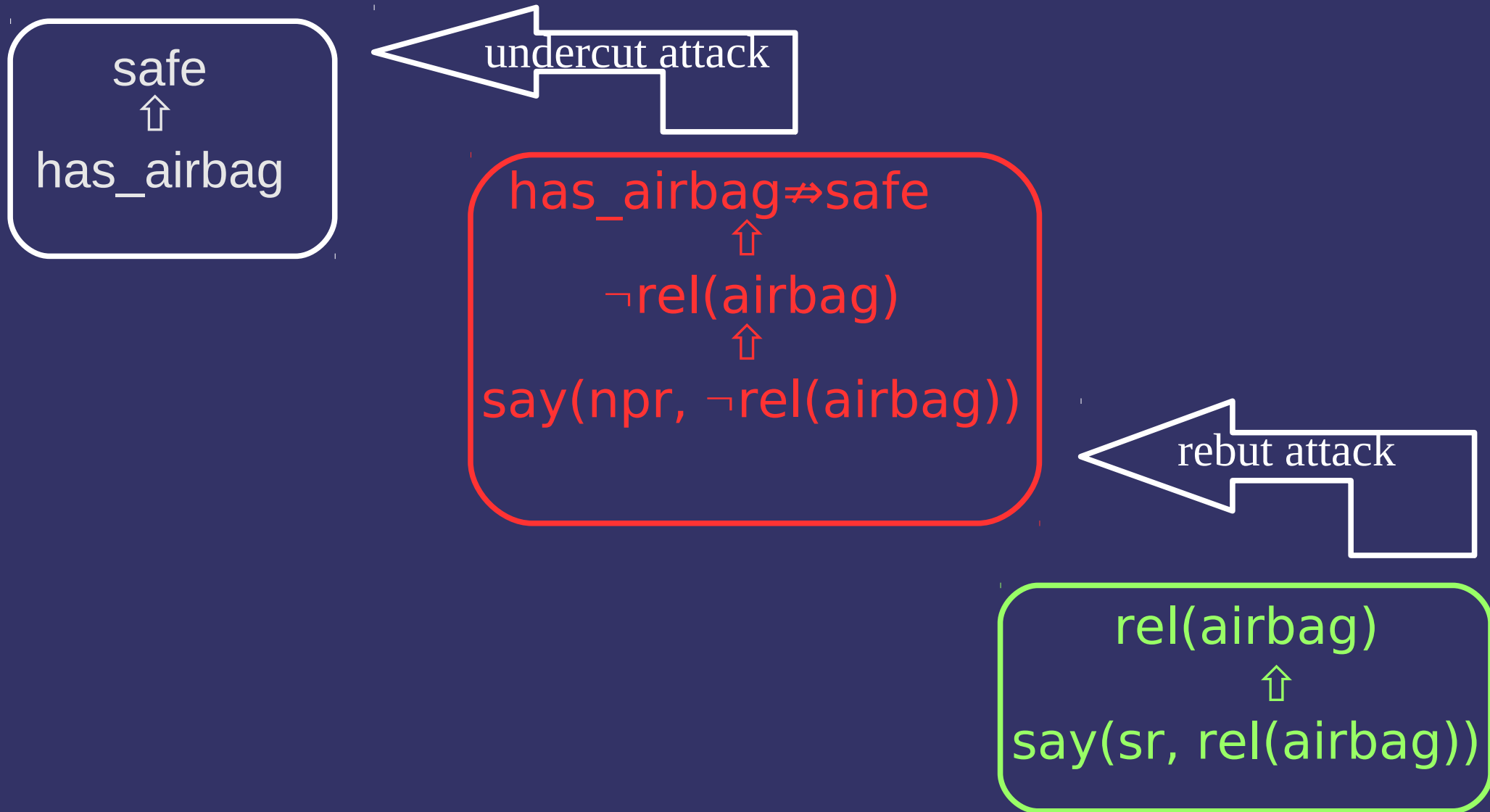
Example



Example



Example



Example

safe
↑
has_airbag

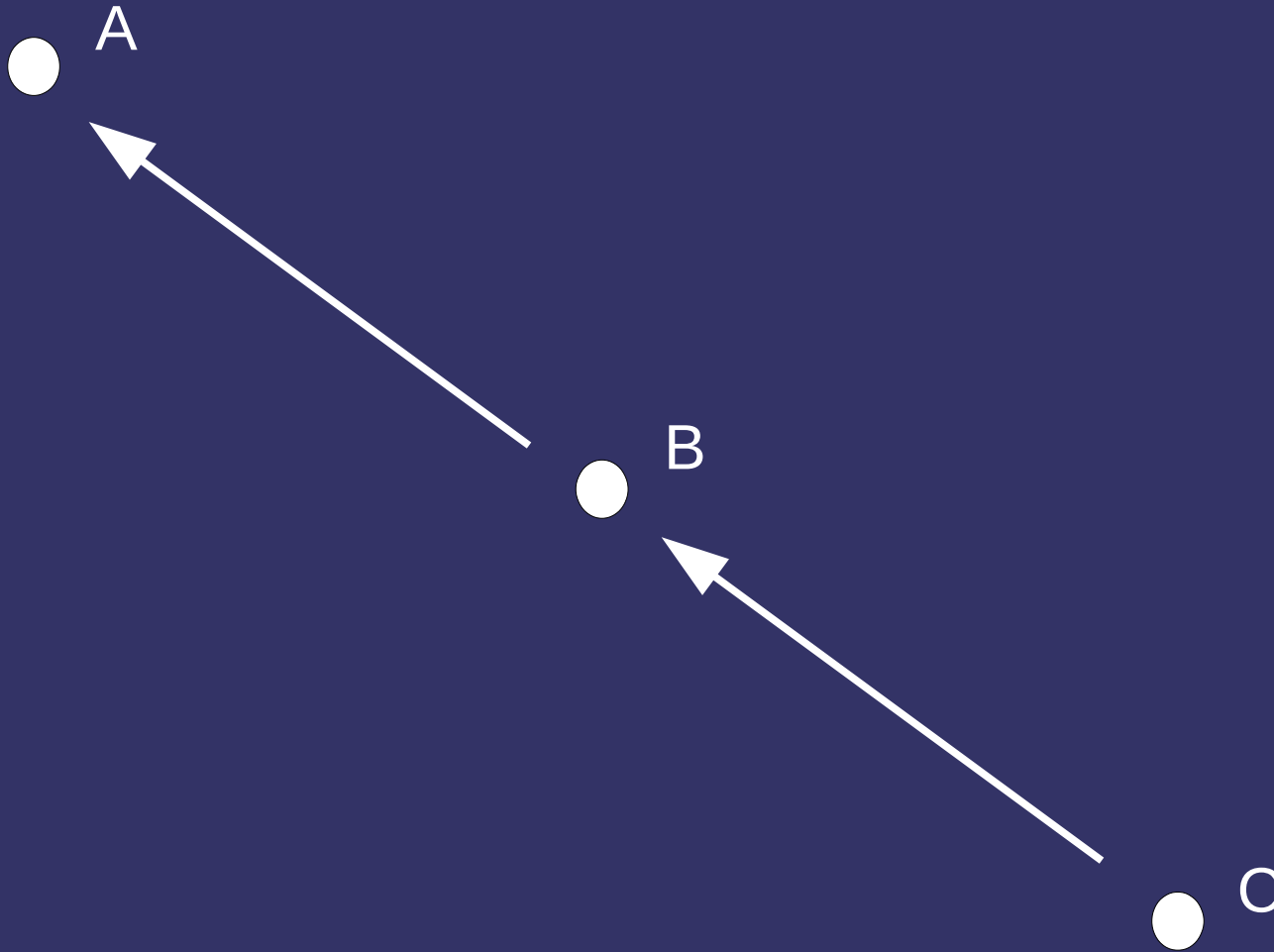
undercut attack

has_airbag \Rightarrow safe
↑
 \neg rel(airbag)
↑
say(npr, \neg rel(airbag))

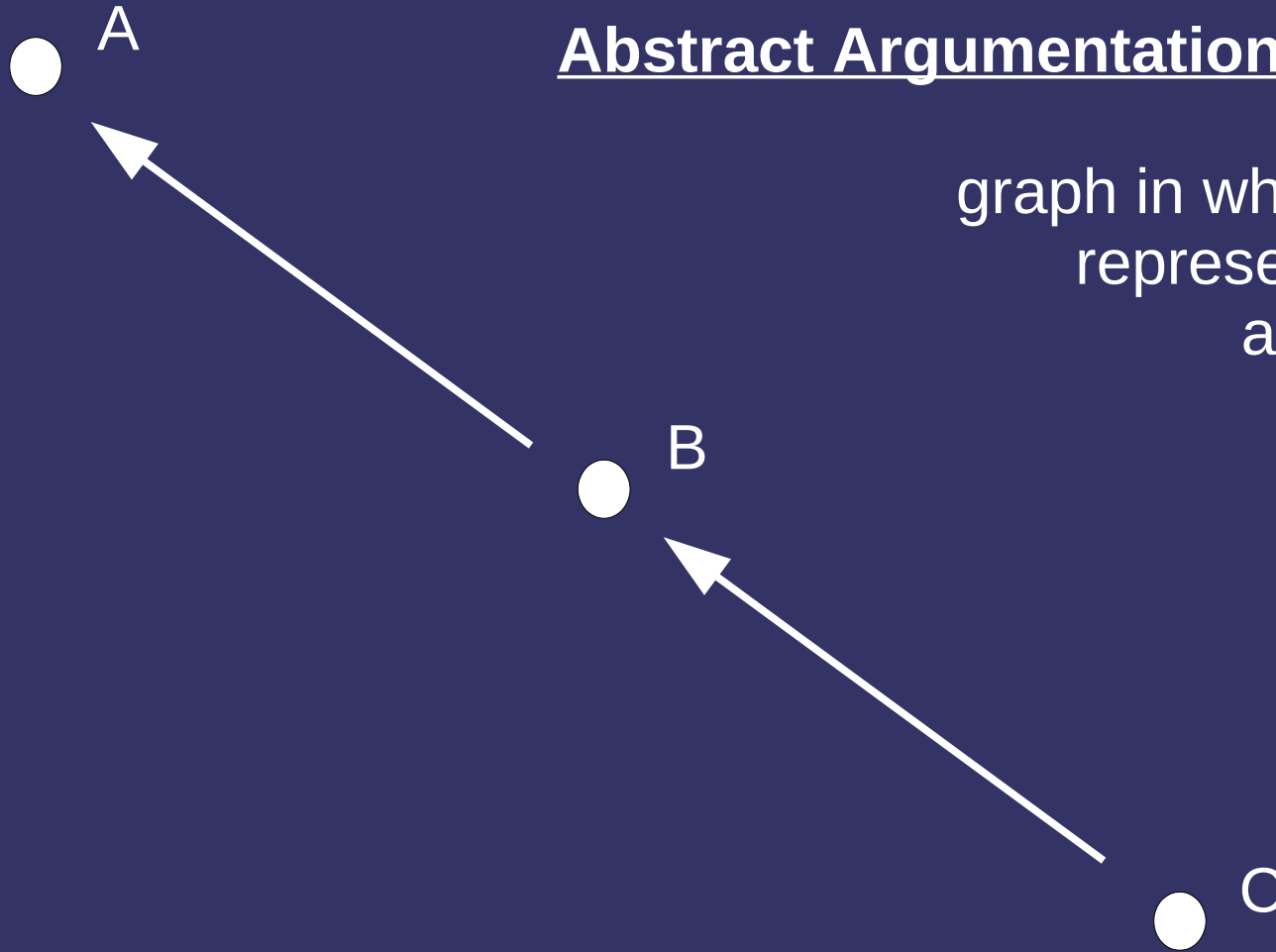
rebut attack

rel(airbag)
↑
say(sr, rel(airbag))

Abstraction



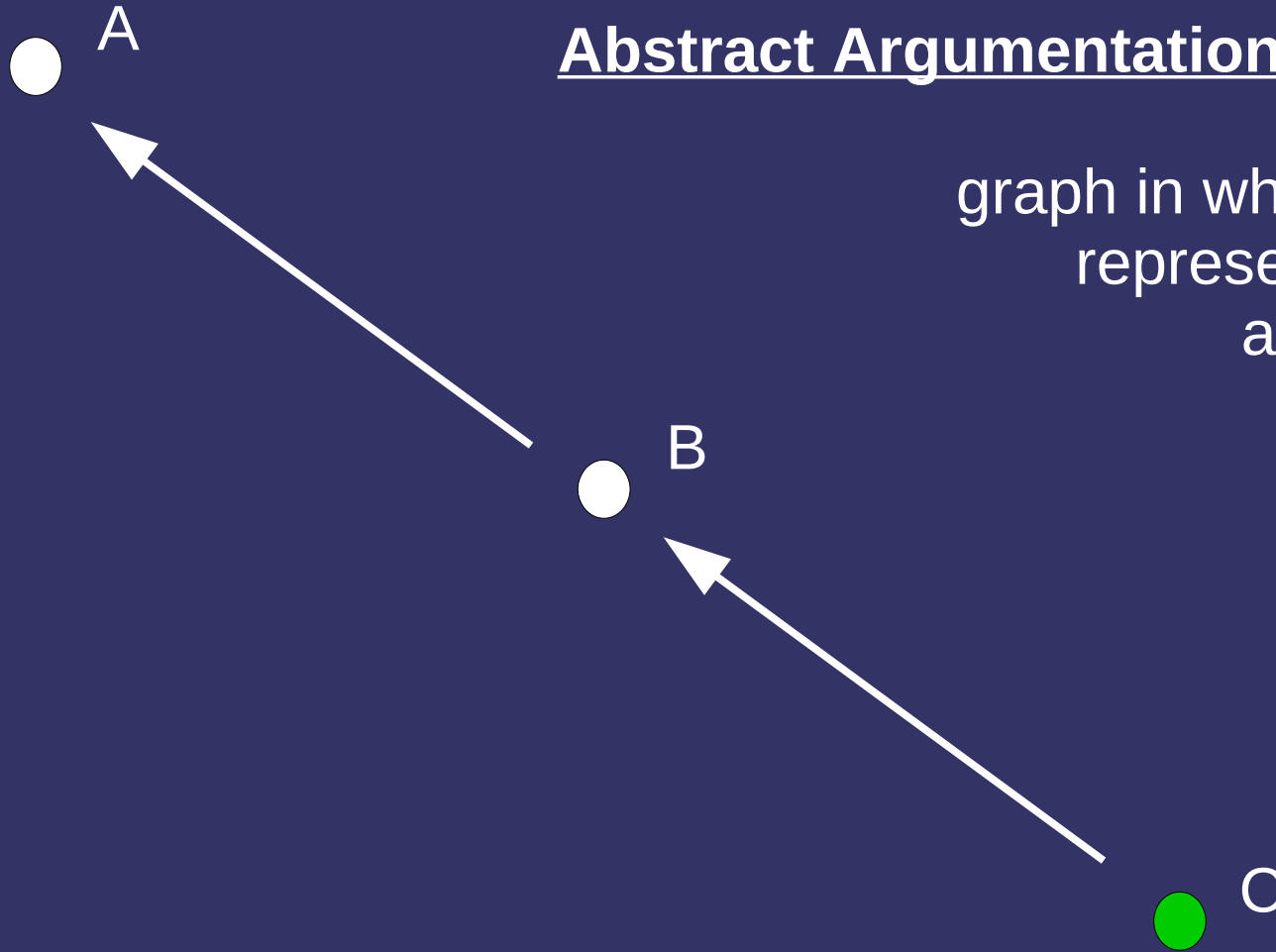
Abstraction



Abstract Argumentation Framework:

graph in which the nodes represent arguments and the arrows represent attacks

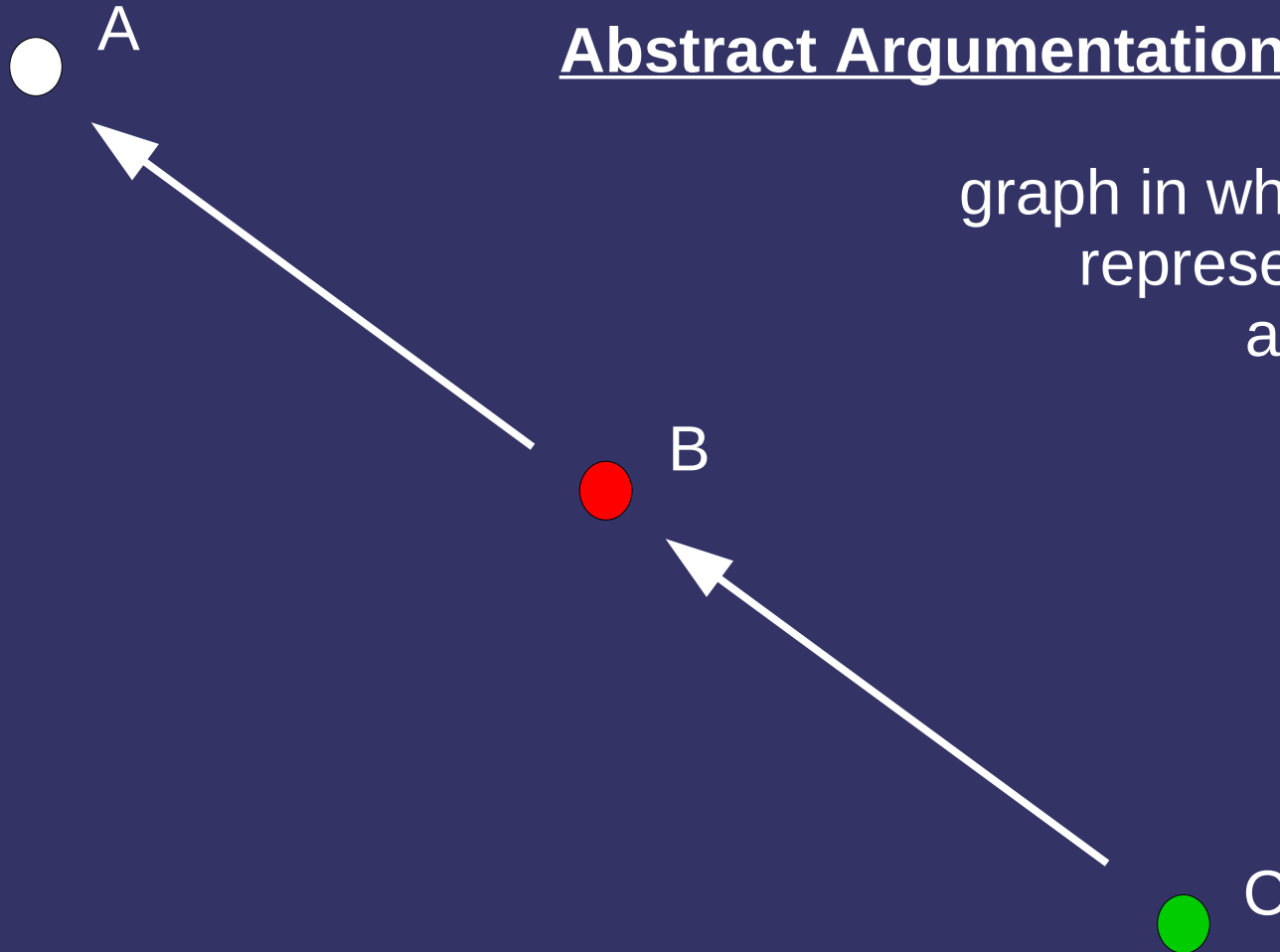
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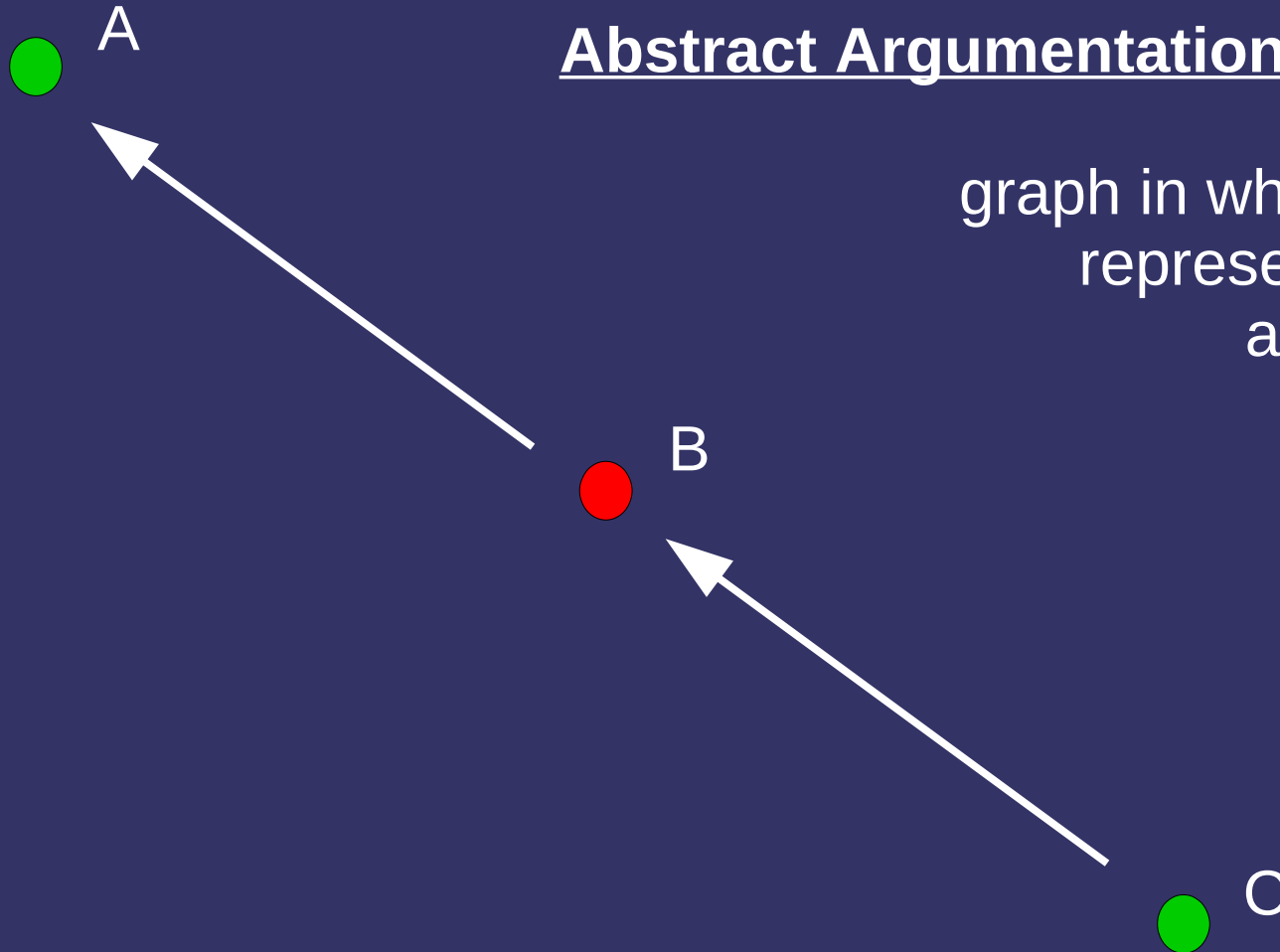
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Abstraction



Abstract Argumentation Framework:

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Next Topic

How do we evaluate an
argumentation framework?

(“*argumentation semantics*”)

Argument Labellings

Each argument is labelled **in**, **out** or undec

an argument is **in** \Leftrightarrow
all its attackers are **out**

an argument is **out** \Leftrightarrow
it has an attacker that is **in**

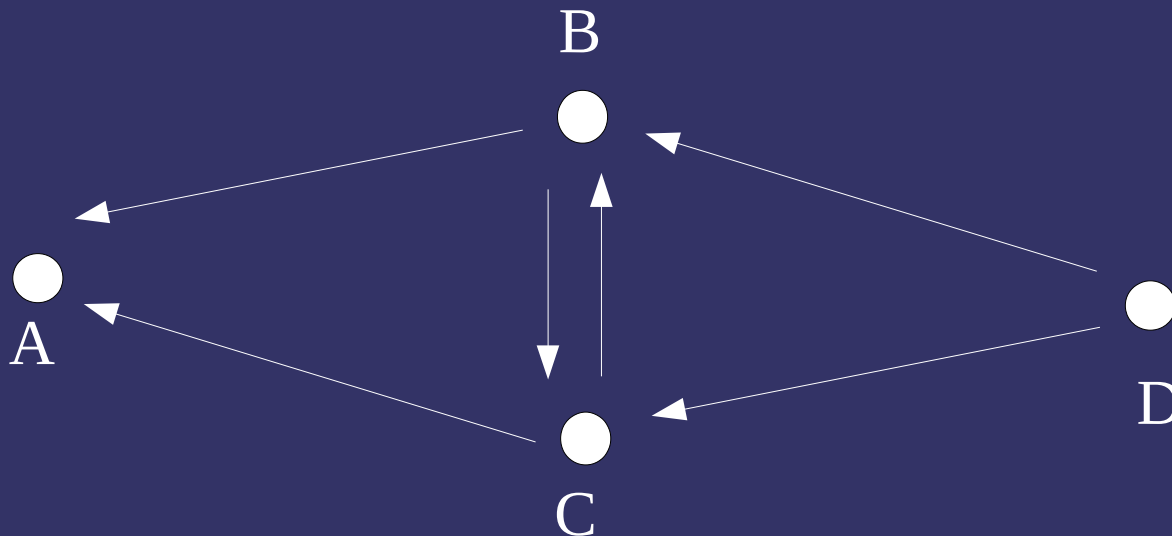
an argument is undec \Leftrightarrow
not all its attackers are **out**
and it does not have an attacker that is **in**

Applying Argument Labellings (1/3)

in \Leftrightarrow all attackers are **out**

out \Leftrightarrow there is an attacker that is **in**

undec \Leftrightarrow not all attackers are **out**, and no attacker is **in**

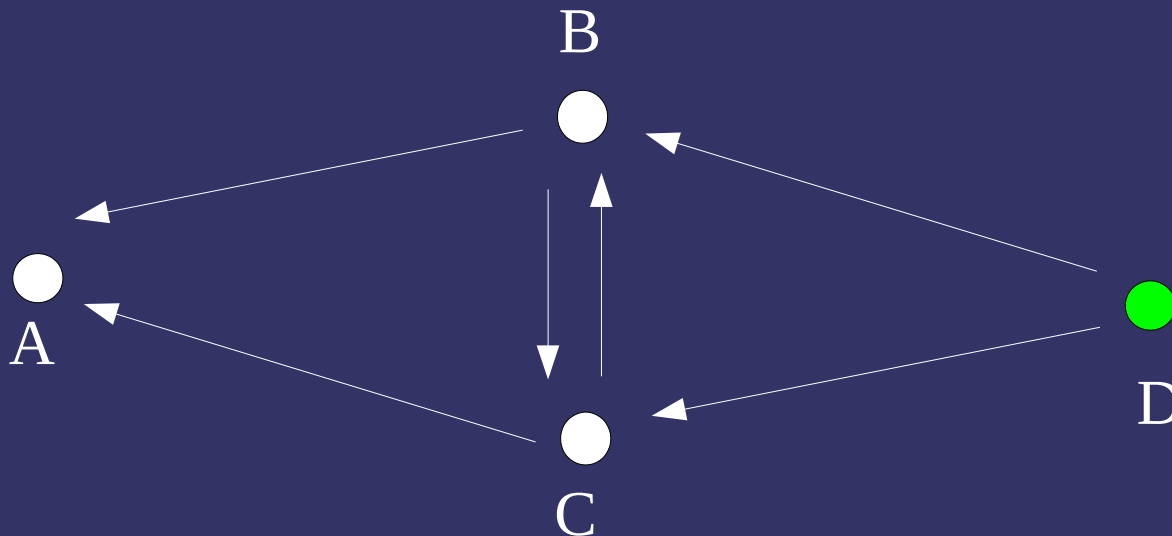


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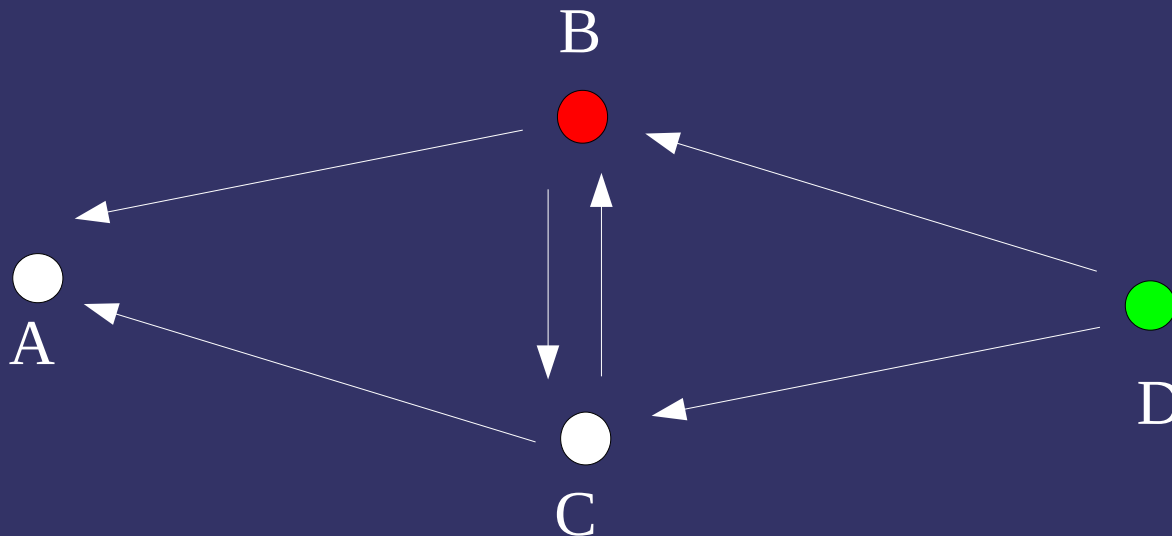


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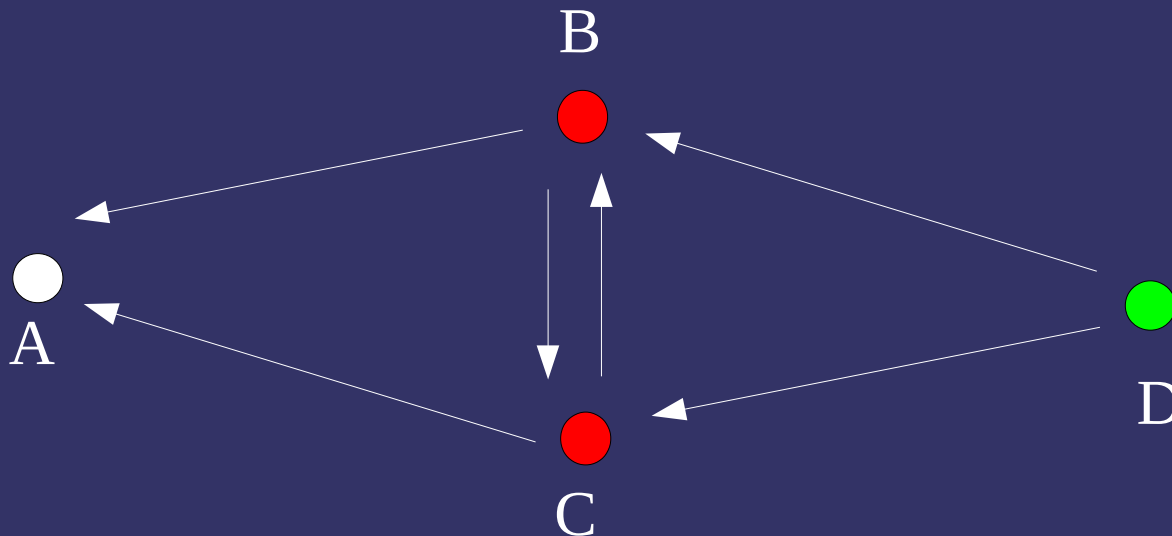


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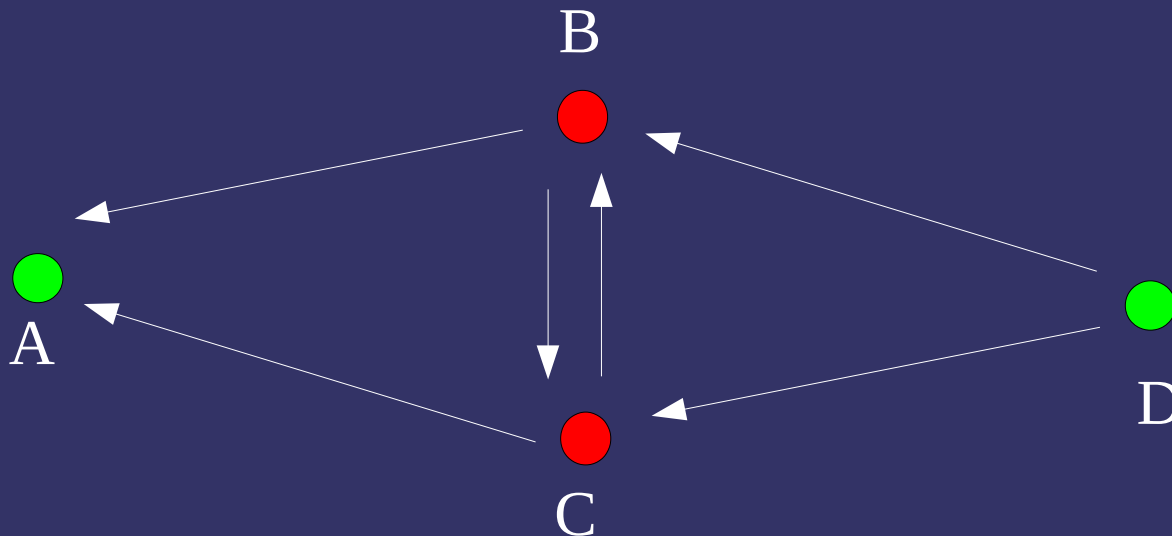


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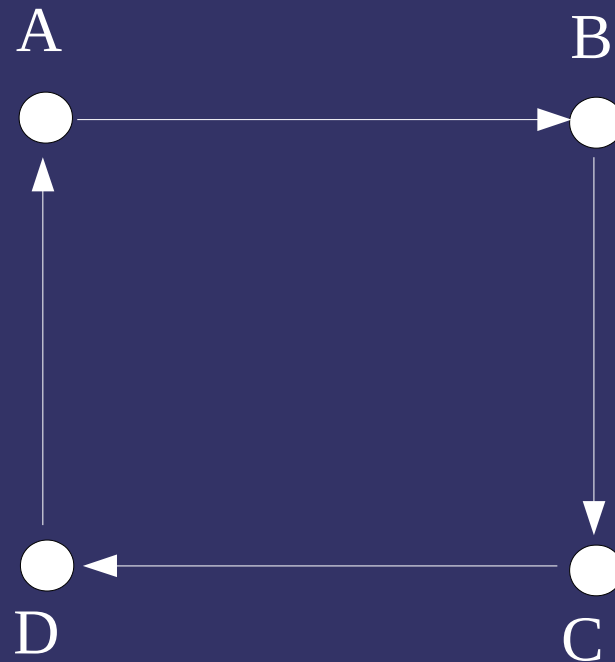
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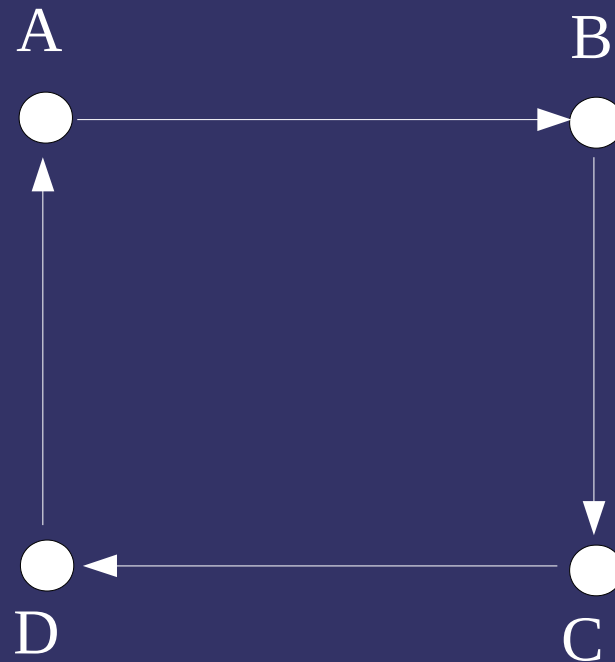
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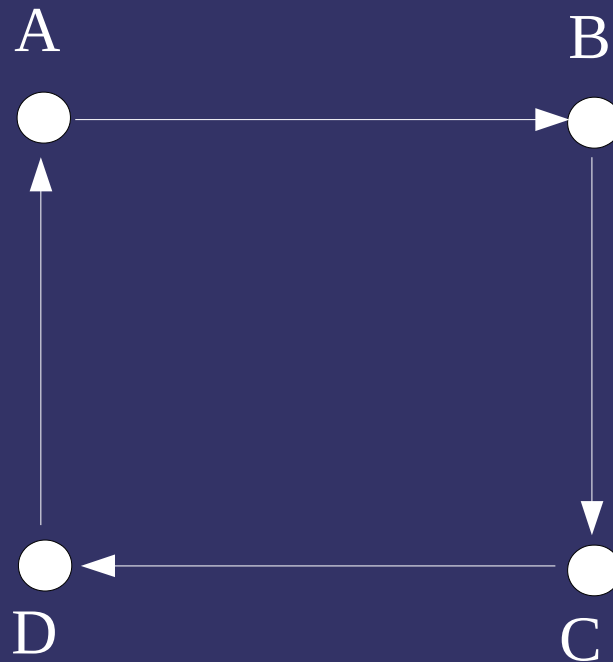
Applying Argument Labellings (2/3)



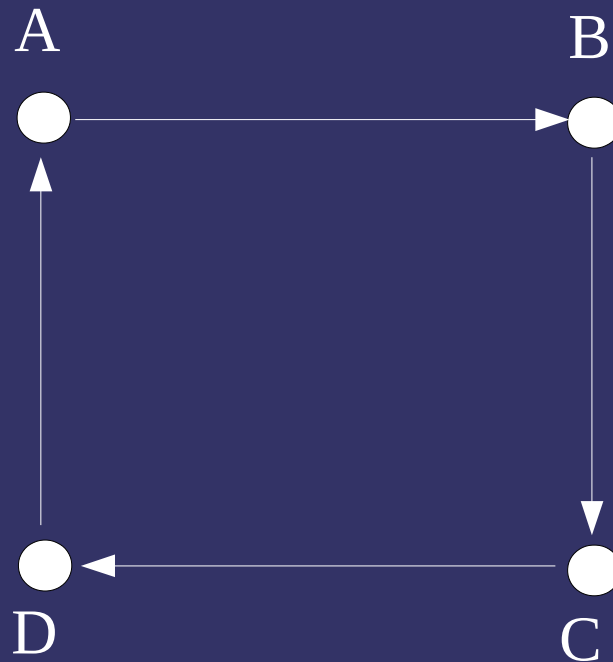
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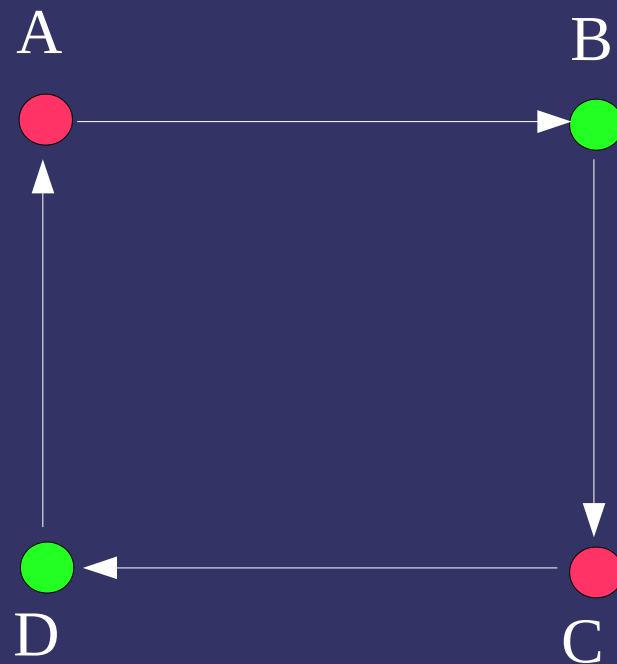
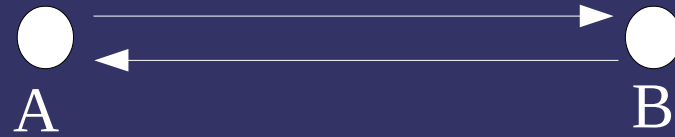
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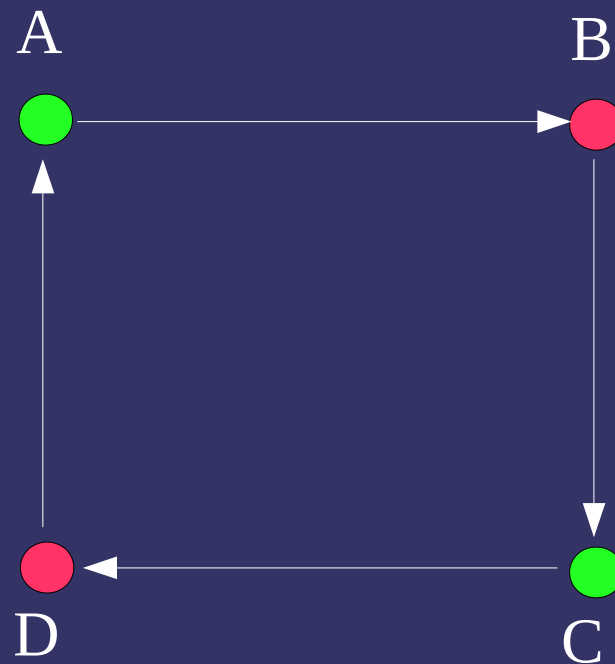
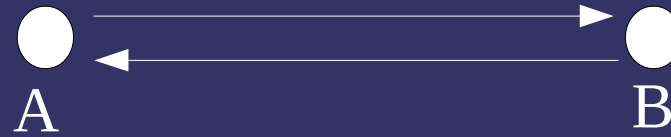
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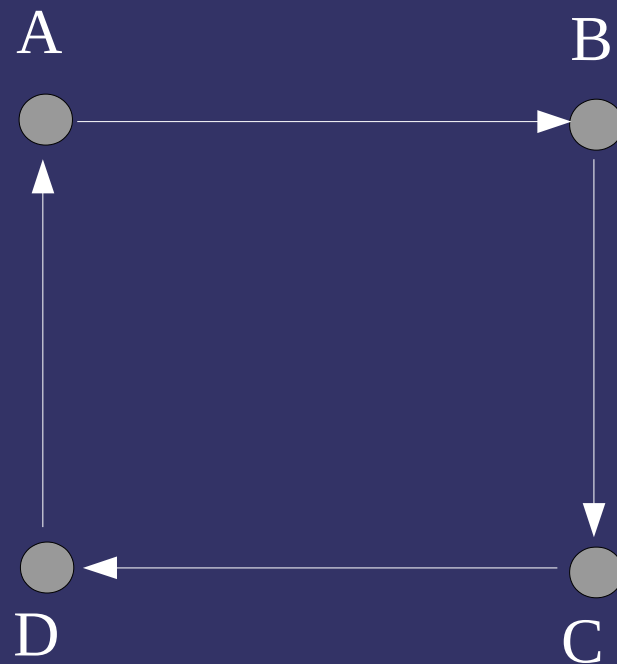
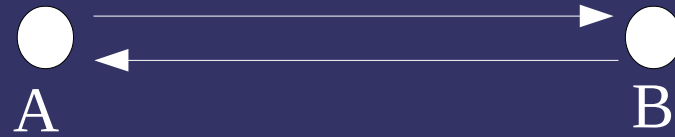
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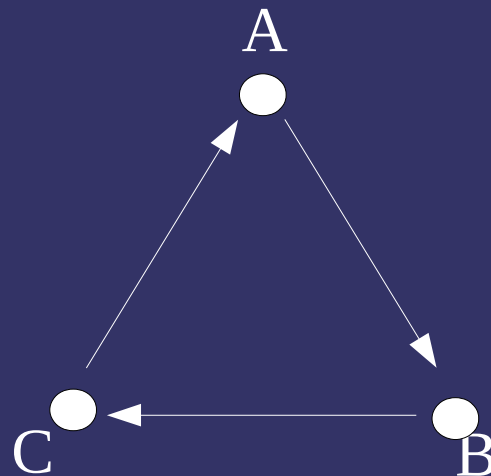
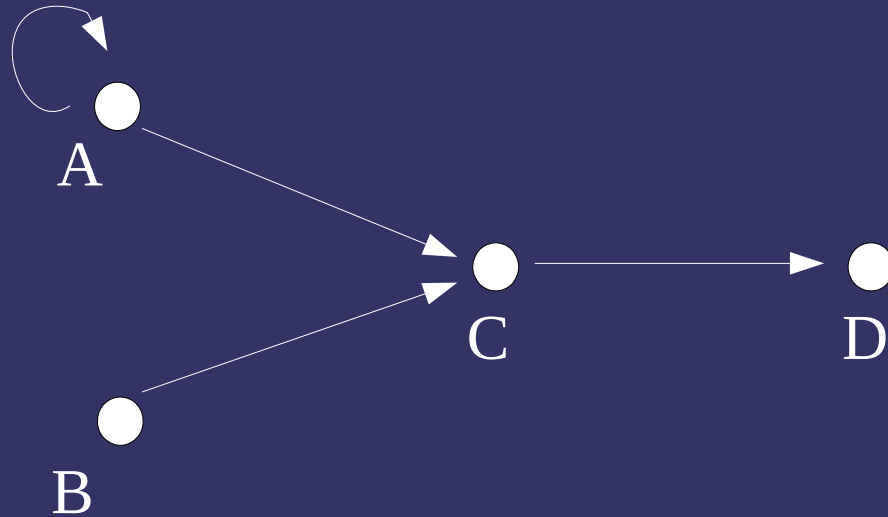
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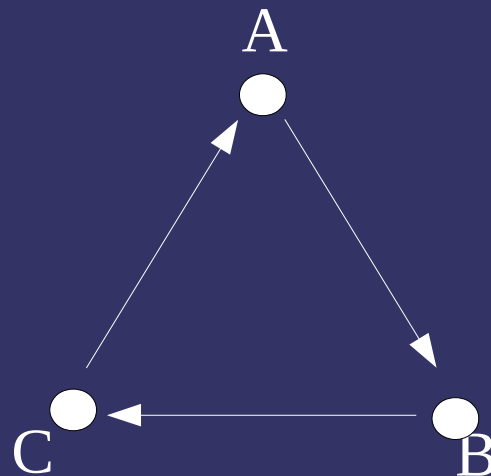
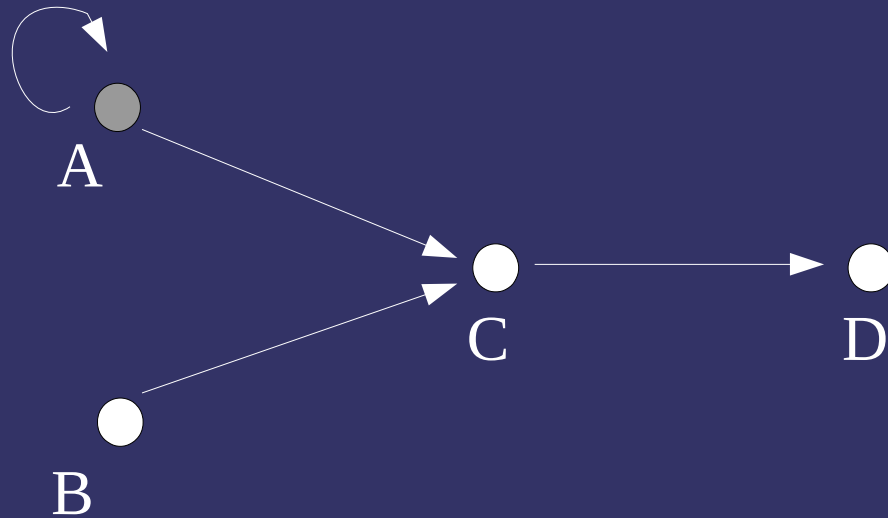
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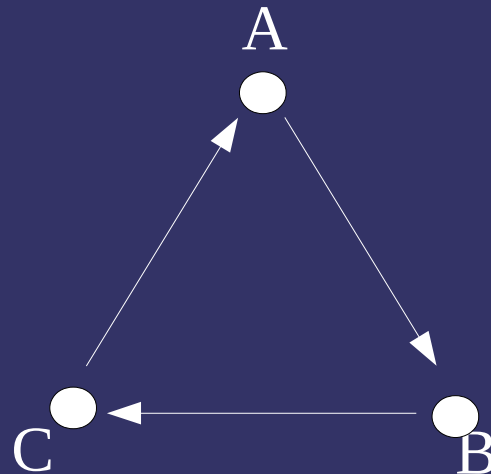
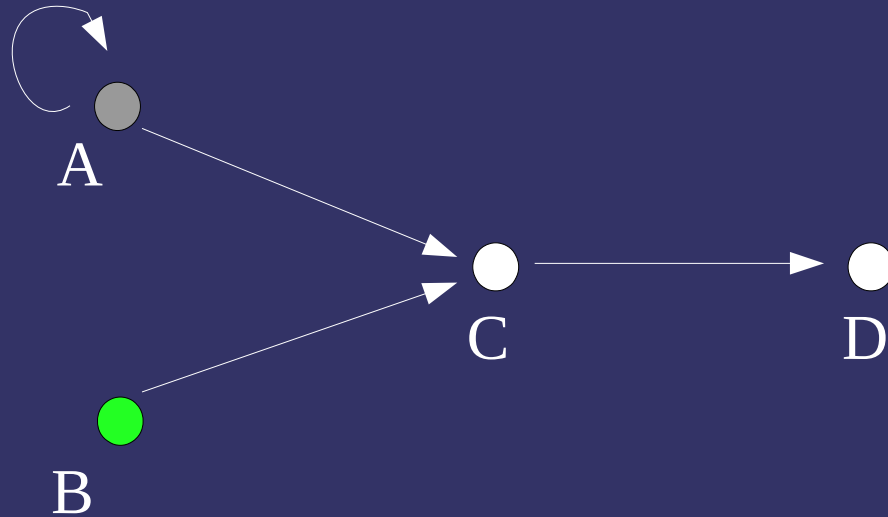
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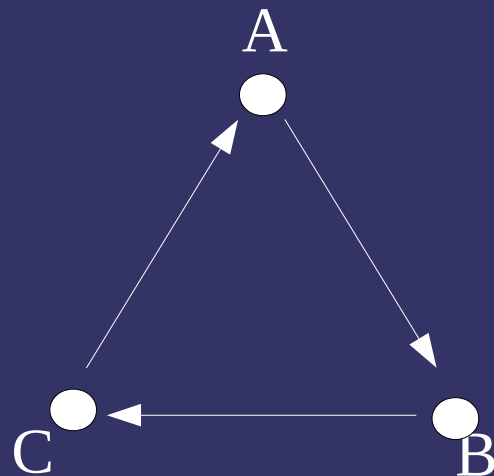
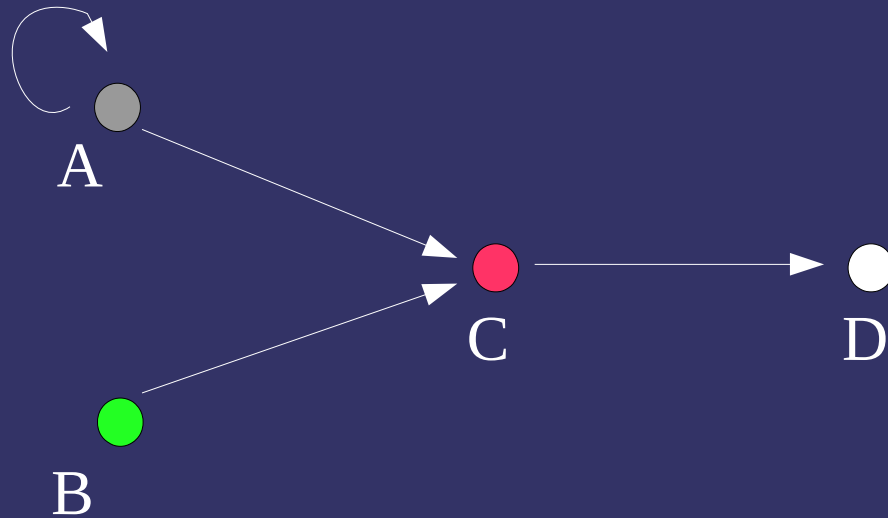
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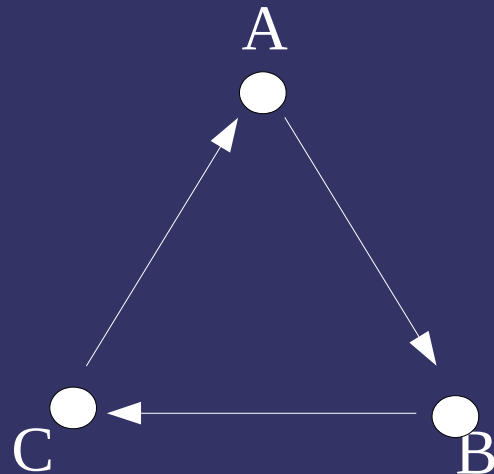
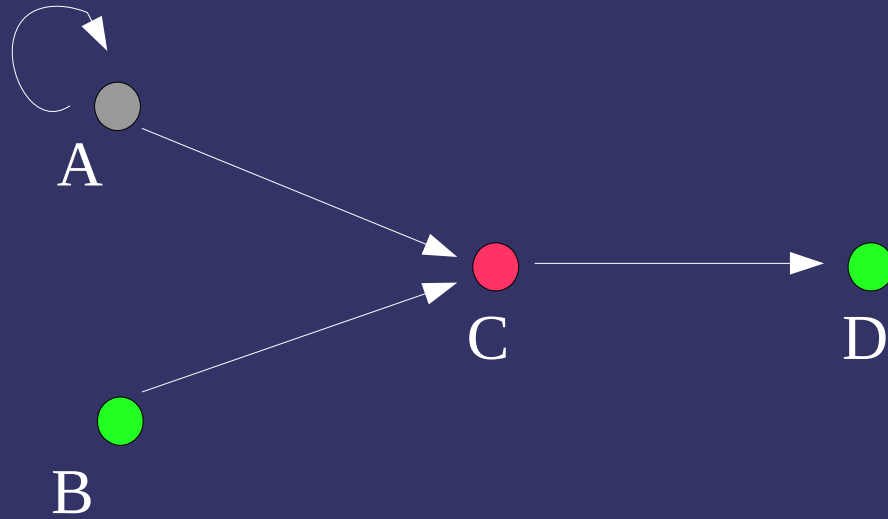
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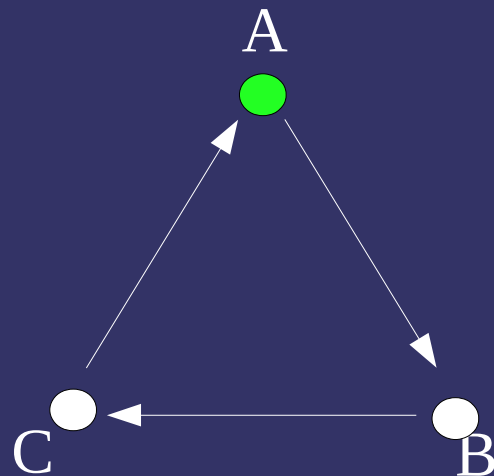
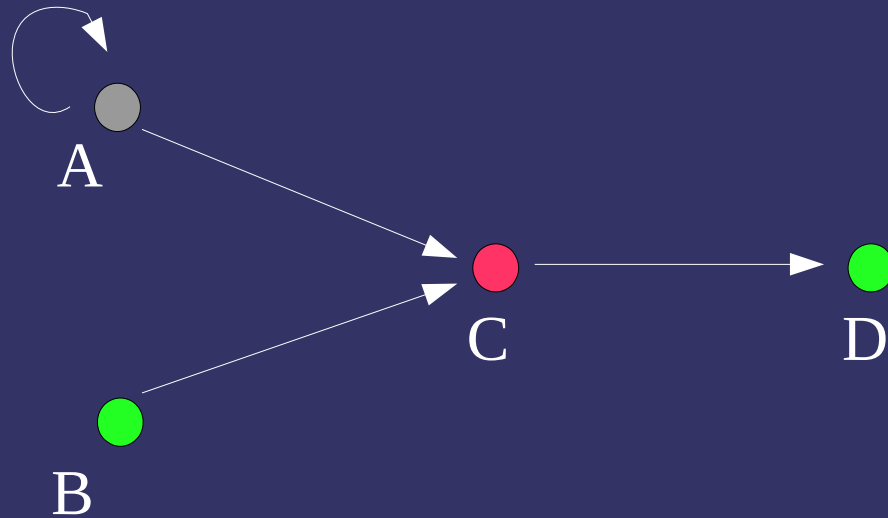
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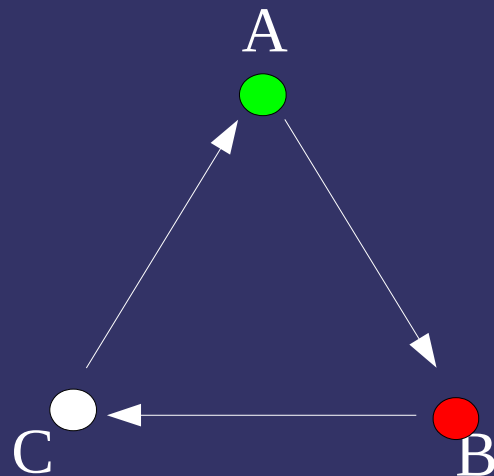
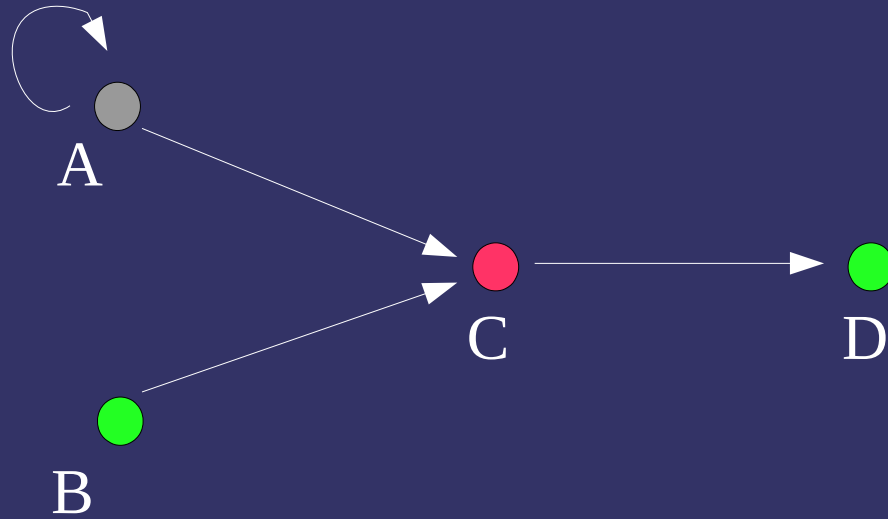
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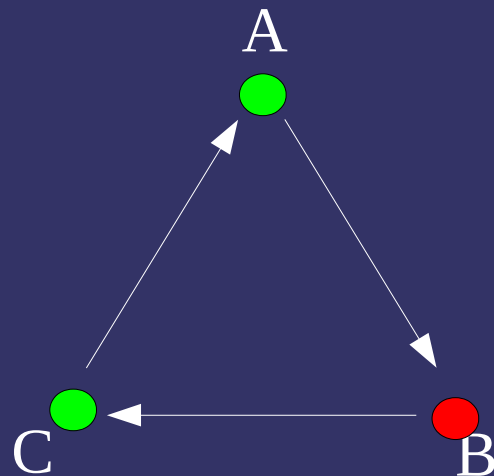
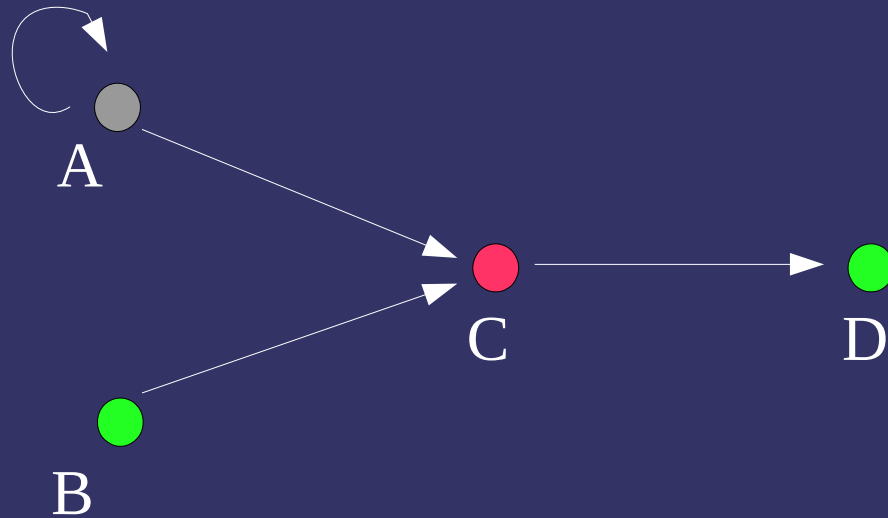
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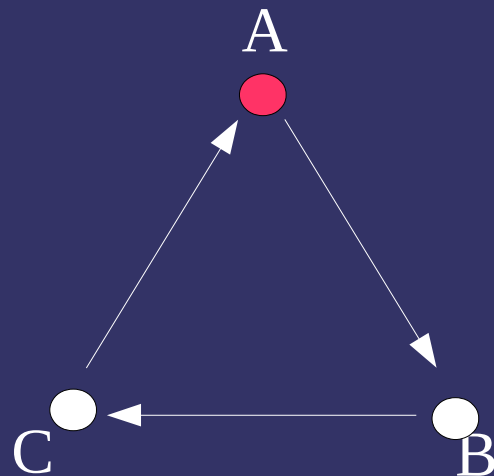
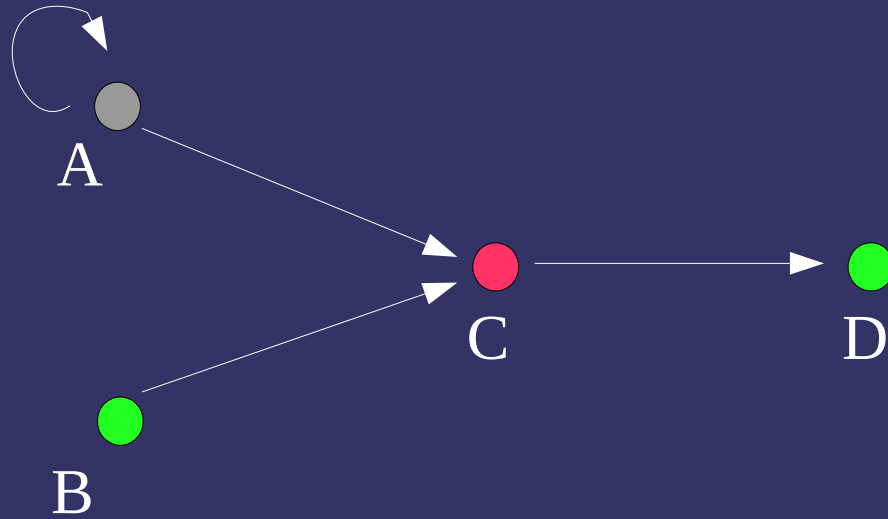
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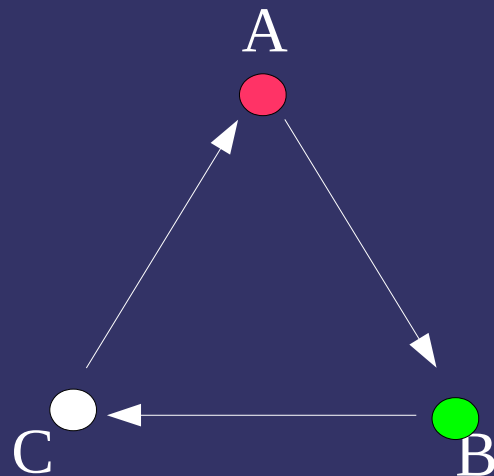
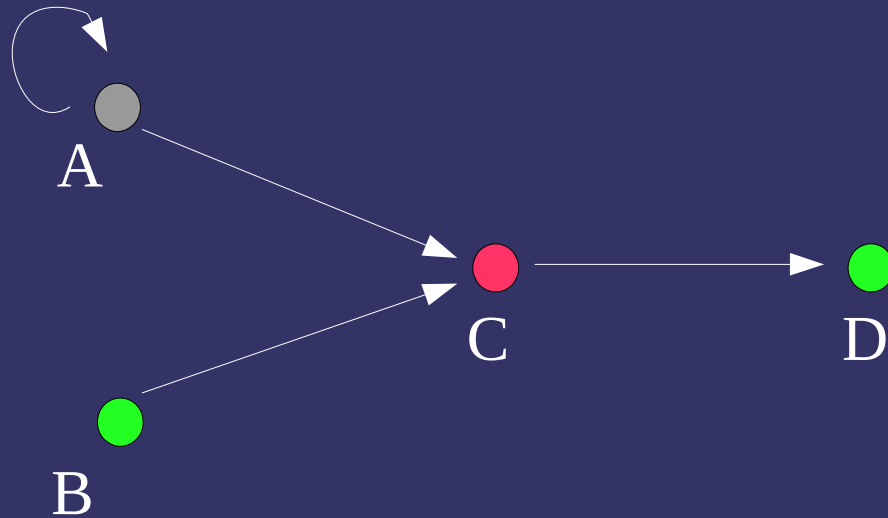
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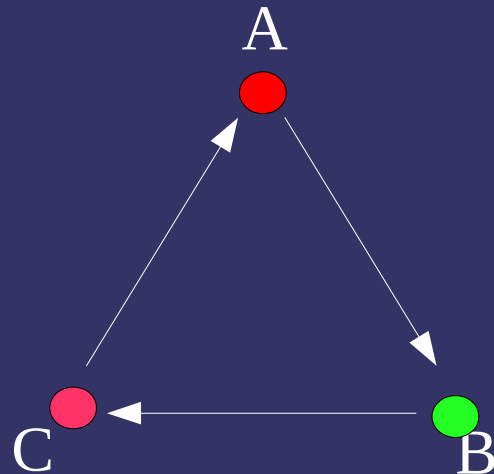
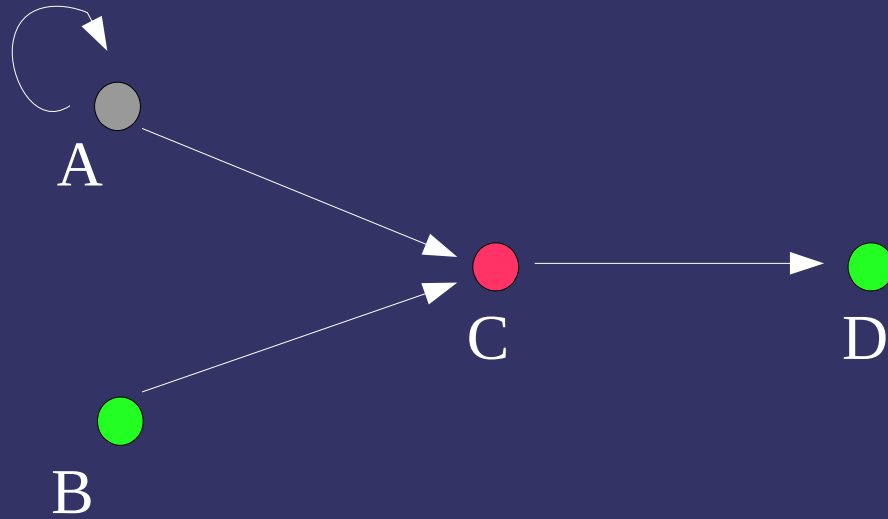
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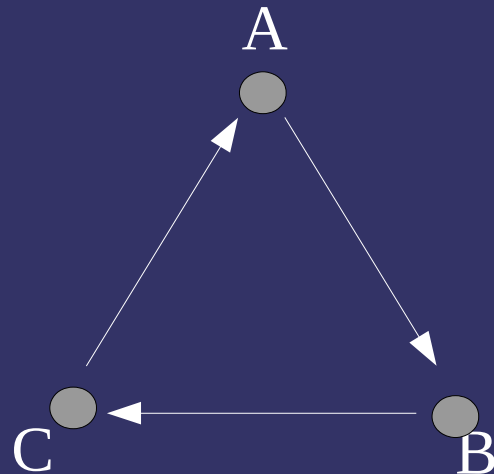
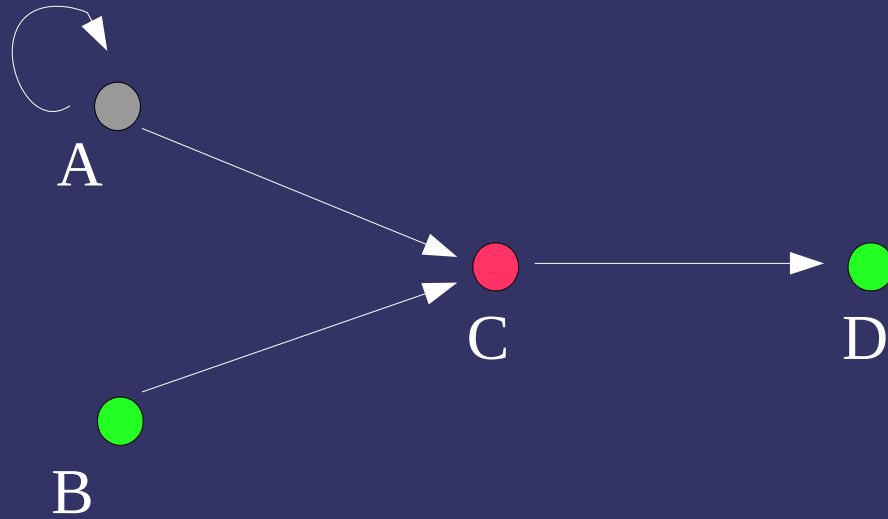
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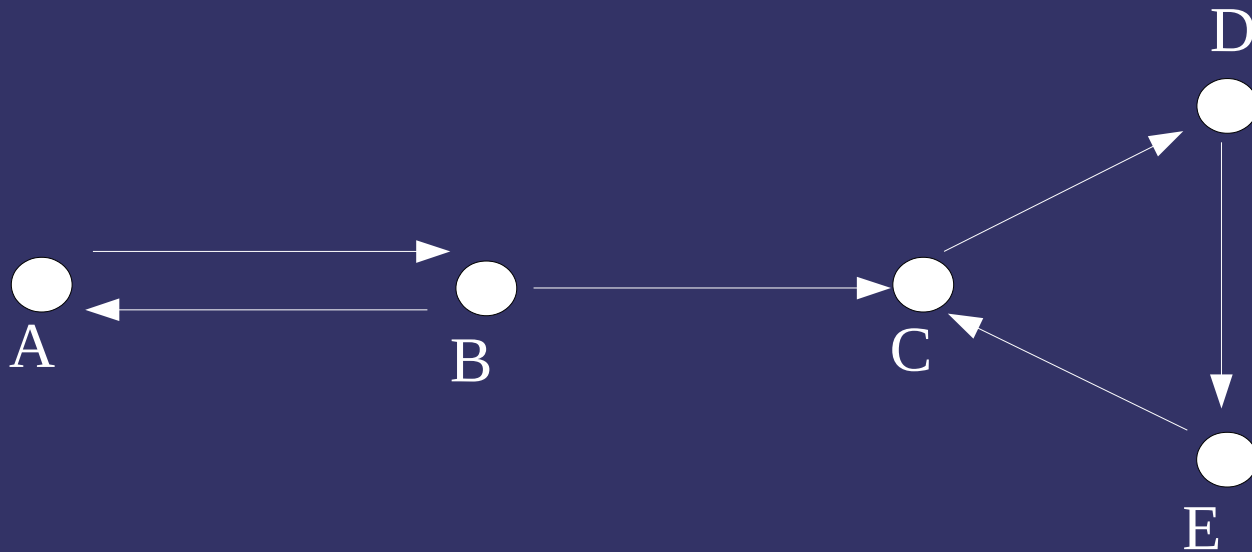
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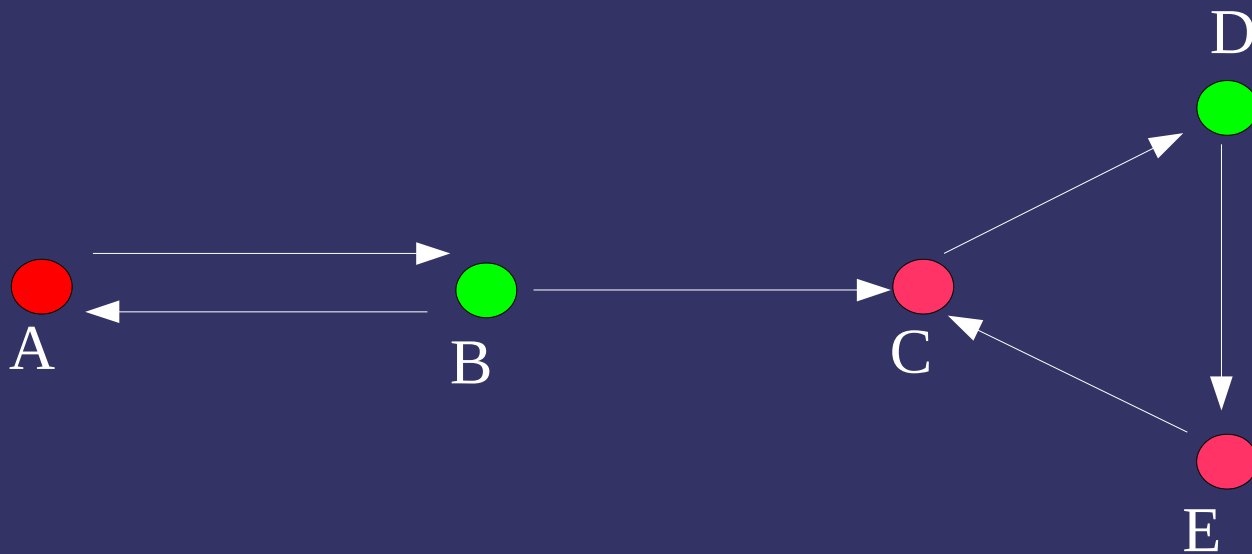


Exercise



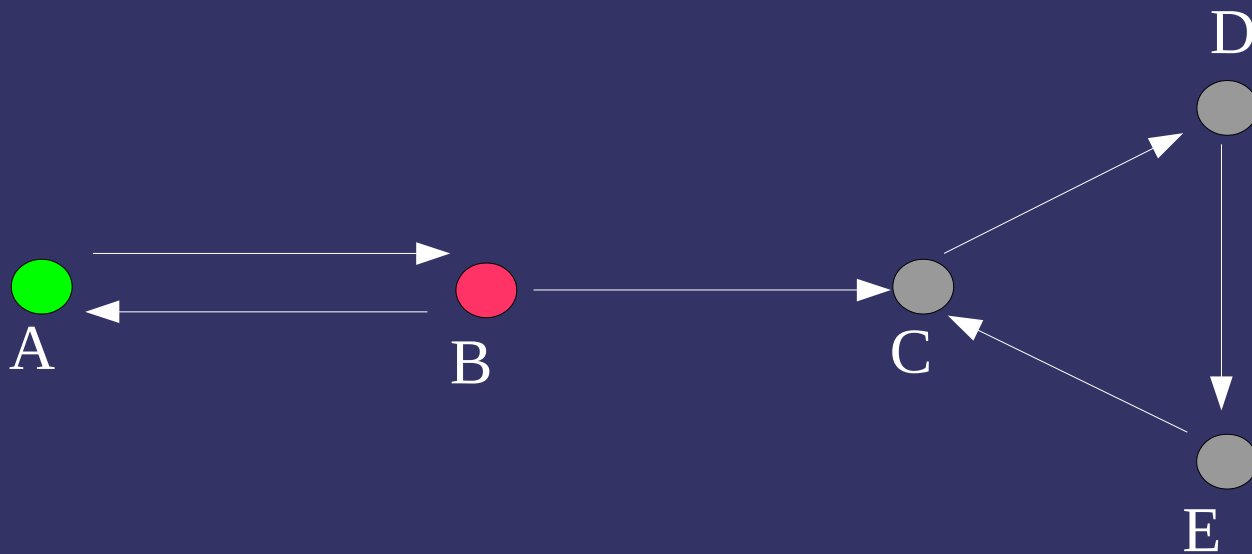
Give the three labellings of this argumentation framework

Exercise



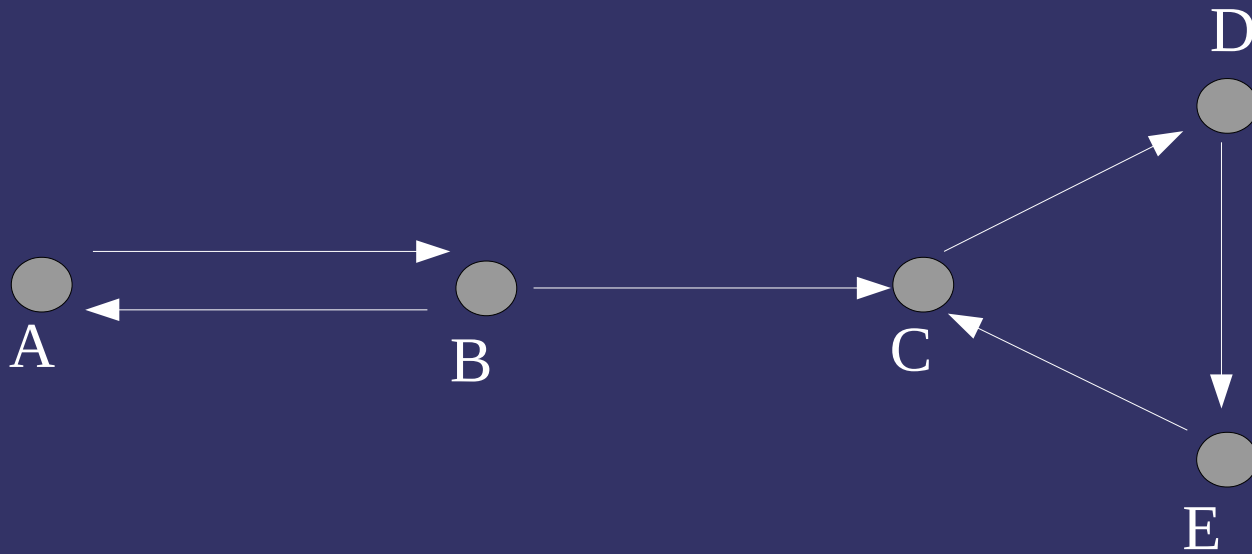
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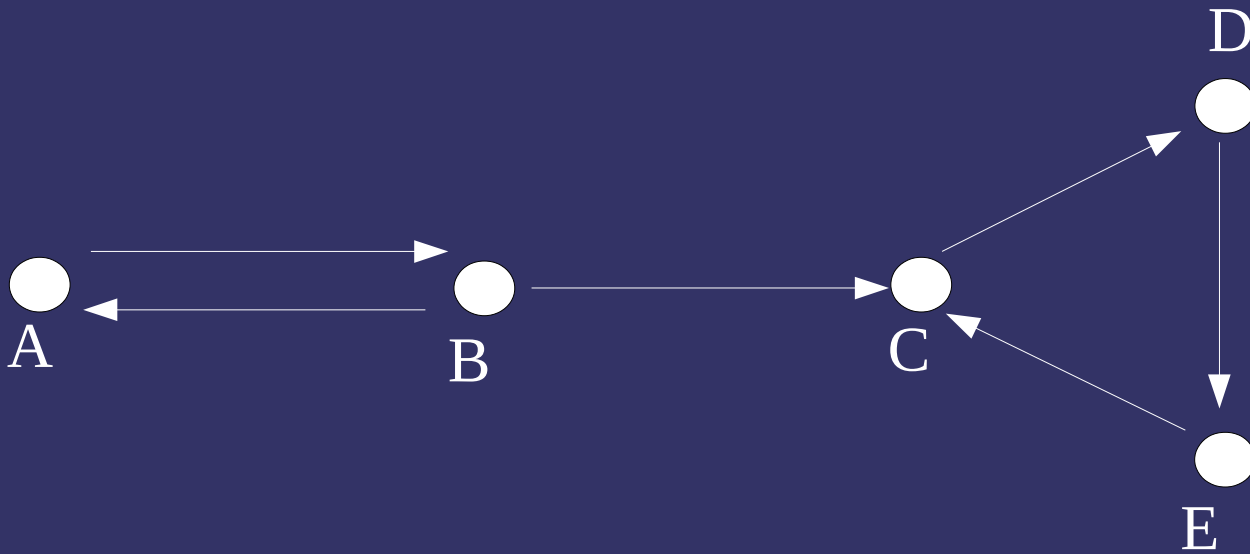
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Give the three labellings of this argumentation framework

Maximisation / Minimisation



A B C D E

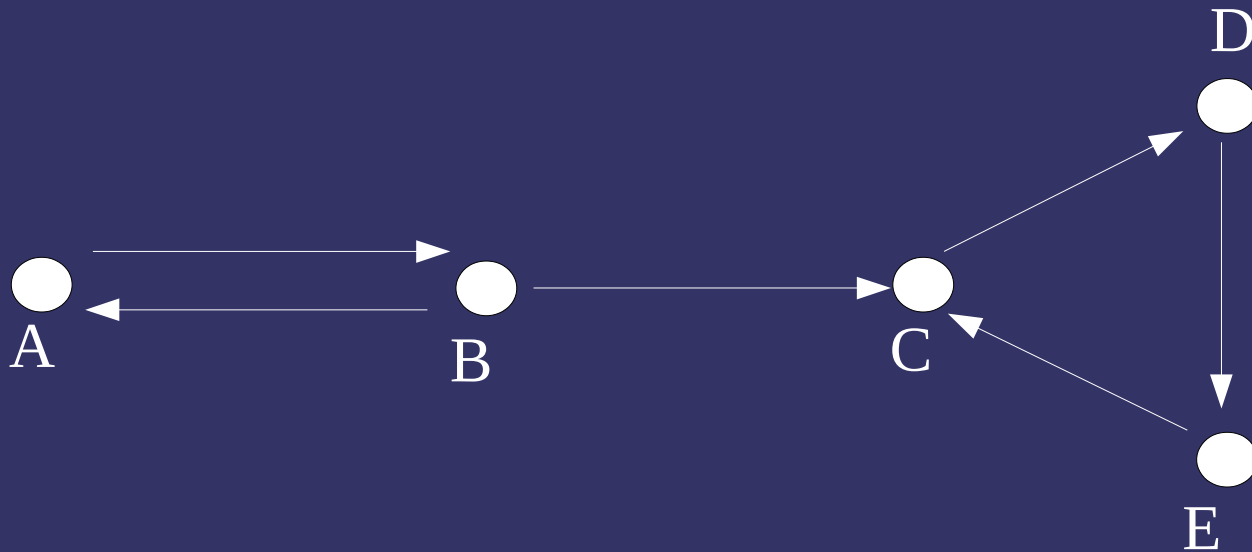
A B C D E

A B C D E

Maximisation / Minimisation

“maximal”: there is no other that has the same plus something

“minimal”: there is no other that has the same minus something



A B C D E

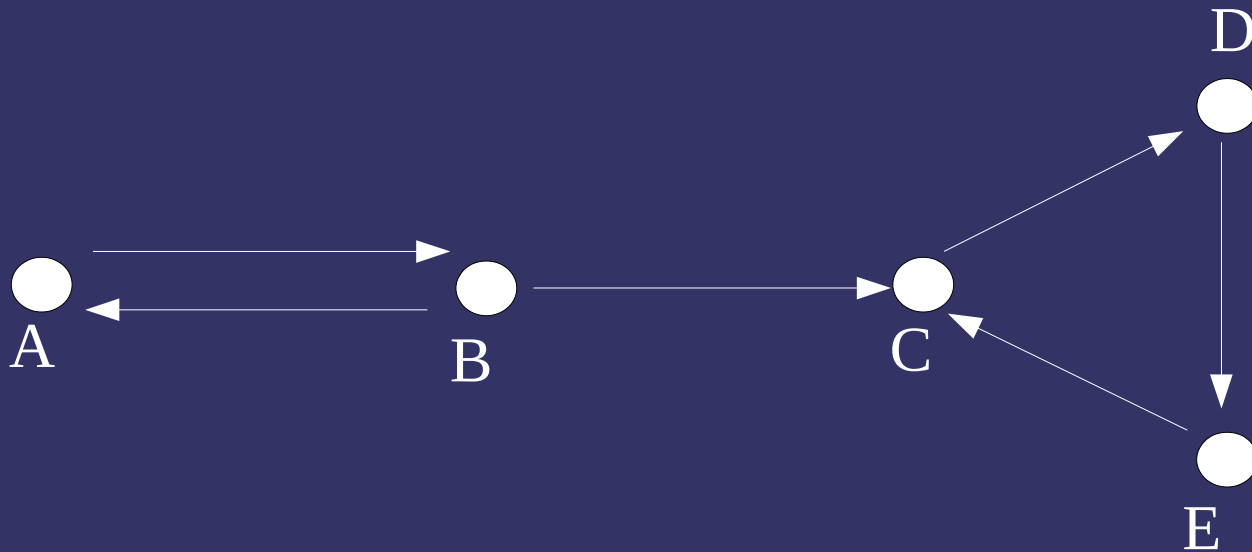
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Maximisation / Minimisation

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A B C D E max in, max out, min undec

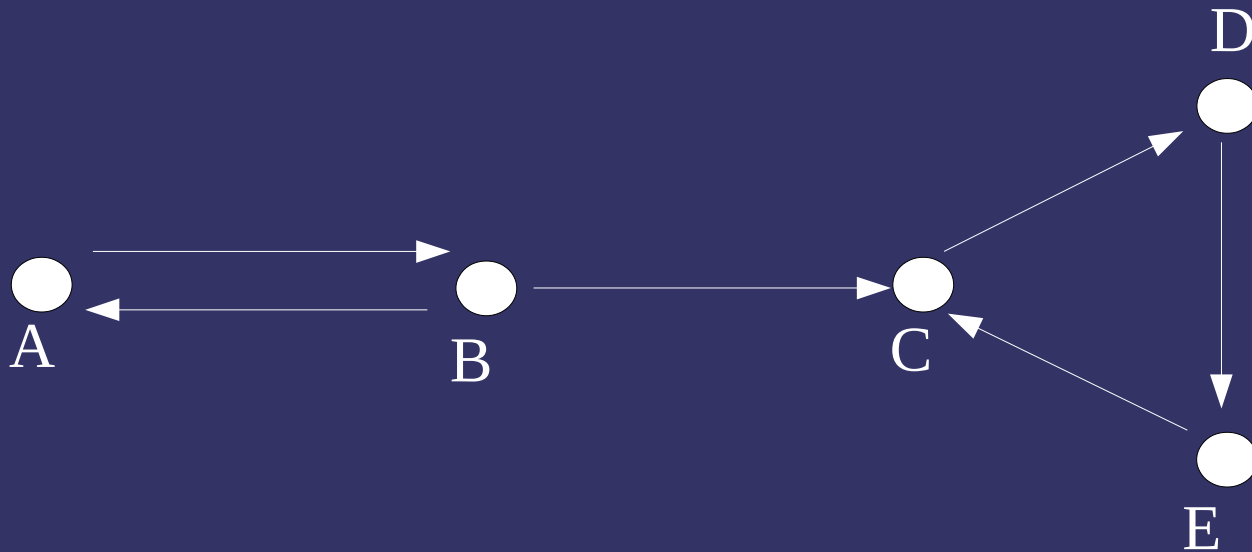
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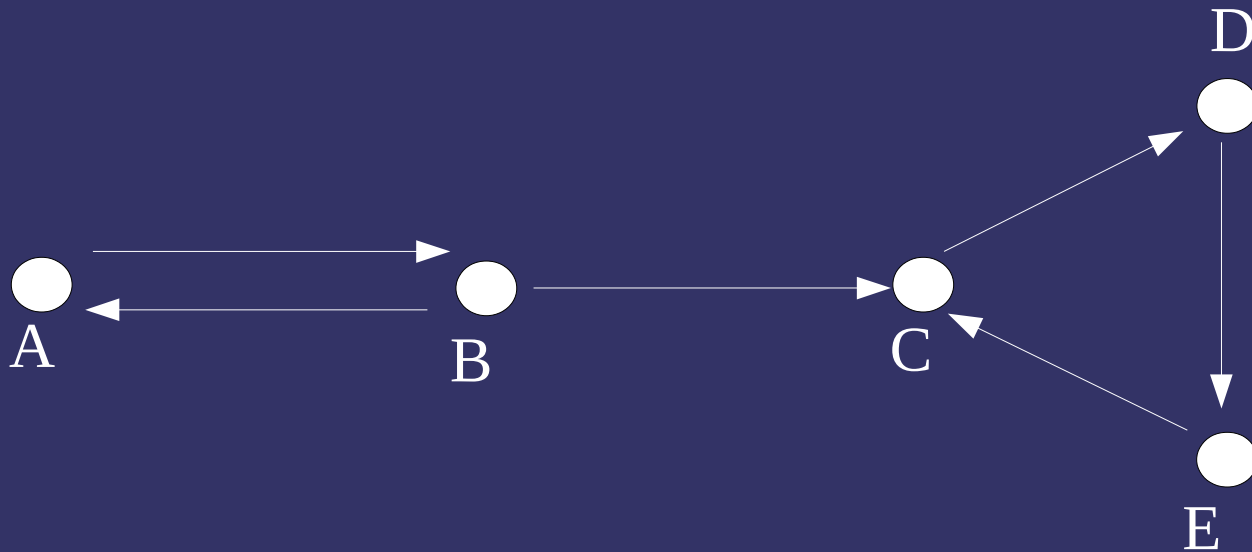
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A B C D E max in, max out

A B C D E min in, min out, max undec

Complete, Stable, Preferred, Grounded and Semi-Stable Labellings

in \Leftrightarrow all attackers are *out*

out \Leftrightarrow there is an attacker that is *in*

undec \Leftrightarrow not all attackers are *out*, and no attacker is *in*

restriction on compl. labeling

no further restrictions

empty undec

maximal *in*

maximal *out*

maximal undec

minimal *in*

minimal *out*

minimal undec

Dung-style semantics

complete semantics

stable semantics

preferred semantics

preferred semantics

grounded semantics

grounded semantics

grounded semantics

semi-stable semantics

Complete Labellings and Admissible Labellings

complete labelling:

in \Leftrightarrow all attackers are *out*

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Complete Labellings and Admissible Labellings

complete labelling:

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Complete Labellings and Admissible Labellings

admissible labelling:

in \Leftrightarrow all attackers are *out*

out \Leftrightarrow there is an attacker that is *in*

Roundup Labelling-Based Argumentation Semantics

admissible labelling:

in \Rightarrow all attackers are *out*
out \Rightarrow there is an attacker that is *in*

complete labelling:

in \Leftrightarrow all attackers are *out*
out \Leftrightarrow there is an attacker that is *in*
undec \Leftrightarrow not all attackers are *out*, and no attacker is *in*

grounded lab.: complete with min *in* / min *out* / max *undec*

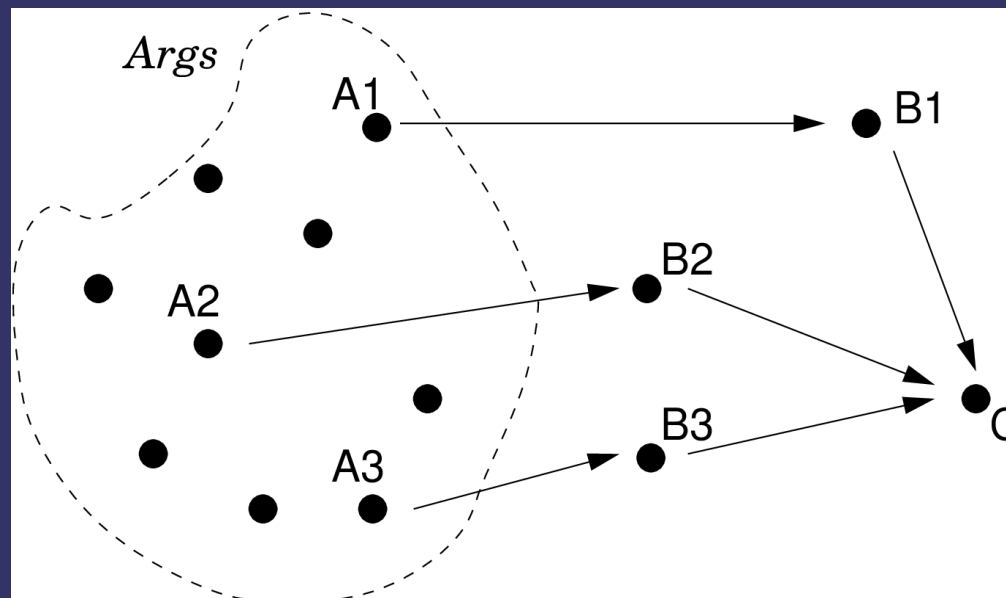
preferred lab.: complete with max *in* / max *out*

semi-stable lab.: complete with min *undec*

stable lab.: complete with no *undec*

Extension-Based Argumentation Semantics (1/2)

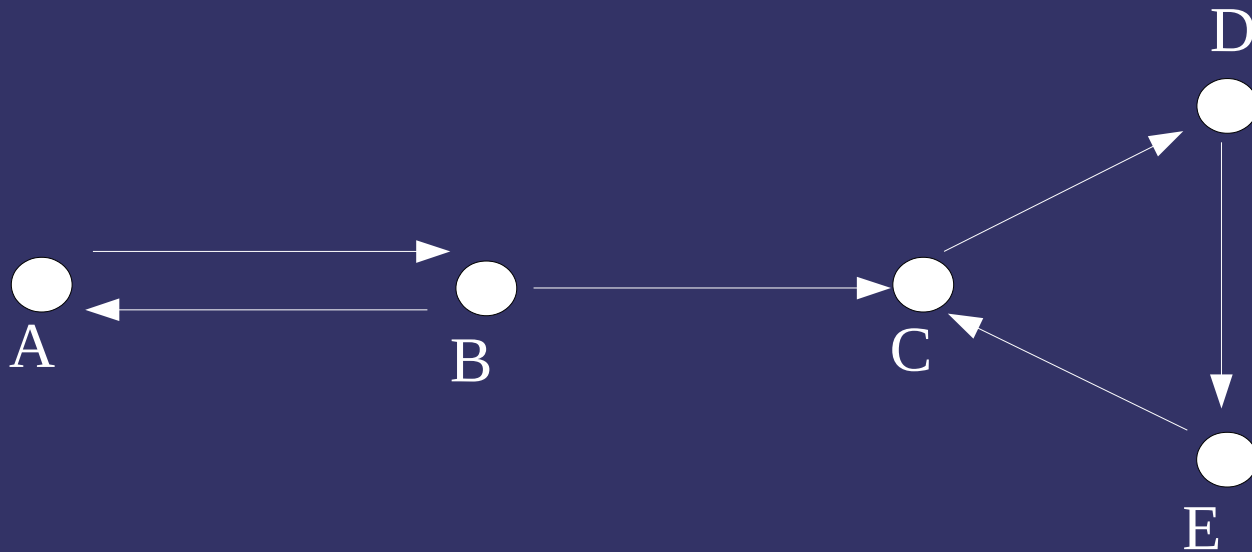
- $Args$ is conflict-free iff $Args$ does not contain A, B such that A attacks B
- $Args$ defends an argument C iff for each argument B that attacks C , $Args$ contains an argument (A) that attacks B



Extension-Based Argumentation Semantics (1/2)

- Args is conflict-free iff
 $\nexists A, B \in \text{Args}: A \text{ attacks } B$
- Args defends an argument C iff
 $\forall B \text{ that attacks } C:$
 $\exists A \in \text{Args}: A \text{ attacks } B$
- $F(\text{Args}) =$ all arguments defended by Args
- $\text{Args}^+ = \{ A \mid \exists B \in \text{Args}: B \text{ attacks } A \}$

Exercise



What are $\{B\}^+$ and $F(\{B\})$
answer: $\{A,C\}$ and $\{B,D\}$

Extension-Based Argumentation Semantics (2/2)

A set of arguments $Args$ is called:

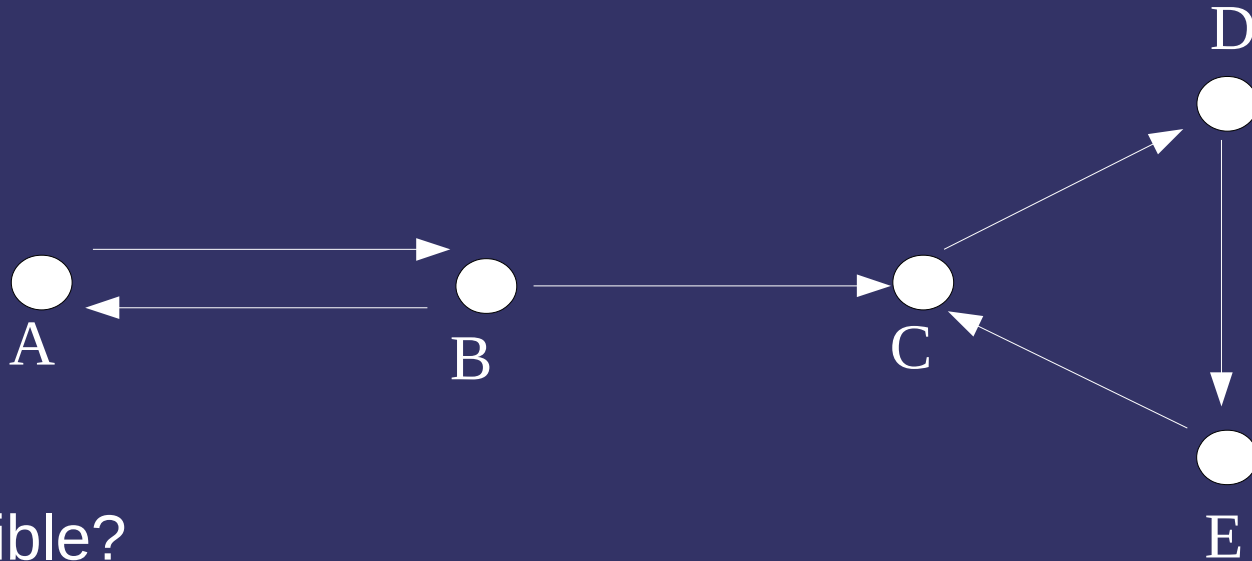
- admissible iff
 $Args$ is conflict-free and $Args \subseteq F(Args)$
- a complete extension iff
 $Args$ is conflict-free and $Args = F(Args)$
- a grounded extension iff
 $Args$ is the minimal complete extension
- a preferred extension iff
 $Args$ is a maximal admissible set
- a stable extension iff $Args$ is a conflict-free set that attacks everything not in it
- a semi-stable extension iff $Args$ is an admissible set with $Args \cup Args^+$ maximal

Extension-Based Argumentation Semantics (2/2)

A set of arguments $Args$ is called:

- admissible iff
 $Args$ is conflict-free and $Args \subseteq F(Args)$
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- a stable extension iff $Args$ is a complete extension that attacks everything not in it
- a semi-stable extension iff $Args$ is a complete extension with $Args \cup Args^+$ maximal

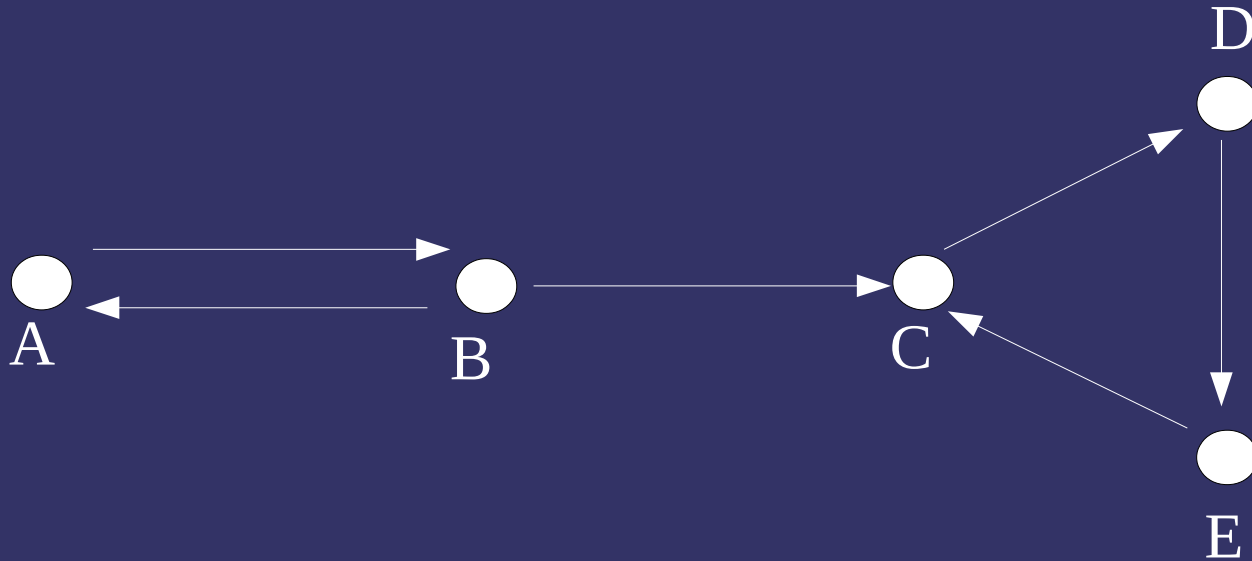
Exercise



Admissible?

- \emptyset
- {A}
- {B}
- {C}
- {D}
- {B,D}
- {A,B}

Exercise



Complete
Extensions:

\emptyset
{A}
{B,D}

Grounded
Extension:

\emptyset

Preferred
Extensions:

{A}
{B,D}

Stable
Extensions:

{B,D}

Semi-Stable
Extensions:

{B,D}

Extension-Based semantics vs. Labelling-Based Semantics

Let $\text{Lab} = (\text{in}(\text{Lab}), \text{out}(\text{Lab}), \text{undec}(\text{Lab}))$

Let Args be a conflict-free set of arguments.

We define:

- $\text{Lab2Ext}(\text{Lab}) = \text{in}(\text{Lab})$
- $\text{Ext2Lab}(\text{Args}) = (\text{Args}, \text{Args}^+, \text{Ar} \setminus (\text{Args} \cup \text{Args}^+))$

It holds that:

- If Lab is a complete labelling,
then $\text{Lab2Ext}(\text{Lab})$ is a complete extension
- If Args is a complete extension,
then $\text{Ext2Lab}(\text{Args})$ is a complete labelling
- For complete labellings/extensions
 Lab2Ext and Ext2Lab are each other's inverse functions

Extension-Based semantics vs. Labelling-Based Semantics

complete labelling \equiv complete extension
grounded labelling \equiv grounded extension
preferred labelling \equiv preferred extension
semi-stable labelling \equiv semi-stable extension
stable labelling \equiv stable extension

(equivalence through Lab2Ext and Ext2Lab)

take home message:

*An extension is
the in-labelled part of a labelling*

Next Topic

What is the relation between
argumentation semantics
and discussion?

Grounded Discussion Game
Preferred Discussion Game

Next Topic

The Grounded Discussion Game

***A Discussion Game
for Grounded Semantics (1/3)***

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

four moves ($A, B \in Ar$)

(1) P: HTB(A)

“A has to be the case”

(2) O: CB(B)

“B can be the case”

(3) O: CONCEDE(A)

“I now agree that A”

(4) O: RETRACT(B)

“I no longer hold that B can be the case”

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

four moves ($A, B \in Ar$)

(1) P: HTB(A)

“A is labelled **in** by every complete”

(2) O: CB(B)

“B can be the case”

(3) O: CONCEDE(A)

“I now agree that A”

(4) O: RETRACT(B)

“I no longer hold that B can be the case”

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

four moves ($A, B \in Ar$)

(1) P: HTB(A)

“A is labelled **in** by every complete”

(2) O: CB(B)

“Perhaps B isn't labelled **out** by every complete”

(3) O: CONCEDE(A)

“I now agree that A”

(4) O: RETRACT(B)

“I no longer hold that B can be the case”

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

four moves ($A, B \in Ar$)

(1) P: HTB(A)

“A is labelled **in** by every complete”

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“Perhaps B isn't labelled **out** by every complete”

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“I now agree that A is labelled **in** by every complete”

(4) O: RETRACT(B)

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A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
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four moves ($A, B \in Ar$)

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“A is labelled **in** by every complete”

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“Perhaps B isn't labelled **out** by every complete”

(3) O: CONCEDE(A)

“I now agree that A is labelled **in** by every complete”

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“I no longer hold that B isn't labelled **out** by every complete”

A Discussion Game for Grounded Semantics (1/3)

two players:

- proponent (P)
- opponent (O)

four moves ($A, B \in Ar$)

(1) P: HTB(A)

“A is labelled **in** by every complete”

(2) O: CB(B)

“Perhaps B isn't labelled **out** by every complete”

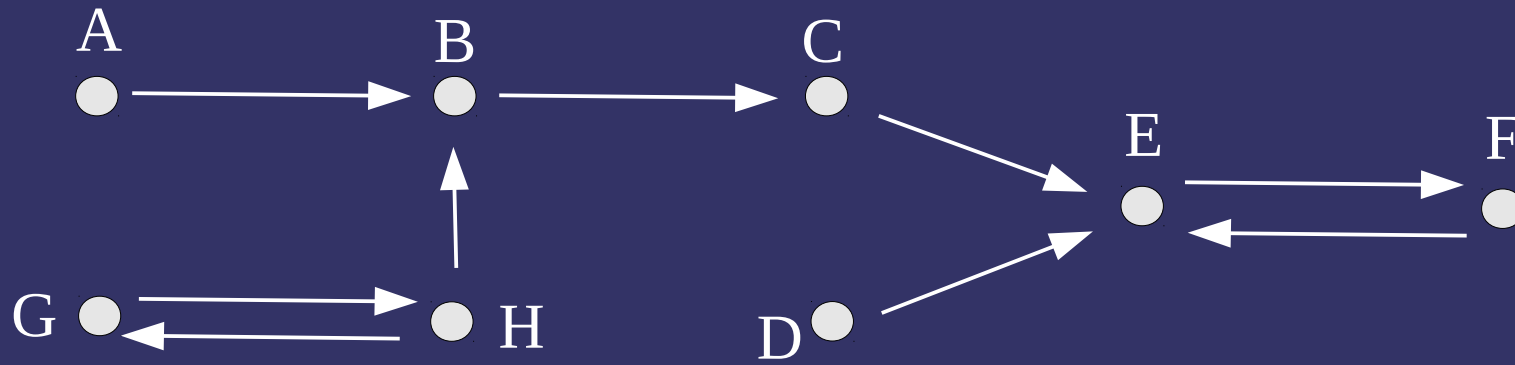
(3) O: CONCEDE(A)

“I now agree that A is labelled **in** by every complete”

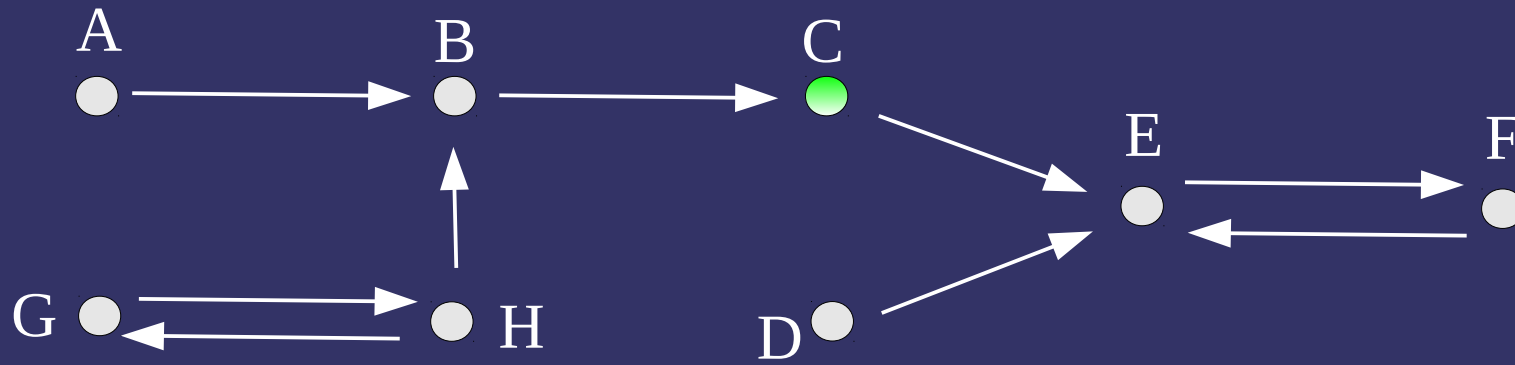
(4) O: RETRACT(B)

“I now think that B is labelled **out** by every complete”

Example

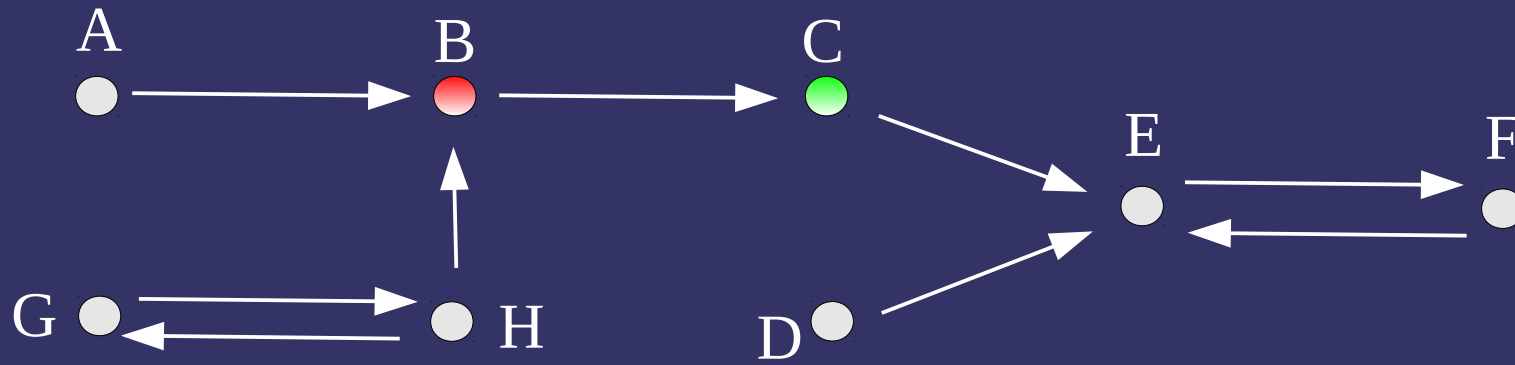


Example



P: HTB(C)

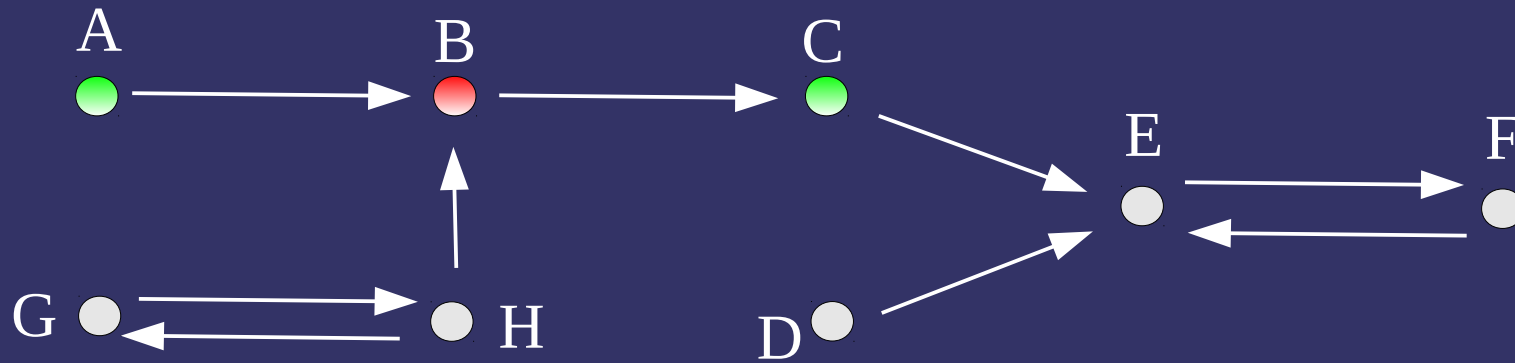
Example



P: HTB(C)

O: CB(B)

Example

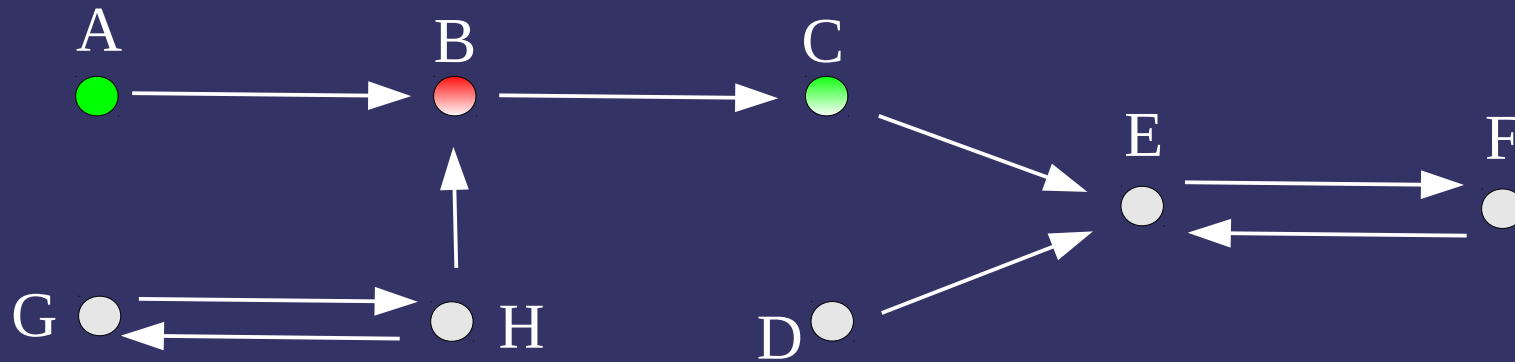


P: HTB(C)

O: CB(B)

P: HTB(A)

Example



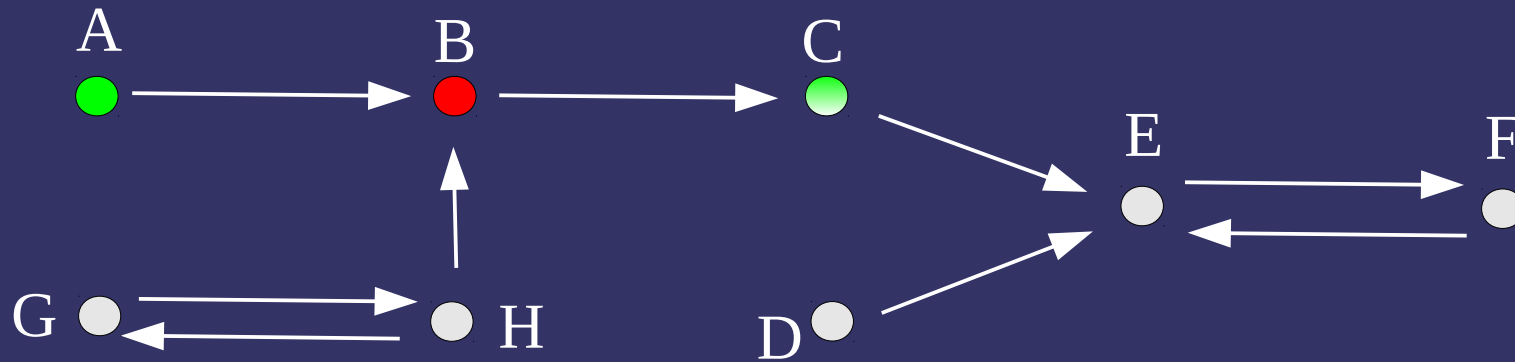
P: HTB(C)

O: CB(B)

P: HTB(A)

O: CONCEDE(A)

Example



P: HTB(C)

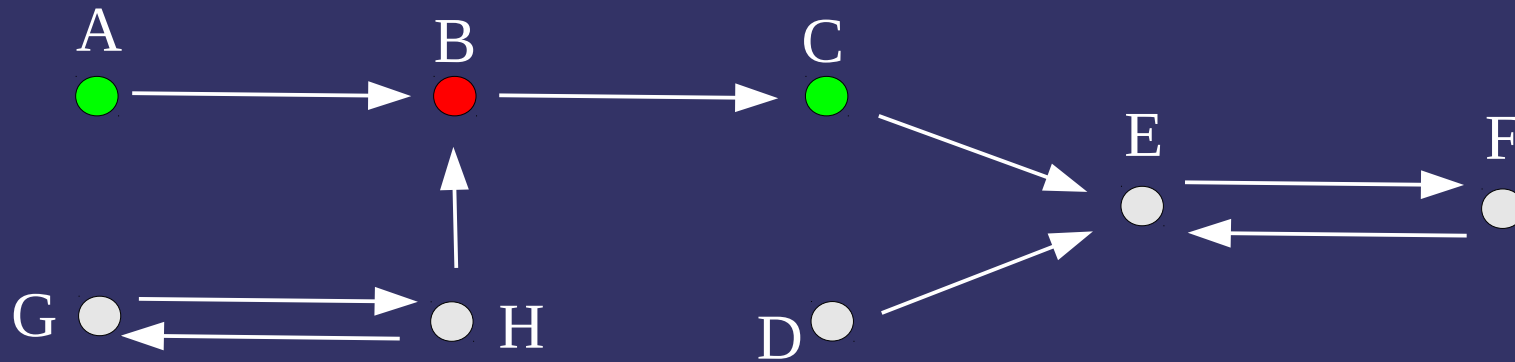
O: CB(B)

P: HTB(A)

O: CONCEDE(A)

O: RETRACT(B)

Example



P: HTB(C)

O: CB(B)

P: HTB(A)

O: CONCEDE(A)

O: RETRACT(B)

O: CONCEDE(C)

***A Discussion Game
for Grounded Semantics (2/3)***

A Discussion Game for Grounded Semantics (2/3)

- HTB(A) This is either the first move, or
- preceding move was CB(B) and A attacks B
 - no CONCEDE or RETRACT move is applicable

A Discussion Game for Grounded Semantics (2/3)

HTB(A) This is either the first move, or

- preceding move was CB(B) and A attacks B
- no CONCEDE or RETRACT move is applicable

CB(B)

- B attacks the last HTB(A) statement that is not yet CONCEDEd
- preceding move was not a CB statement
- B has not yet been RETRACTed
- no CONCEDE or RETRACT move is applicable

A Discussion Game for Grounded Semantics (2/3)

HTB(A) This is either the first move, or

- preceding move was CB(B) and A attacks B
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CB(B)

- B attacks the last HTB(A) statement that is not yet CONCEDEd
- preceding move was not a CB statement
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CONCEDE(A)

- there has been a HTB(A) statement in the past...
- ...of which every attacker has been RETRACTed
- and CONCEDE(A) hasn't yet been moved

A Discussion Game for Grounded Semantics (2/3)

HTB(A) This is either the first move, or

- preceding move was CB(B) and A attacks B
- no CONCEDE or RETRACT move is applicable

CB(B)

- B attacks the last HTB(A) statement that is not yet CONCEDEd
- preceding move was not a CB statement
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CONCEDE(A)

- there has been a HTB(A) statement in the past...
- ...of which every attacker has been RETRACTed
- and CONCEDE(A) hasn't yet been moved

RETRACT(B)

- there has been a CB(B) statement in the past...
- ...of which an attacker has been CONCEDEd
- and RETRACT(B) hasn't yet been moved

A Discussion Game for Grounded Semantics (2/3)

HTB(A) This is either the first move, or

- preceding move was CB(B) and A attacks B
- no CONCEDE or RETRACT move is applicable

CB(B)

- B attacks the last HTB(A) statement that is not yet CONCEDEd
- preceding move was not a CB statement
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CONCEDE(A)

- there has been a HTB(A) statement in the past...
- ...of which every attacker has been RETRACTed
- and CONCEDE(A) hasn't yet been moved

RETRACT(B)

- there has been a CB(B) statement in the past...
- ...of which an attacker has been CONCEDEd
- and RETRACT(B) hasn't yet been moved

additional
condition
for all moves
no HTB-CB
repeats have
occurred

Example



Example



P: HTB(D)

Example



P: HTB(D)

O: CB(C)

Example



P: HTB(D)

O: CB(C)

P: HTB(B)

Example



P: HTB(D)

O: CB(C)

P: HTB(B)

O: CB(A)

Example



P: HTB(D)

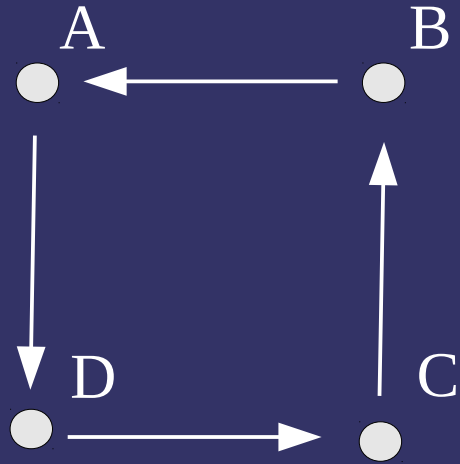
O: CB(C)

P: HTB(B)

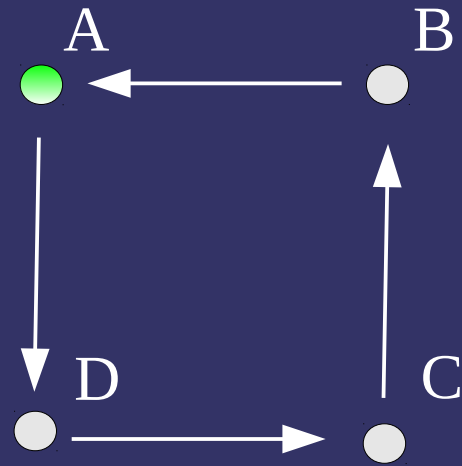
O: CB(A)

*Proponent cannot move anymore, so discussion is terminated.
Main claim not CONCEDEd, so proponent loses.*

Example

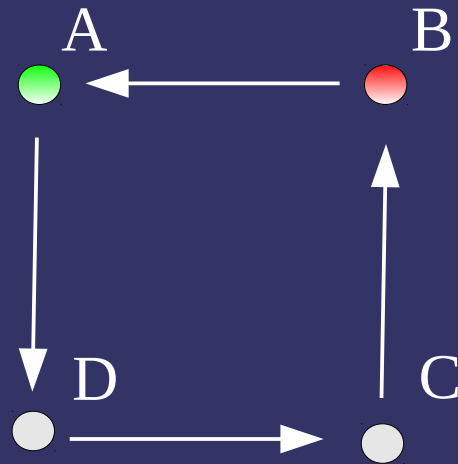


Example



P: HTB(A)

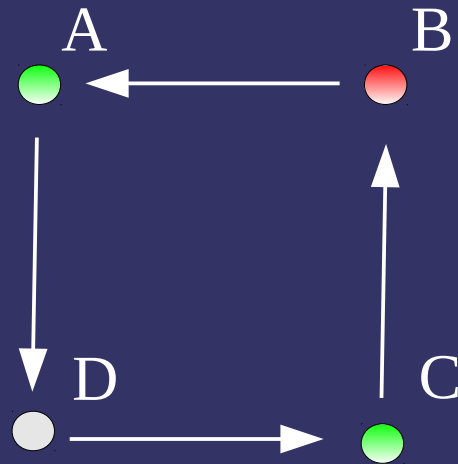
Example



P: HTB(A)

O: CB(B)

Example

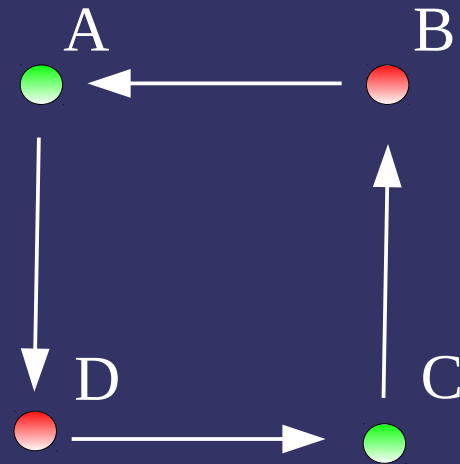


P: HTB(A)

O: CB(B)

P: HTB(C)

Example



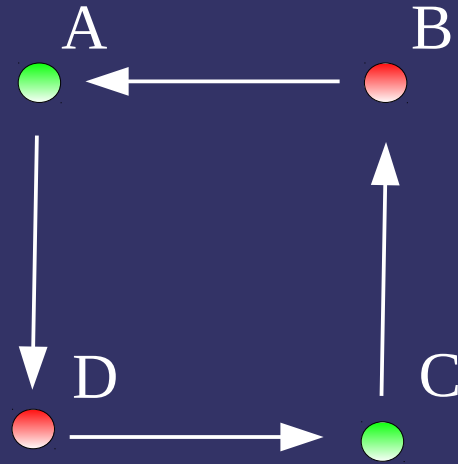
P: HTB(A)

O: CB(B)

P: HTB(C)

O: CB(D)

Example



P: HTB(A)

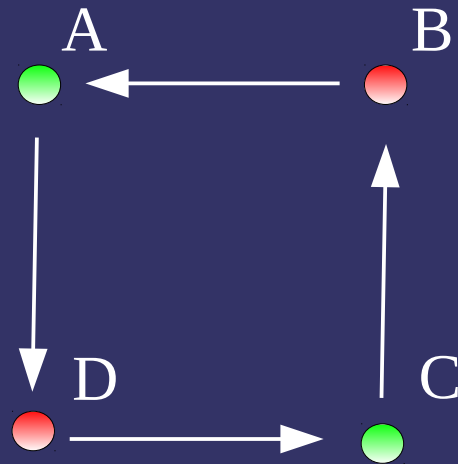
O: CB(B)

P: HTB(C)

O: CB(D)

P: HTB(A)

Example



P: HTB(A)

O: CB(B)

P: HTB(C)

O: CB(D)

P: HTB(A)

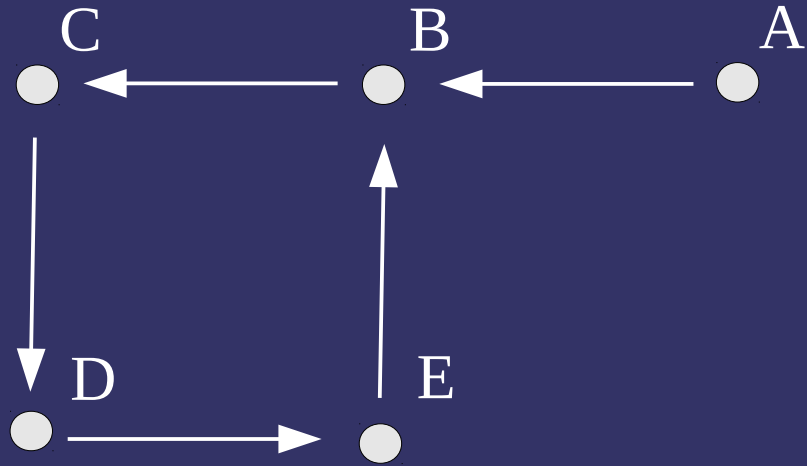
Now we have a HTB(A)-HTB(A) repeat, so all following moves are blocked: discussion terminated.

Main claim not CONCEDEd, so proponent loses

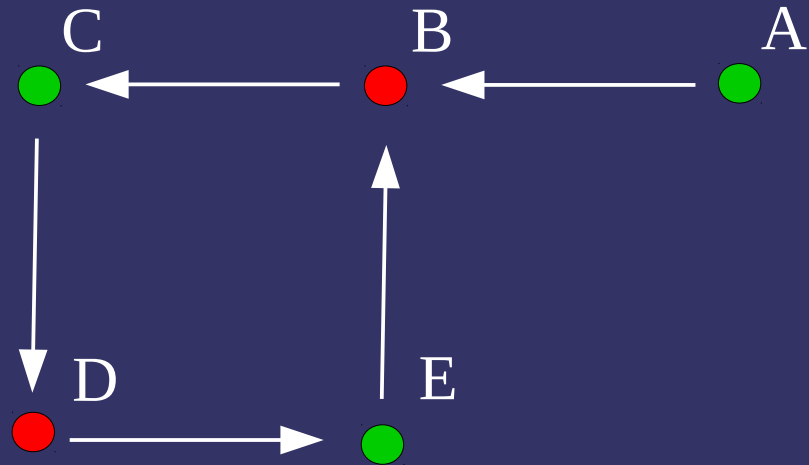
A Discussion Game for Grounded Semantics (3/3)

- A discussion is *terminated* iff no next move is possible
- A terminated discussion (starting with HTB(A)) is won by the proponent iff the opponent has moved CONCEDE(A)
- soundness: if a discussion is won by the proponent, then the main argument is **in** in the grounded labelling
- completeness: if an argument is **in** in the grounded labelling, then the proponent has a winning strategy for it

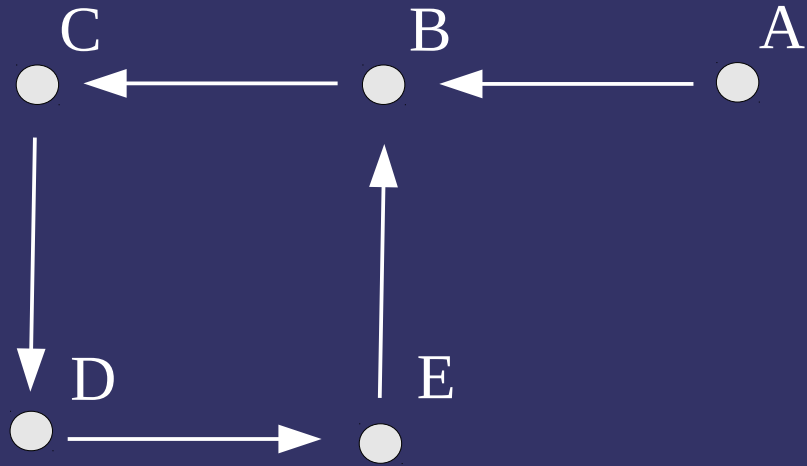
Example



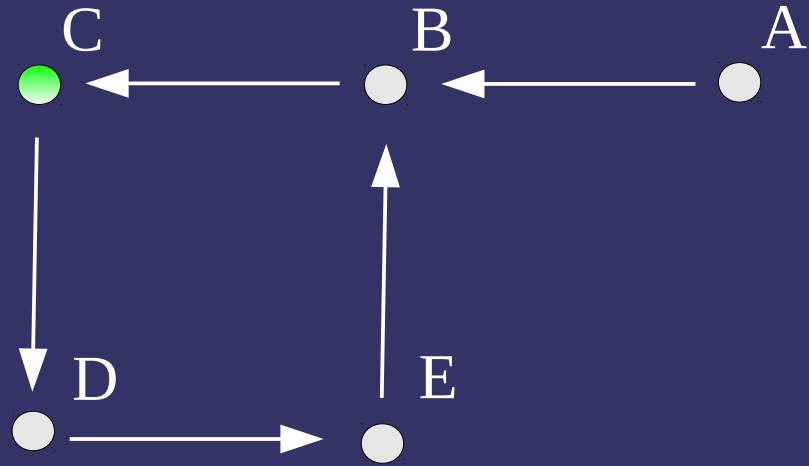
Example



Example

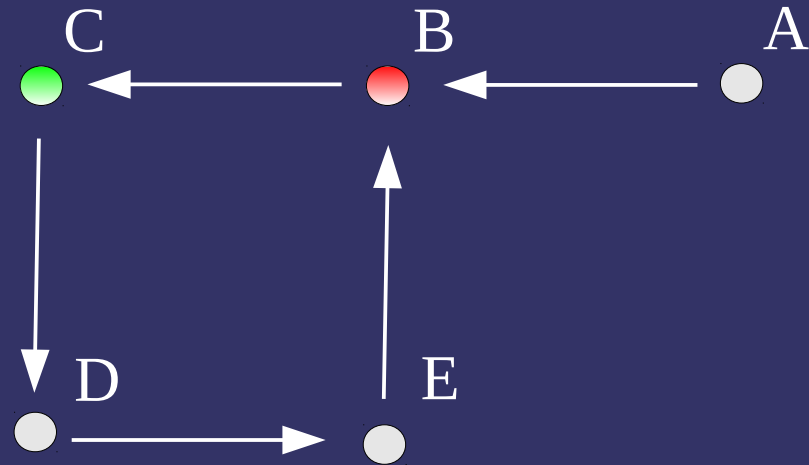


Example



P: HTB(C)

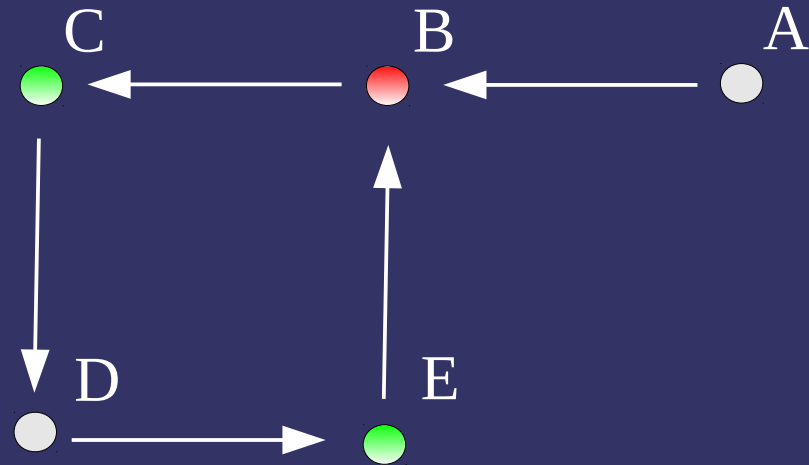
Example



P: HTB(C)

O: CB(B)

Example

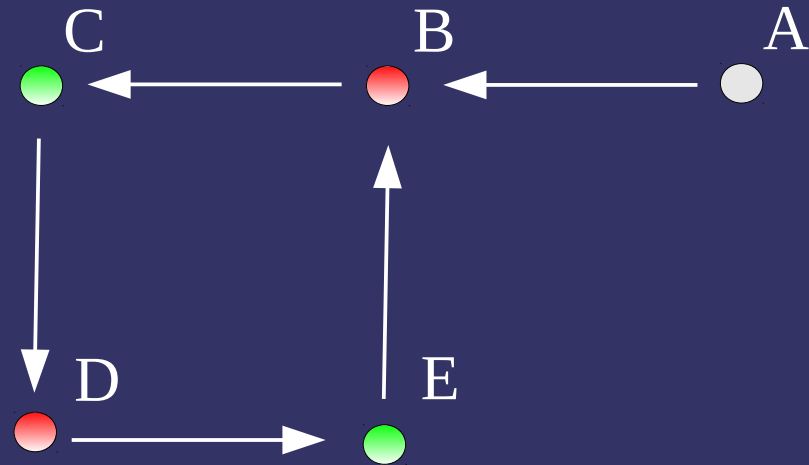


P: HTB(C)

O: CB(B)

P: HTB(E)

Example



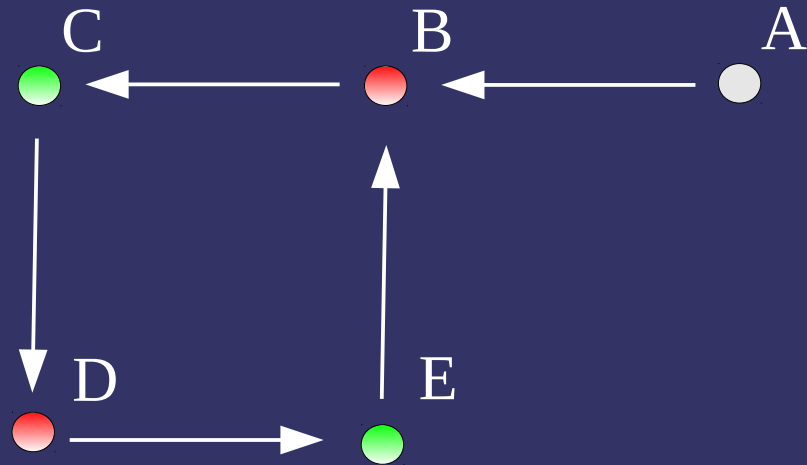
P: HTB(C)

O: CB(B)

P: HTB(E)

O: CB(D)

Example



P: HTB(C)

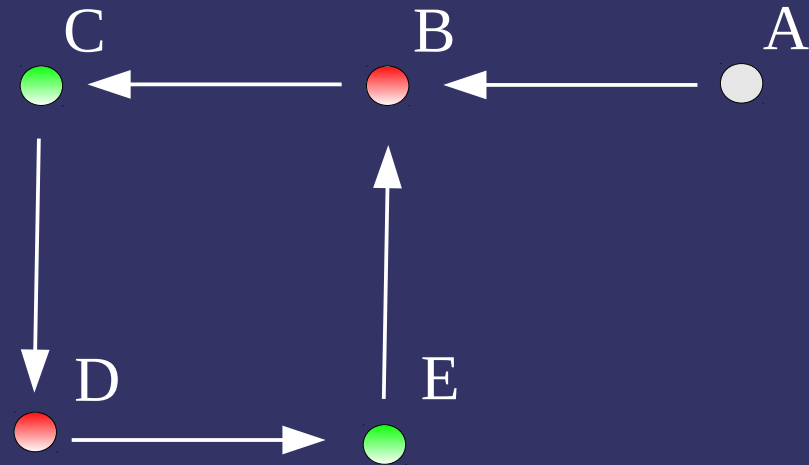
O: CB(B)

P: HTB(E)

O: CB(D)

P: HTB(C)

Example



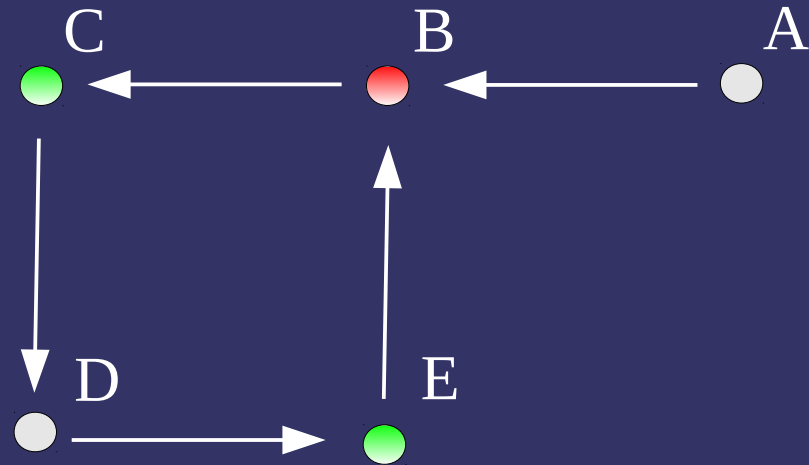
P: HTB(C)

O: CB(B)

P: HTB(E)

O: CB(D)

Example

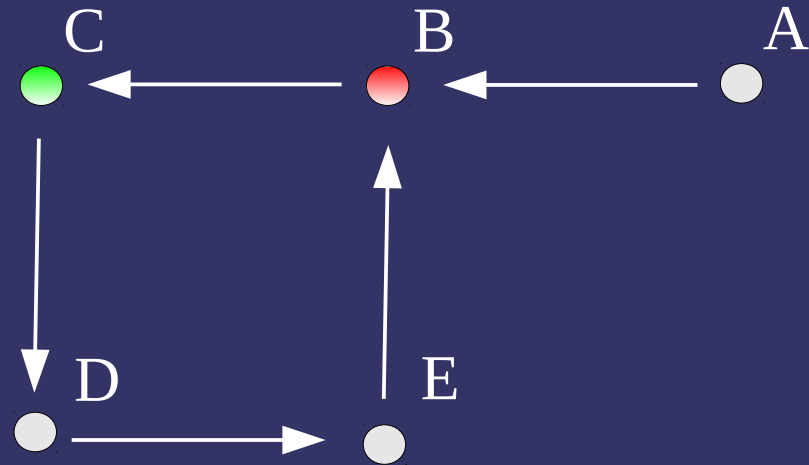


P: HTB(C)

O: CB(B)

P: HTB(E)

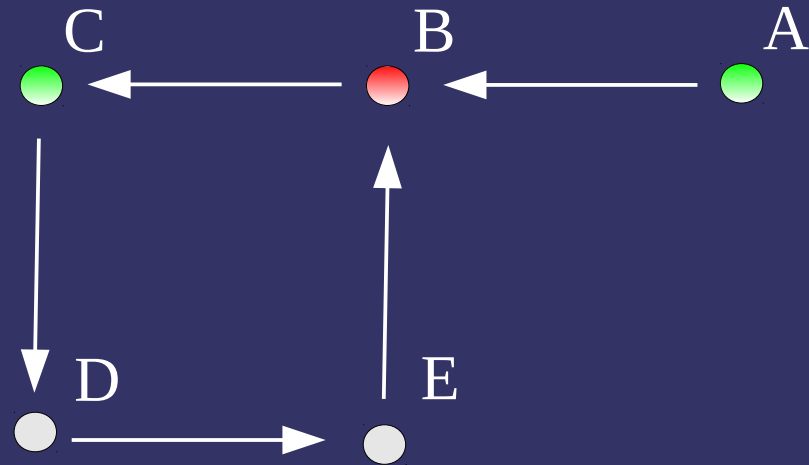
Example



P: HTB(C)

O: CB(B)

Example

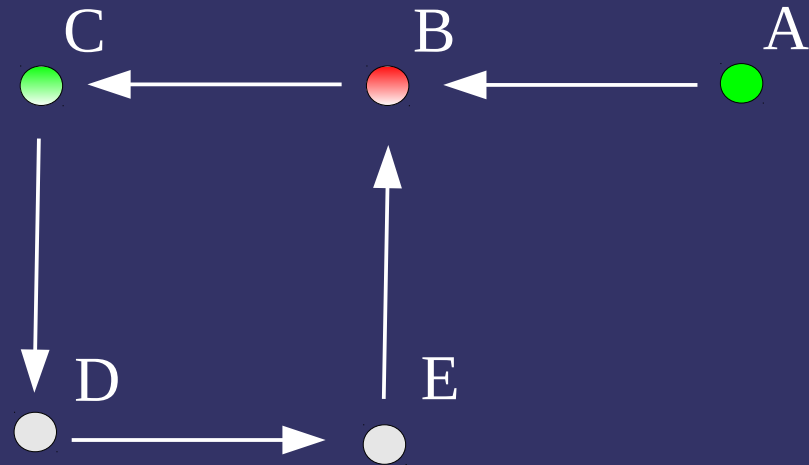


P: HTB(C)

O: CB(B)

P: HTB(A)

Example



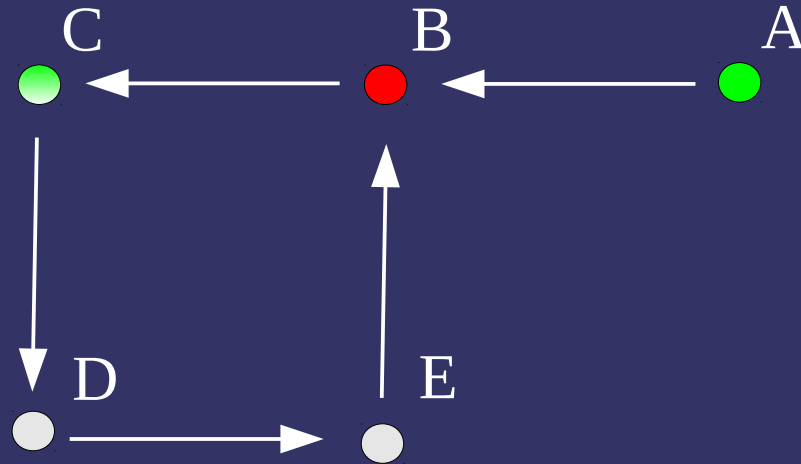
P: HTB(C)

O: CB(B)

P: HTB(A)

O: CONCEDE(A)

Example



P: HTB(C)

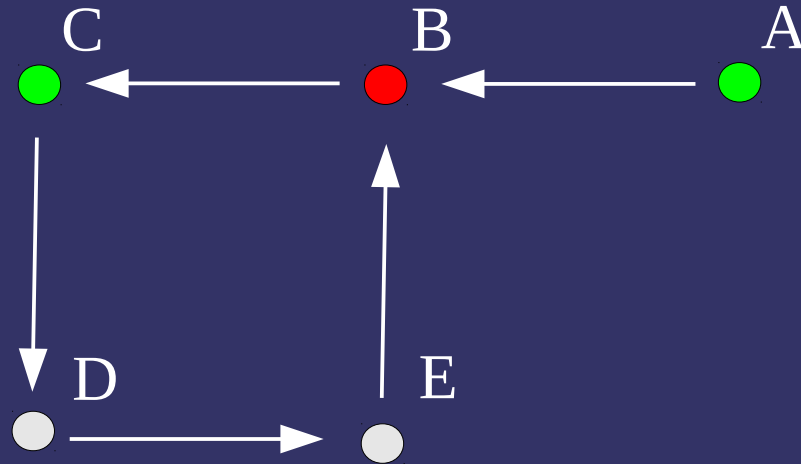
O: CB(B)

P: HTB(A)

O: CONCEDE(A)

O: RETRACT(B)

Example



P: HTB(C)

O: CB(B)

P: HTB(A)

O: CONCEDE(A)

O: RETRACT(B)

O: CONCEDE(C)

Example [Prakken]

Example [Prakken]

Paul: My car is very safe, because it has an airbag.

Olga: I do not think having an airbag makes your car safe, because airbags are unreliable: the newspapers had several reports on cases where airbags did not work.

Paul: A recent scientific study shows that airbags are in fact 99% reliable, and scientific studies are more important than newspaper reports.

Olga: OK, I admit that airbags are reliable. However, your car is not very safe, since its maximum speed is much too high.

Example [Prakken]

P: My car is very safe, because it has an airbag.

O: I do not think having an airbag makes your car safe, because airbags are unreliable: the newspapers had several reports on cases where airbags did not work.

P: A recent scientific study shows that airbags are in fact 99% reliable, and scientific studies are more important than newspaper reports.

O: OK, I admit that airbags are reliable. However, your car is not very safe, since its maximum speed is much too high.

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: I do not think having an airbag makes your car safe, because airbags are unreliable: the newspapers had several reports on cases where airbags did not work.

P: A recent scientific study shows that airbags are in fact 99% reliable, and scientific studies are more important than newspaper reports.

O: OK, I admit that airbags are reliable. However, your car is not very safe, since its maximum speed is much too high.

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: CB(npr $\Rightarrow \neg$ airbagrel $\Rightarrow \neg$ [airbag \Rightarrow safe])

P: A recent scientific study shows that airbags are in fact 99% reliable, and scientific studies are more important than newspaper reports.

O: OK, I admit that airbags are reliable.
However, your car is not very safe,
since its maximum speed is much too high.

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: CB(npr $\Rightarrow \neg$ airbagrel $\Rightarrow \neg$ [airbag \Rightarrow safe])

P: HTB(study \Rightarrow airbagrel)

O: OK, I admit that airbags are reliable.
However, your car is not very safe,
since its maximum speed is much too high.

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: CB(npr $\Rightarrow \neg$ airbagrel $\Rightarrow \neg$ [airbag \Rightarrow safe])

P: HTB(study \Rightarrow airbagrel)

O: CONCEDE(study \Rightarrow airbagrel)

However, your car is not very safe,
since its maximum speed is much too high.

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: CB(npr \Rightarrow \neg airbagrel \Rightarrow \neg [airbag \Rightarrow safe])

P: HTB(study \Rightarrow airbagrel)

O: CONCEDE(study \Rightarrow airbagrel)

RETRACT(npr \Rightarrow \neg airbagrel \Rightarrow \neg [airbag \Rightarrow safe])

Example [Prakken]

P: HTB(airbag \Rightarrow safe)

O: CB(npr $\Rightarrow \neg$ airbagrel $\Rightarrow \neg$ [airbag \Rightarrow safe])

P: HTB(study \Rightarrow airbagrel)

O: CONCEDE(study \Rightarrow airbagrel)

RETRACT(npr $\Rightarrow \neg$ airbagrel $\Rightarrow \neg$ [airbag \Rightarrow safe])

CB(highspeed $\Rightarrow \neg$ safe)

Next Topic

The Preferred Discussion Game

Socratic Discussion

Answer me this. As soon as one man loves another, which of the two becomes the friend? the lover of the loved, or the loved of the lover? Or does it make no difference?

None in the world, that I can see

How? Are both friends, if only one loves?

I think so

Indeed! is it not possible for one who loves, not to be loved in return (...) ?

It is.

Nay, is it not possible for him even to be hated? (...) Don't you believe this to be true?

Quite true.

Well, in such a case as this, the one loves, the other is loved.

Just so.

Which of the two, then, is the friend of the other? The lover of the loved, whether or not he be loved in return, and even if he be hated, or the loved of the lover? or is neither the friend of the other, unless both love each other?

The latter certainly seems to be the case, Socrates.

If so, I continued, we think differently now from what we did before. (...)

Yes, I'm afraid we have contradicted ourselves.

Traditional Dialogue vs. Socratic Dialogue

P: claim tr

"I think that there will be a tax relief."

O: why tr

"Why do you think so?"

P: because pmp \Rightarrow tr

"Because of the fact that the politicians made a promise."

O: concede tr

"OK, you are right."

Traditional Dialogue vs. Socratic Dialogue

P: claim tr

"I think that tr ."

O: but-then $tr \Rightarrow bd$

"Then you implicitly also hold that bd ."

P: concede bd

"Yes I do."

O: but-then $bd \Rightarrow feu$

"Then you implicitly also hold that feu ."

P: concede feu

"Yes I do."

O: but-then $feu \Rightarrow \neg tr$

"Then you implicitly also hold that $\neg tr$."

P: concede $\neg tr$

"Oops, you're right; I caught myself in..."

“because” versus “but-then”



reasoning goes backward

reasoning goes forward

proponent constructs path

opponent constructs path

originates from *true*

leads to *false*

both parties
become committed

only proponent
becomes committed

Preferred Semantics as Socratic Discussion

Preferred Semantics as Socratic Discussion

definition

admissible labelling:

if argument is **in** then all its attackers are **out**

if argument is **out** then it has an attacker that is **in**

Preferred Semantics as Socratic Discussion

definition

admissible labelling:

if argument is **in** then all its attackers are **out**

if argument is **out** then it has an attacker that is **in**

proposition

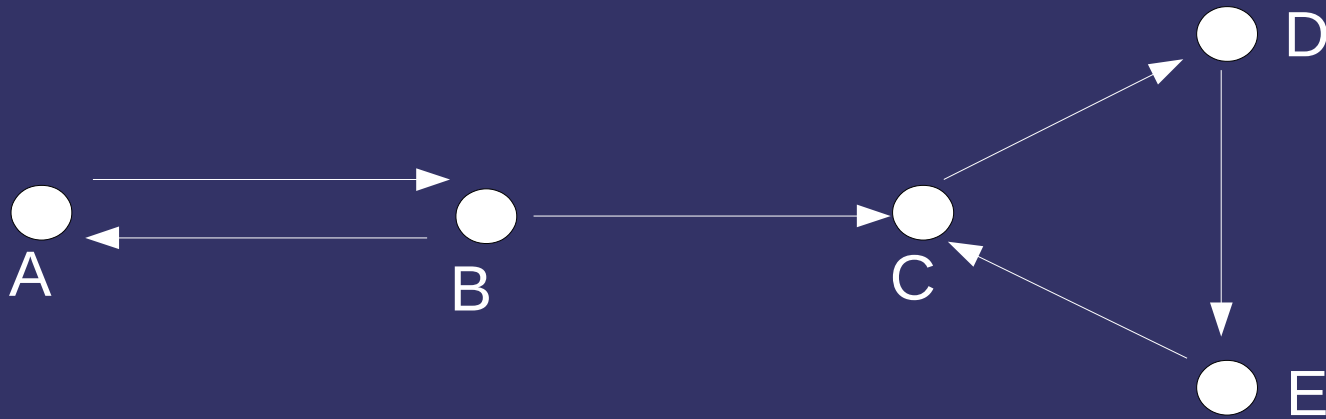
An argument is in a preferred extension

iff it is in a complete extension

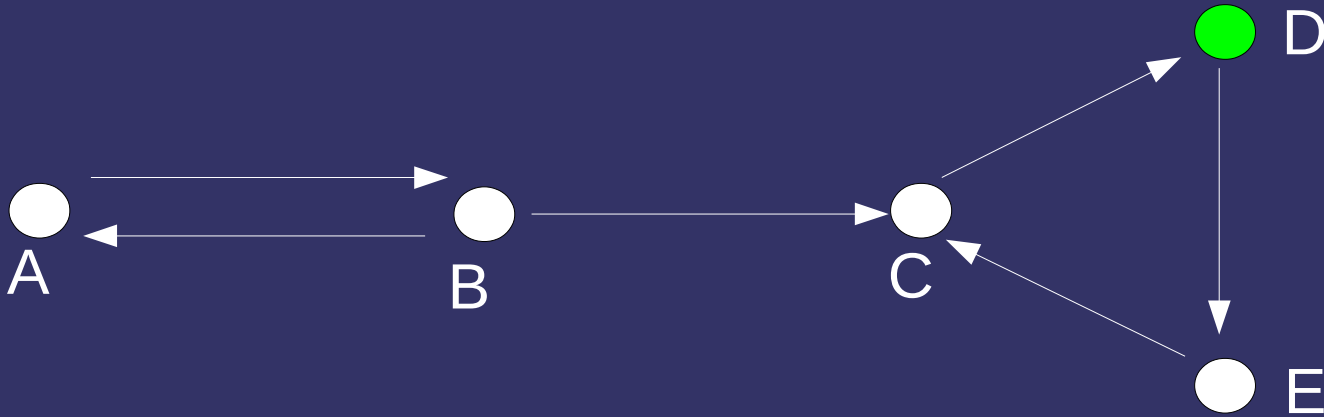
iff it is in an admissible set

iff it is labelled **in** by an admissible labelling

Preferred Semantics as Socratic Discussion

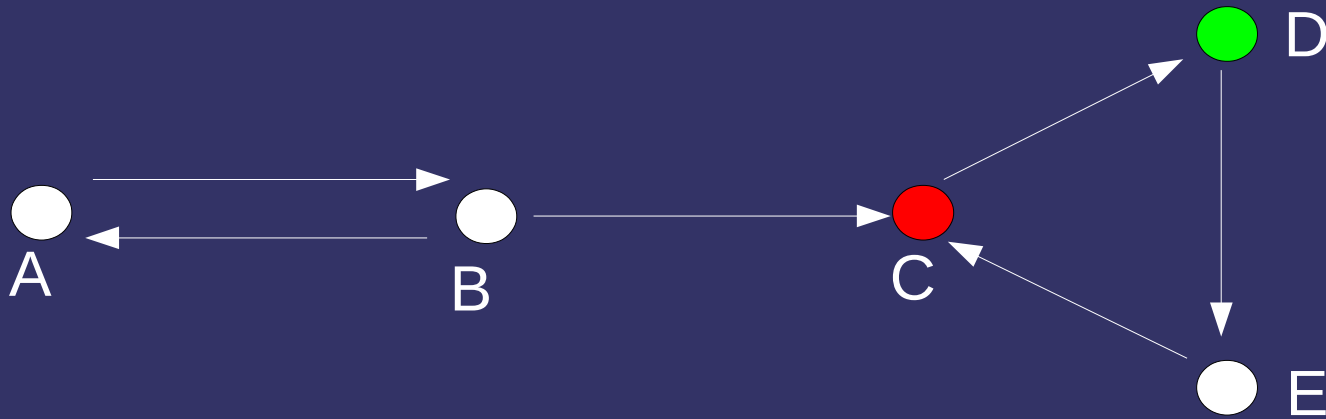


Preferred Semantics as Socratic Discussion



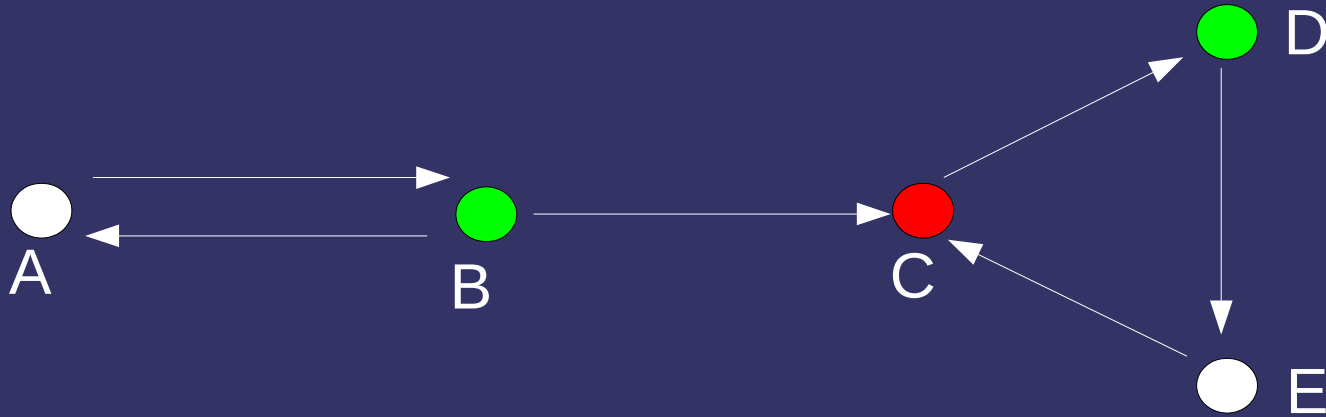
M: $in(D)$ “I have an admissible labelling in which D is labelled in .”

Preferred Semantics as Socratic Discussion



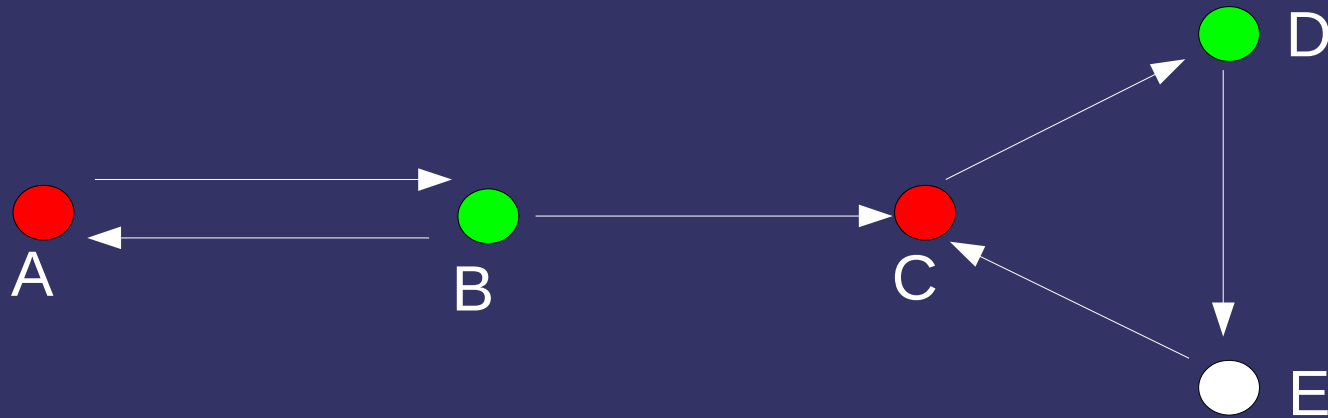
M: **in**(D) “I have an admissible labelling in which D is labelled **in**.”
S: **out**(C) “But then in your labelling it must also be the case that D’s attacker C is labelled **out**. Based on which grounds?”

Preferred Semantics as Socratic Discussion



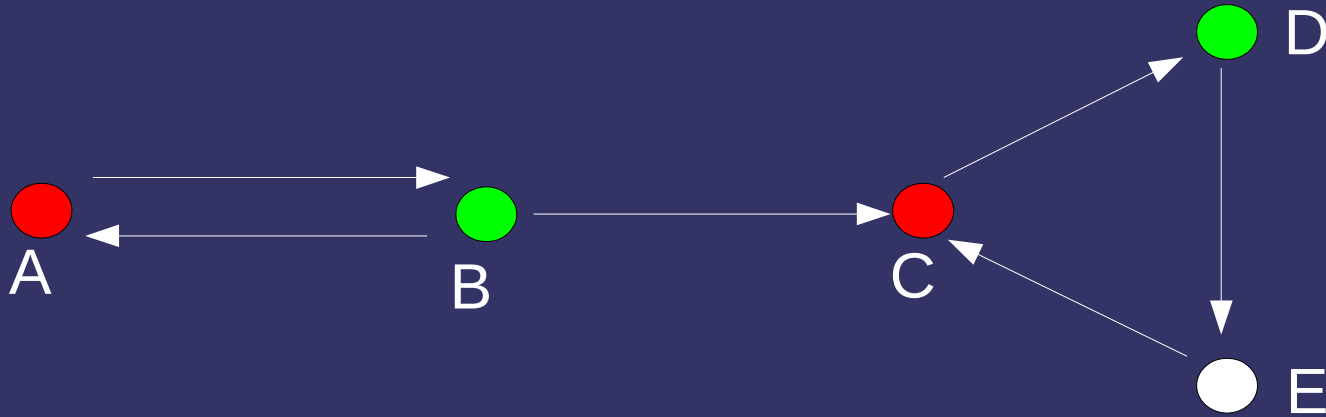
- M: **in**(D) “I have an admissible labelling in which D is labelled **in**.”
- S: **out**(C) “But then in your labelling it must also be the case that D’s attacker C is labelled **out**. Based on which grounds?”
- M: **in**(B) “C is labelled **out** because B is labelled **in**.”

Preferred Semantics as Socratic Discussion



- M: **in**(D) “I have an admissible labelling in which D is labelled **in**.”
- S: **out**(C) “But then in your labelling it must also be the case that D’s attacker C is labelled **out**. Based on which grounds?”
- M: **in**(B) “C is labelled **out** because B is labelled **in**.”
- S: **out**(A) “But then in your labelling it must also be the case that B’s attacker A is labelled **out**. Based on which grounds?”

Preferred Semantics as Socratic Discussion



- M: **in**(D) “I have an admissible labelling in which D is labelled **in**.”
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(1) Each move of M (except the first) contains an attacker of the directly preceding move of S.

Preferred Semantics as Socratic Discussion

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*(2) Each move of S
contains an attacker of some previous move of M.*

Preferred Semantics as Socratic Discussion

- M: **in**(D) “I have an admissible labelling in which D is labelled **in**.”
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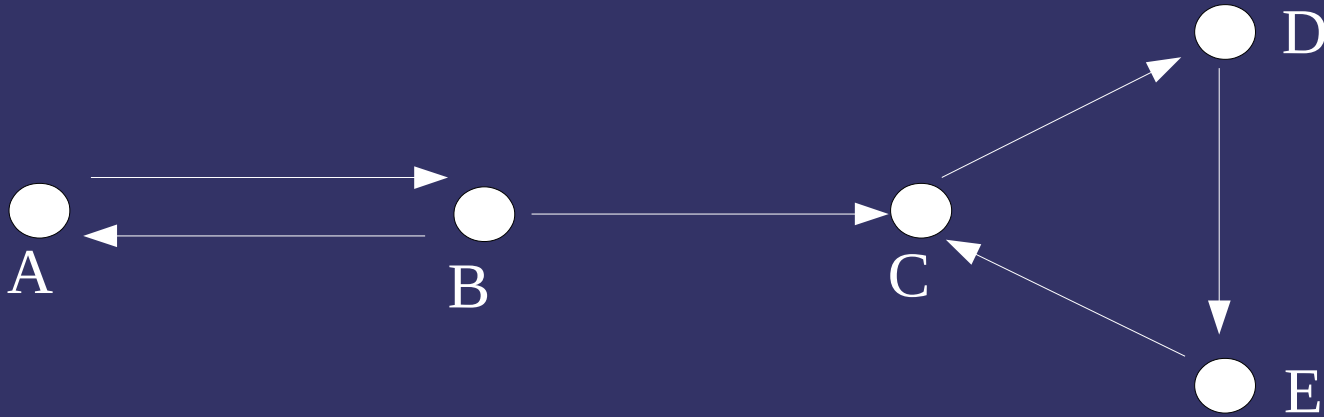
(3) S is not allowed to repeat his moves.

Preferred Semantics as Socratic Discussion

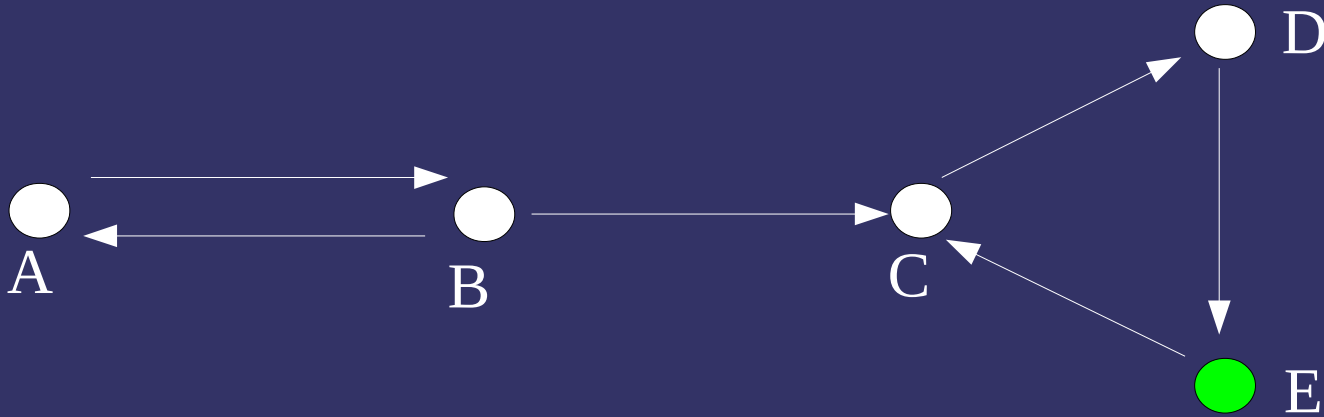
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(4) M is allowed to repeat his moves.

Preferred Semantics as Socratic Discussion

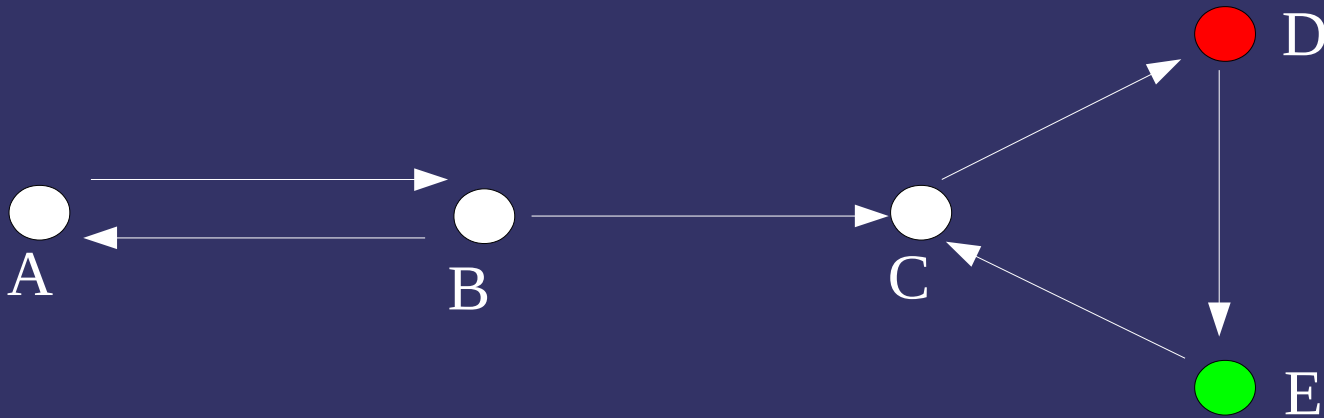


Preferred Semantics as Socratic Discussion



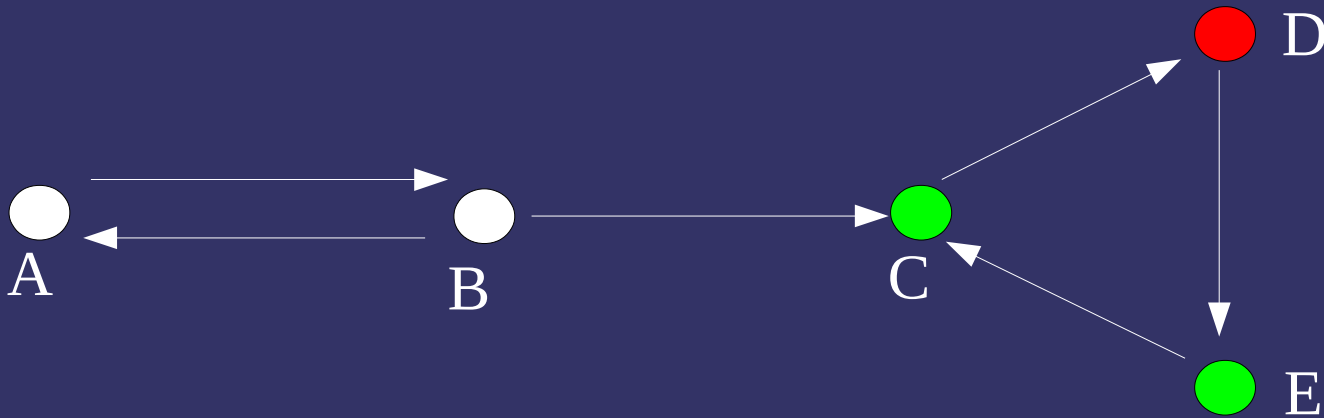
M: $in(E)$ “I have an admissible labelling in which E is labelled in .”

Preferred Semantics as Socratic Discussion



M: **in**(E) “I have an admissible labelling in which E is labelled **in**.”
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Preferred Semantics as Socratic Discussion

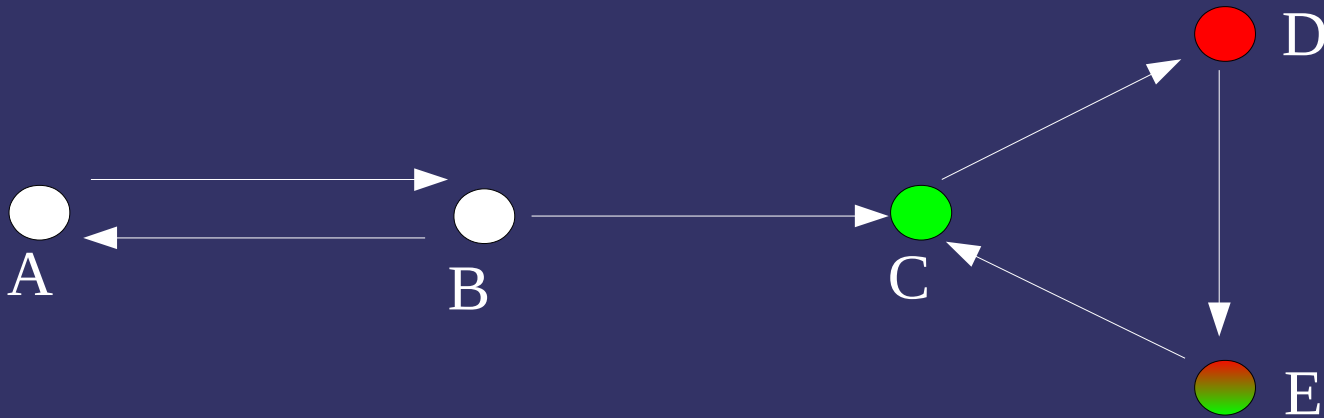


M: **in**(E) “I have an admissible labelling in which E is labelled **in**.”

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M: **in**(C) “D is labelled **out** because C is labelled **in**.”

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(5) If S uses an argument previously used by M, then S wins the discussion.

Preferred Semantics as Socratic Discussion

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(6) If M uses an argument previously used by S, then S wins the discussion.

Preferred Semantics as Socratic Discussion

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(7) If M cannot make a move anymore,
then S wins the discussion.

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(8) If S cannot make a move anymore,
then M wins the discussion.

Preferred Semantics as Socratic Discussion

THEOREM

Argument A is labelled **in** by at least one admissible labelling
iff M can win the Socratic discussion game (for A).

Preferred Semantics as Socratic Discussion

THEOREM

Argument A is in at least one preferred extension
iff M can win the Socratic discussion game (for A).

Complete Semantics as Socratic Discussion

THEOREM

Argument A is in at least one complete extension
iff M can win the Socratic discussion game (for A).

Skeptical Complete vs Credulous Complete

- Skeptical Complete (= grounded)
The argument is accepted in every reasonable position (complete labelling)
“Therefore you have to hold that...”
persuasion dialogue
- Credulous Complete (= credulous preferred)
The argument is accepted in at least one reasonable position (complete labelling)
“Therefore I can hold that...”
Socratic dialogue

Why These Results Matter

- classical logic:
- argumentation:

Why These Results Matter

- classical logic: based on notion of truth
(entails what is model-theoretically true)
- argumentation:

Why These Results Matter

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Why These Results Matter

- classical logic: based on notion of truth
(entails what is model-theoretically true)
- argumentation: based on notion of justification
(entails what can be defended in rational discussion)
- discussions can be used by the system to explain
its answer to the user
- different semantics express
different types of rational discussion
- allows (in principle) for dynamic and user-based updating
of the underlying knowledge base

Next Topic

Rationality Postulates

*If we select arguments using only
the structure of the graph,
then how do we know
their conclusions make sense?*

Argumentation for Inference: 3-step process

Argumentation for Inference: 3-step process

knowledge
base

Argumentation for Inference: 3-step process

argumentation
framework

↑ (1) *argument (+attack) construction*

knowledge
base

Argumentation for Inference: 3-step process

labellings
of arguments

↑ *(2) applying argumentation semantics*

argumentation
framework

↑ *(1) argument (+attack) construction*

knowledge
base

Argumentation for Inference: 3-step process

labellings
of conclusions

↑ (3) *determining status of conclusions*

labellings
of arguments

↑ (2) *applying argumentation semantics*

argumentation
framework

↑ (1) *argument (+attack) construction*

knowledge
base

From Arguments to Conclusions

labelling of args → labelling of concls
*for each conclusion, give it the label of
the “best” (highest label) argument that
yields it*

How Things Go Wrong (1/5)

r $r \Rightarrow m$ $m \rightarrow hs$
 p $p \Rightarrow b$ $b \rightarrow \neg hs$

$A1 = (r) \Rightarrow m$

$A2 = (p) \Rightarrow b$

$A3 = A1 \rightarrow hs$

$A4 = A2 \rightarrow \neg hs$

Conclusions m and b are justified under any semantics but what about hs and $\neg hs$?

How Things Go Wrong (2/5)

r $r \Rightarrow m$ $m \supset hs$ (“ \rightarrow ” \equiv “ \vdash ”)
 p $p \Rightarrow b$ $b \supset \neg hs$

A1: $(r) \Rightarrow m$

A2: $(p) \Rightarrow b$

A3: $(A1, m \supset hs) \rightarrow hs$

A4: $(A2, b \supset \neg hs) \rightarrow \neg hs$

A5: $(A3, b \supset \neg hs) \rightarrow \neg b$

A6: $(A4, m \supset hs) \rightarrow \neg m$

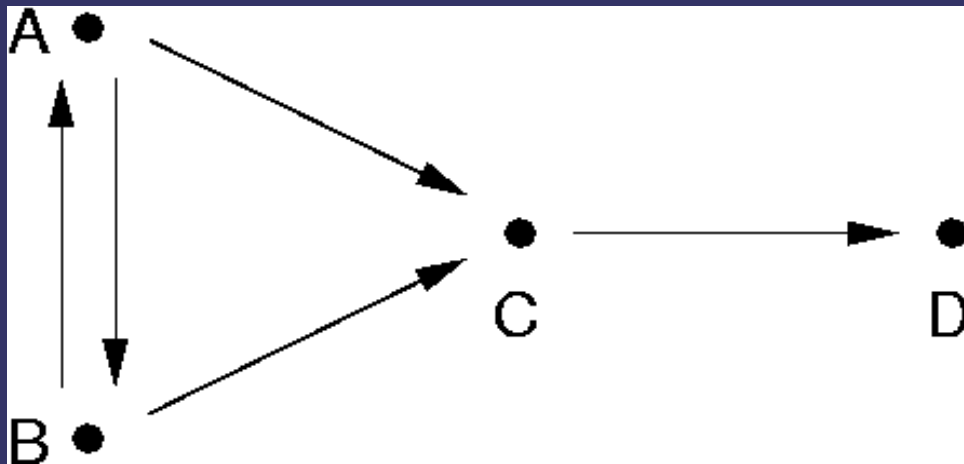
So far,
so good...

How Things Go Wrong (3/5)

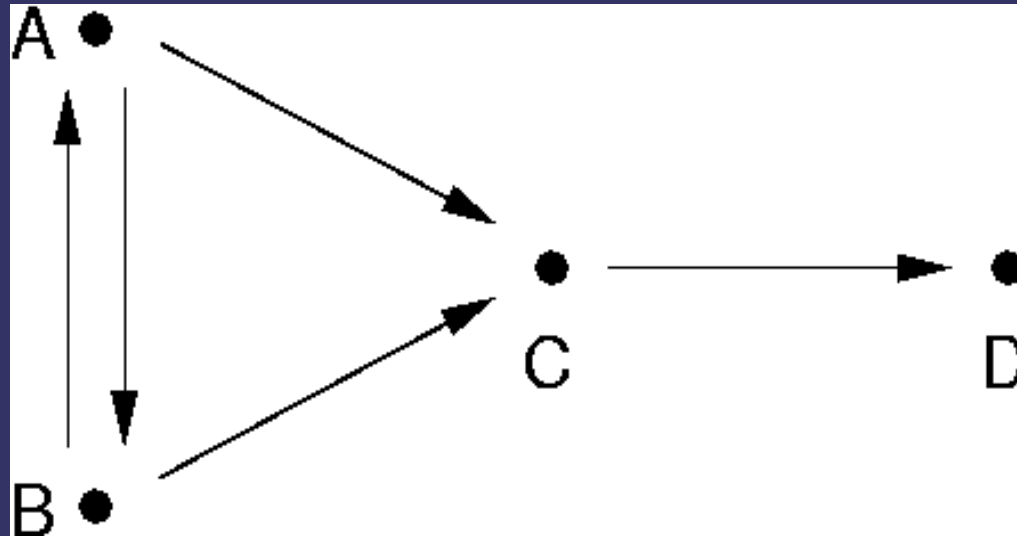
j $j \Rightarrow s$ ($\rightarrow \equiv \vdash$)
 m $m \Rightarrow \neg s$ wf wf $\Rightarrow r$

There now exist the following arguments:

$A = (j) \Rightarrow s$ (unfortunately,
 $B = (m) \Rightarrow \neg s$ there also exists:
 $D = (wf) \Rightarrow r$ $C = A, B \rightarrow \neg r$)



How Things Go Wrong (4/5)



- Grounded semantics: no justified arguments
- Why not use preferred or stable semantics?
- Reiter and Pollock also do this...

How Things Go Wrong (5/5)

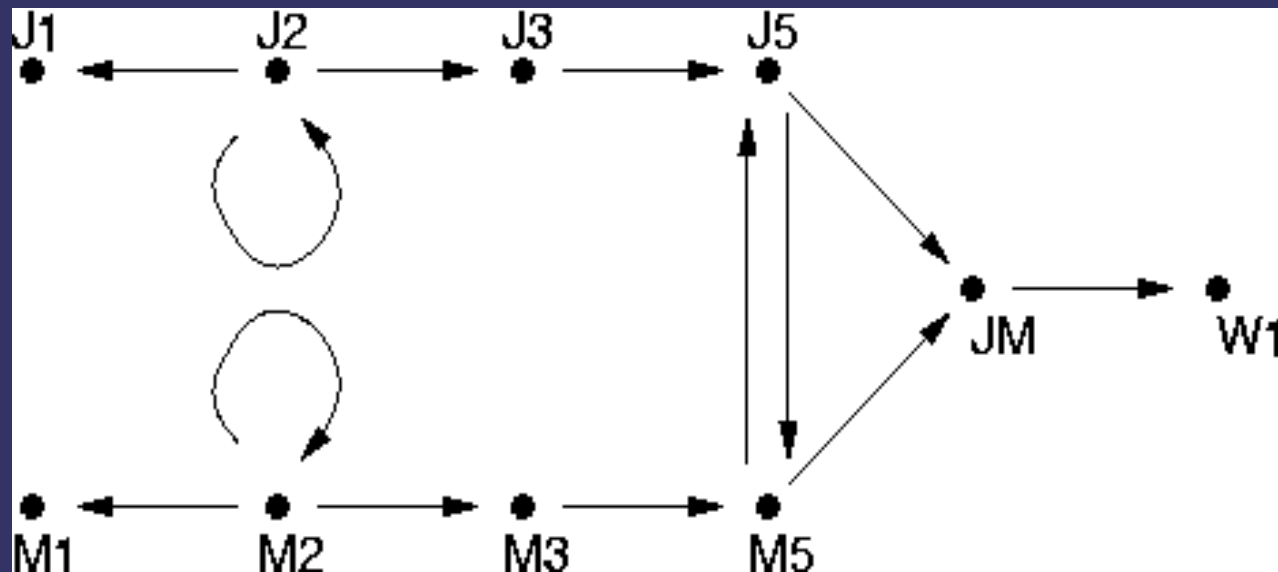
John: "Cup of coffee contains sugar."

Mary: "Cup of coffee doesn't contain sugar."

John: "I'm unreliable."

Mary: "I'm unreliable."

Weather Forecaster: "Tomorrow rain."



Rationality Postulates

Let J be a set of conclusions yielded by an argumentation formalism.

- *direct consistency*

J does not contain contraries (p and $\neg p$)

- *closure*

J is closed under the strict rules

- *indirect consistency*

the closure of J under strict rules is directly consistent

- *crash-resistance*

no set of formulas can make a totally unrelated set of formulas completely irrelevant, when being merged to it

- *non-interference*

no set of formulas can influence the entailment of a totally unrelated set of formulas, when being merged to it

Rationality Postulates

direct consistency
closure
indirect consistency

Caminada & Amgoud
AIJ 2007

crash-resistance
non-interference
backwards compatibility

Caminada, Dunne & Carnielli
JLC 2011

Transposition

Take the following strict rule:

$$a_1, \dots, a_{i-1}, a_i, a_{i+1}, \dots, a_n \rightarrow c$$

A *transposition* of this rule is:

$$a_1, \dots, a_{i-1}, \neg c, a_{i+1}, \dots, a_n \rightarrow \neg a_i$$

(for some $1 \leq i \leq n$)

A set of strict rules S is closed under transposition iff it contains all transpositions of the rules in S .

Restricted versus unrestricted rebut

$((a) \Rightarrow b) \Rightarrow c$

$((d) \Rightarrow e) \Rightarrow \neg c$

Restricted versus unrestricted rebut

$((a) \rightarrow b) \rightarrow c$

$((d) \Rightarrow e) \Rightarrow \neg c$

Restricted versus unrestricted rebut

$((a) \Rightarrow b) \rightarrow c$

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Restricted versus unrestricted rebut

$((a) \Rightarrow b) \rightarrow c$

$((d) \rightarrow e) \Rightarrow \neg c$

unrestricted rebut:

an argument can be rebutted on a conclusion derived by at least one defeasible rule

restricted rebut:

an argument can be rebutted only on the direct consequent of a defeasible rule

Satisfying the rationality postulates (1/2)

Satisfying the rationality postulates (1/2)

When using strict rules as primitives:

Satisfying the rationality postulates (1/3)

When using strict rules as primitives:

- Step 1:
 - close the strict rules under transposition
 - use restricted rebut for defining the attack relation
- Step 2:
 - use a complete-based semantics that yields at least one extension/labelling
- Step 3:
(standard)

Satisfying the rationality postulates (2/3)

When using strict rules as primitives:

- Step 1:
 - close the strict rules under transposition
 - use unrestricted rebut for defining the attack relation
- Step 2:
 - use grounded semantics
- Step 3:
 - (standard)

Satisfying the rationality postulates (2/2)

When using strict rules as classical entailment:

Satisfying the rationality postulates (3/3)

When using strict rules as classical entailment:

- Step 1:
 - use restricted rebut for defining the attack relation
 - remove all inconsistent arguments
- Step 2:
 - use a complete-based semantics that yields at least one extension/labelling
- Step 3:
(standard)

Why Restricted Rebut

$S = \{ w1; w2; w3; \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

Why Restricted Rebut

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

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$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

$A_2: (w2) \Rightarrow b2$

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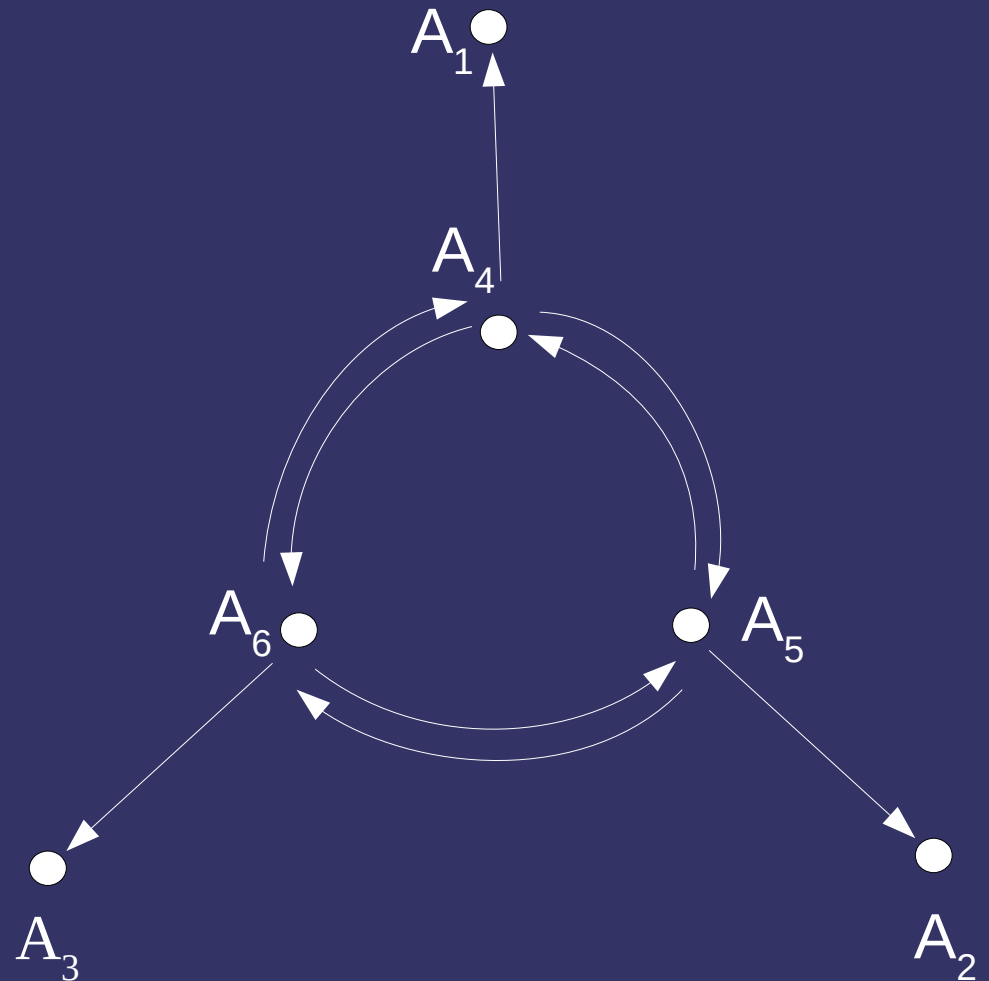
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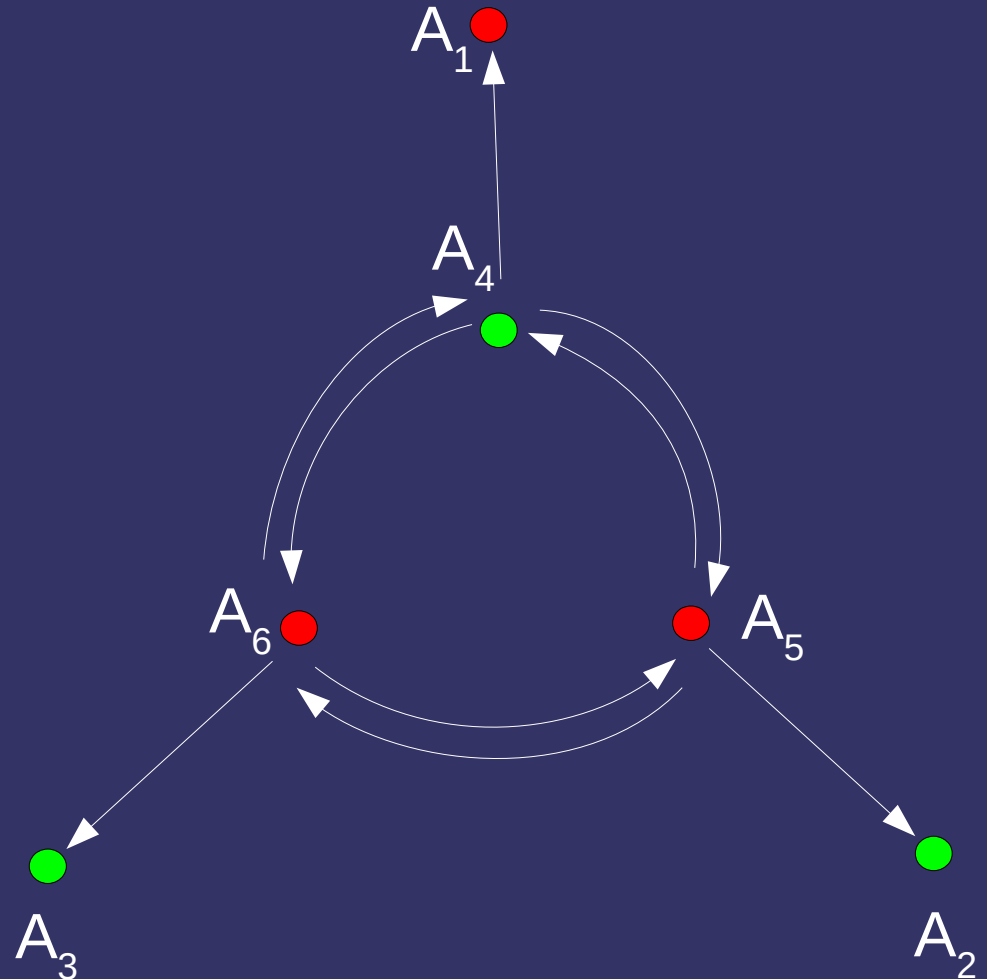
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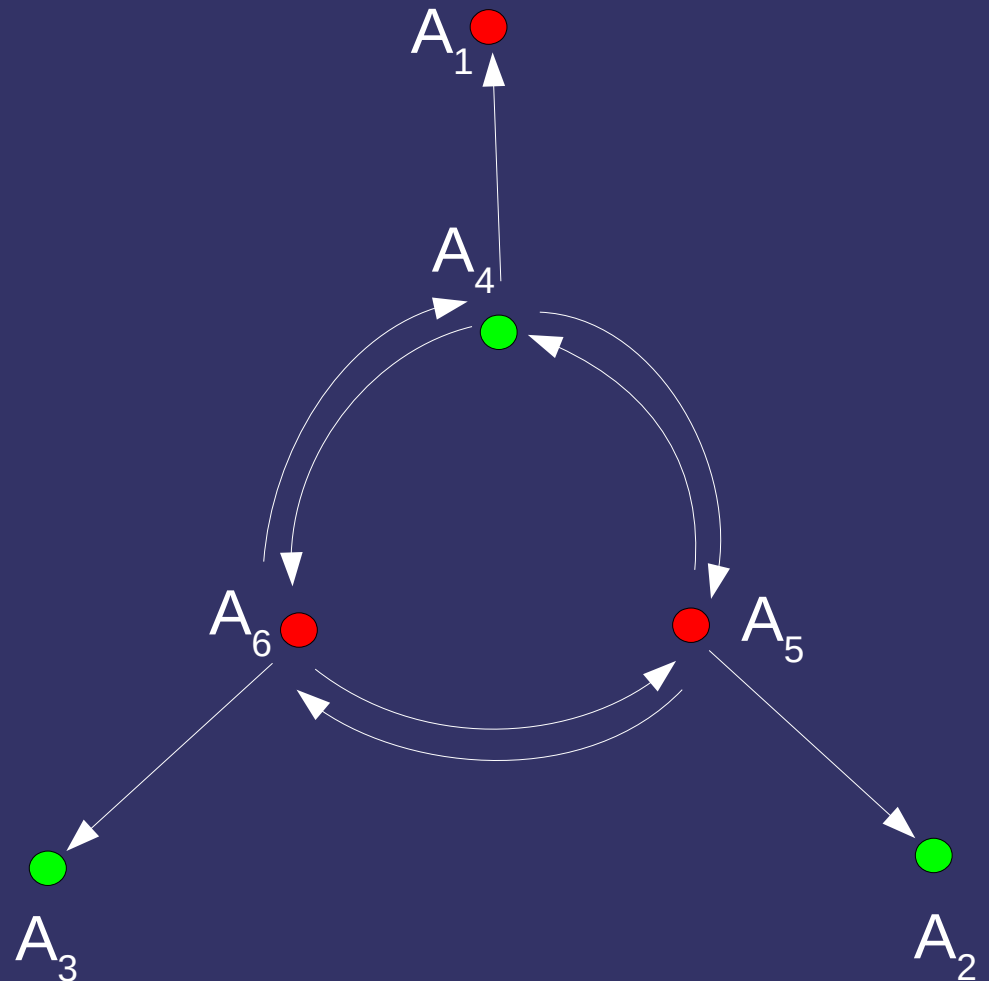
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$b1$ $b2$ $b3$ $\neg b1$ $\neg b2$ $\neg b3$



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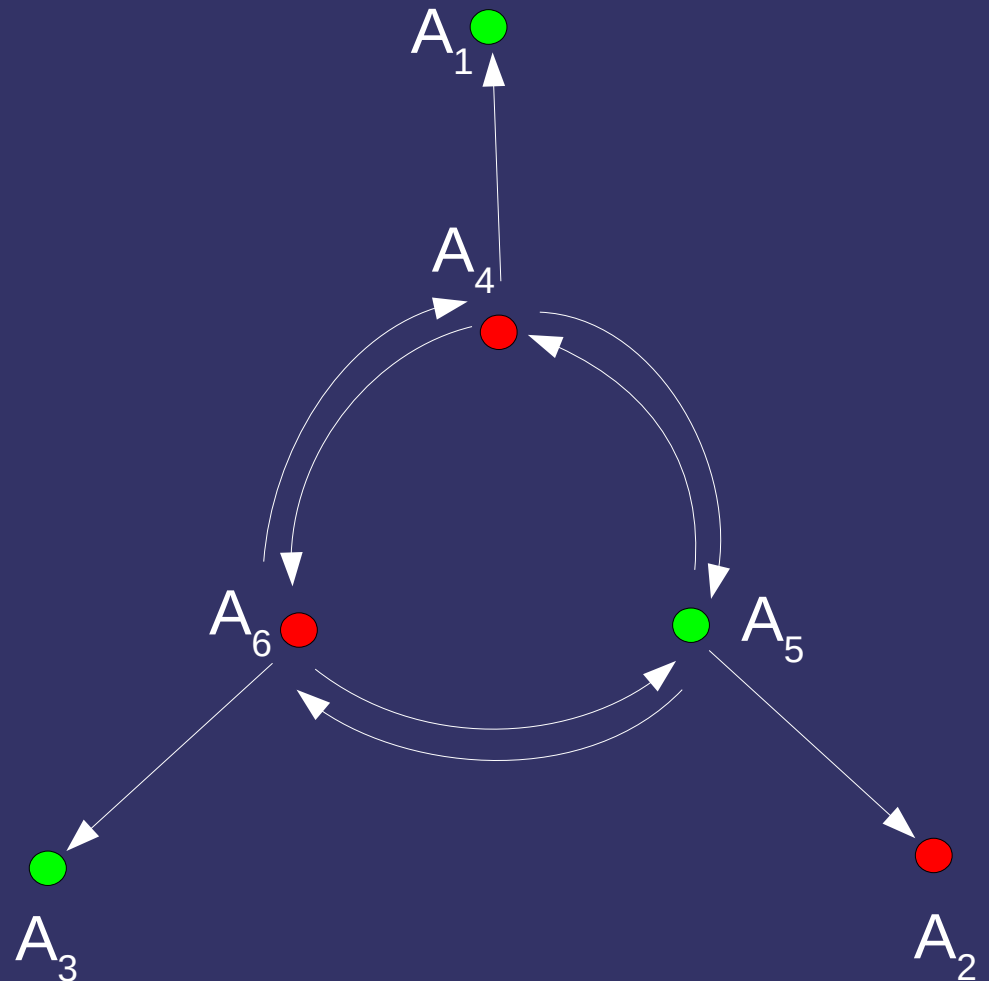
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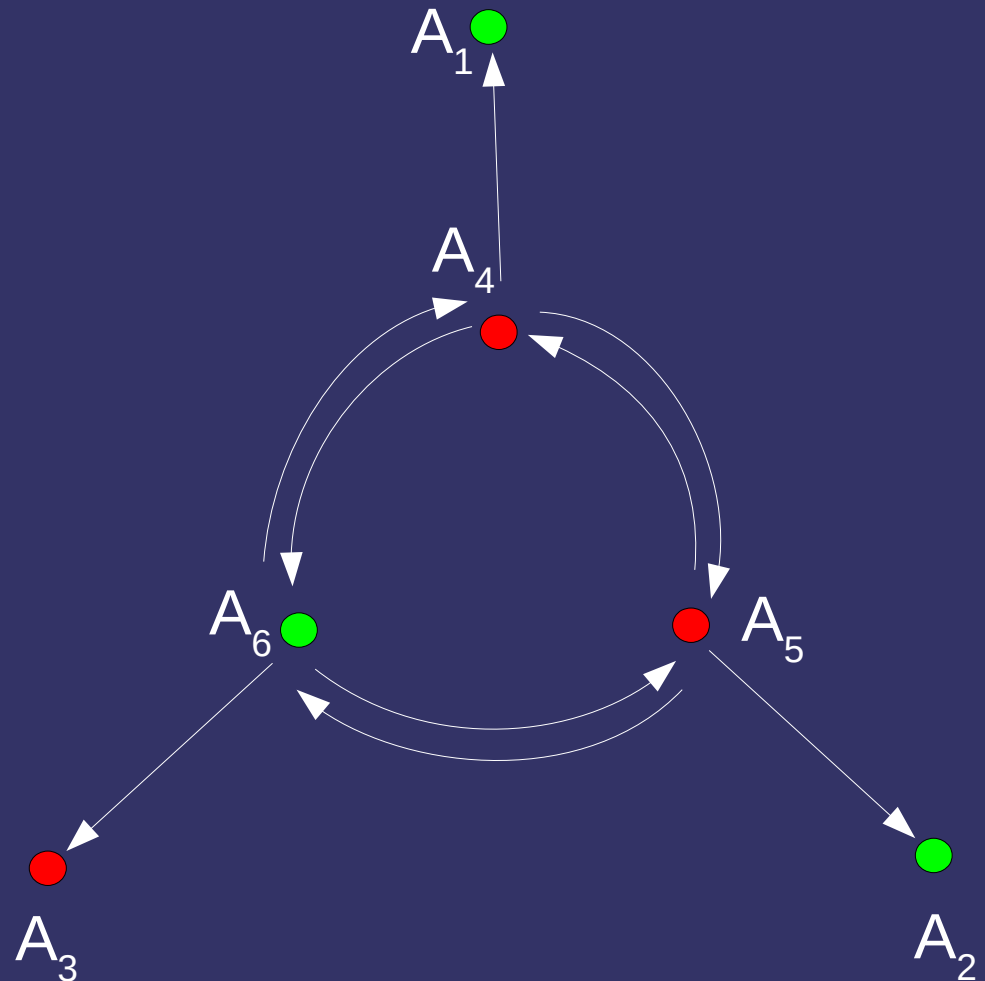
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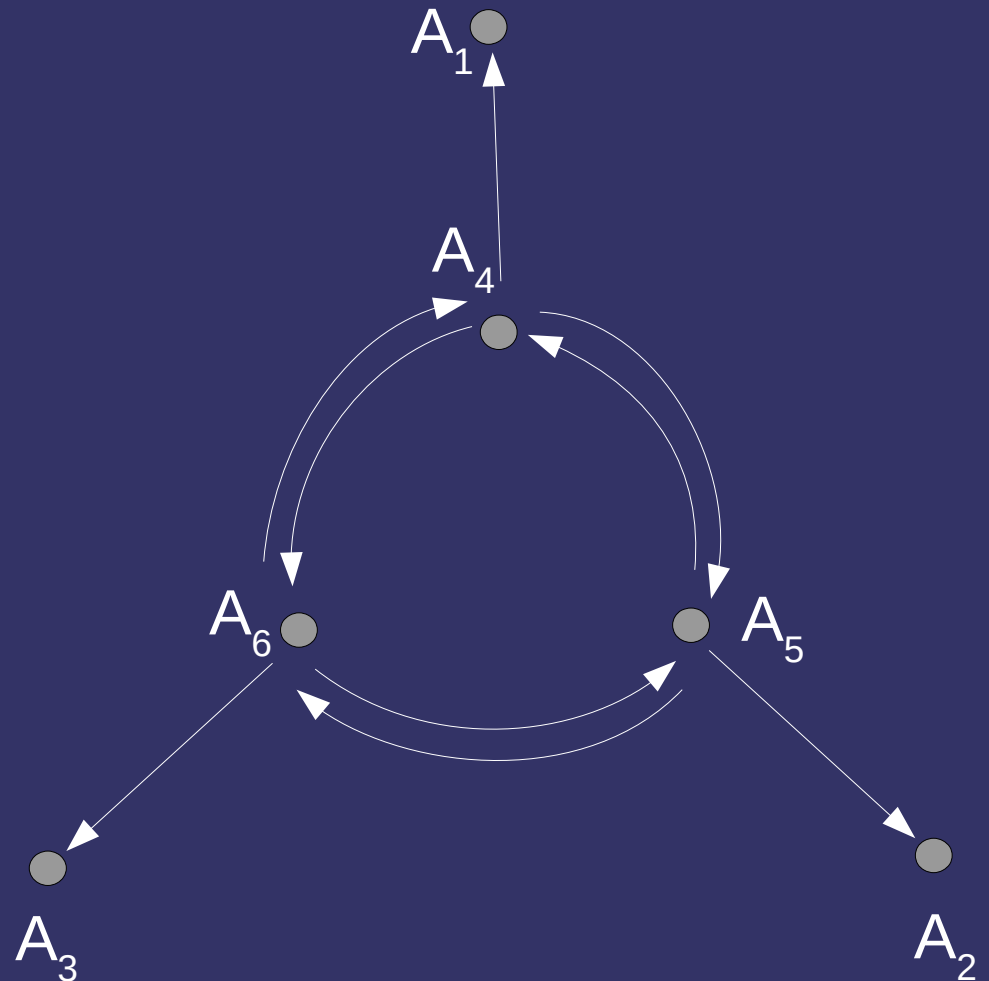
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b1 b2 b3 $\neg b1$ $\neg b2$ $\neg b3$



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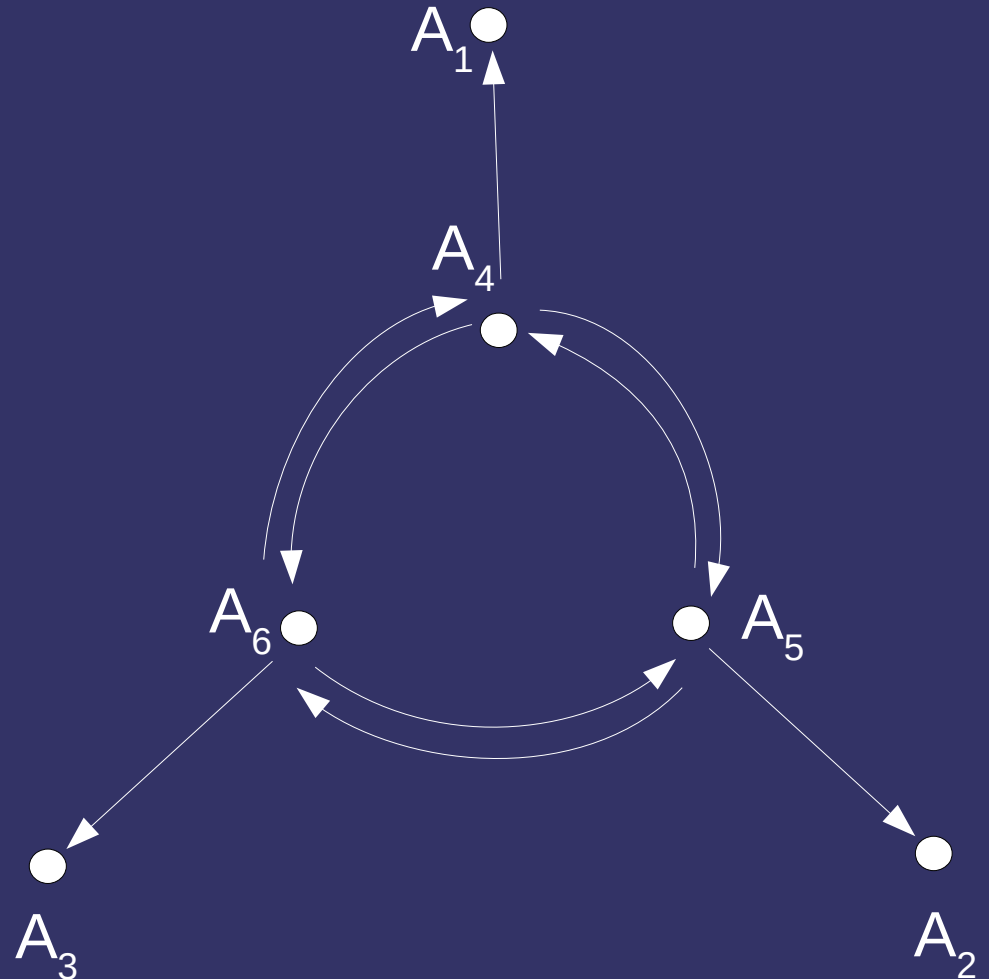
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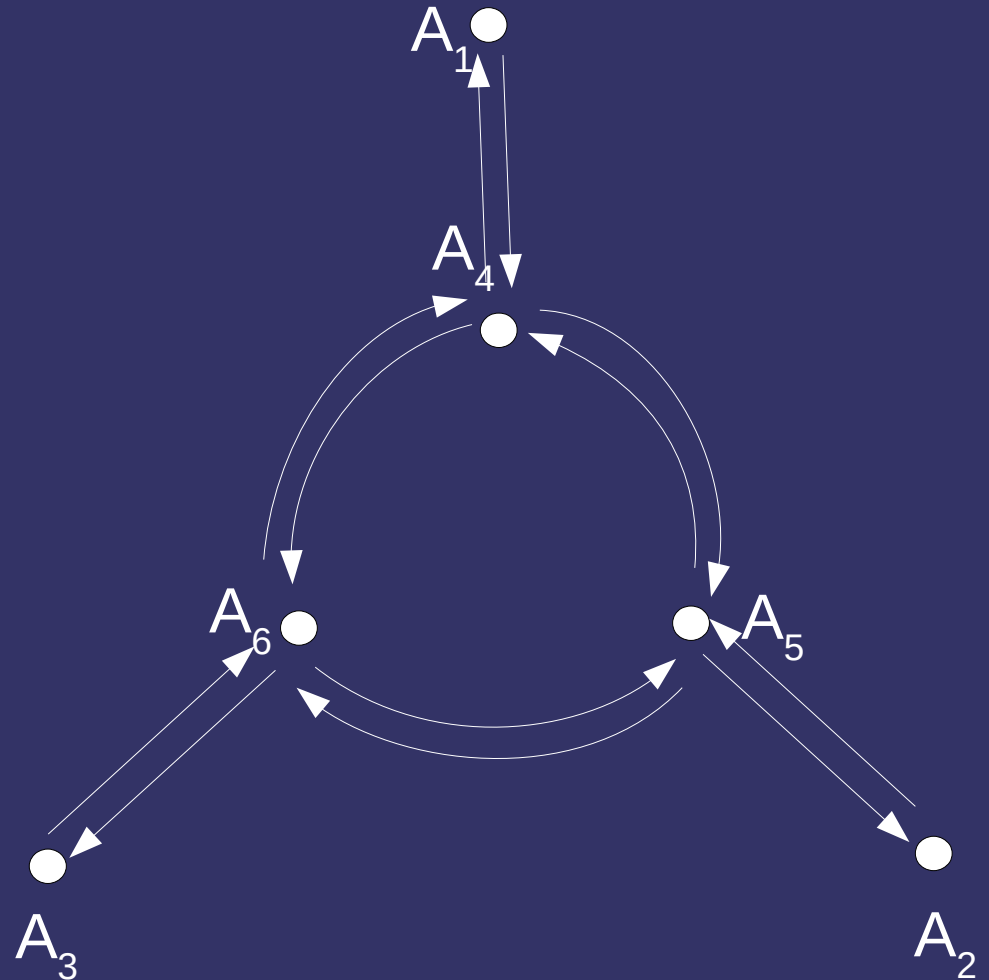
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$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$



Why Restricted Rebut

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

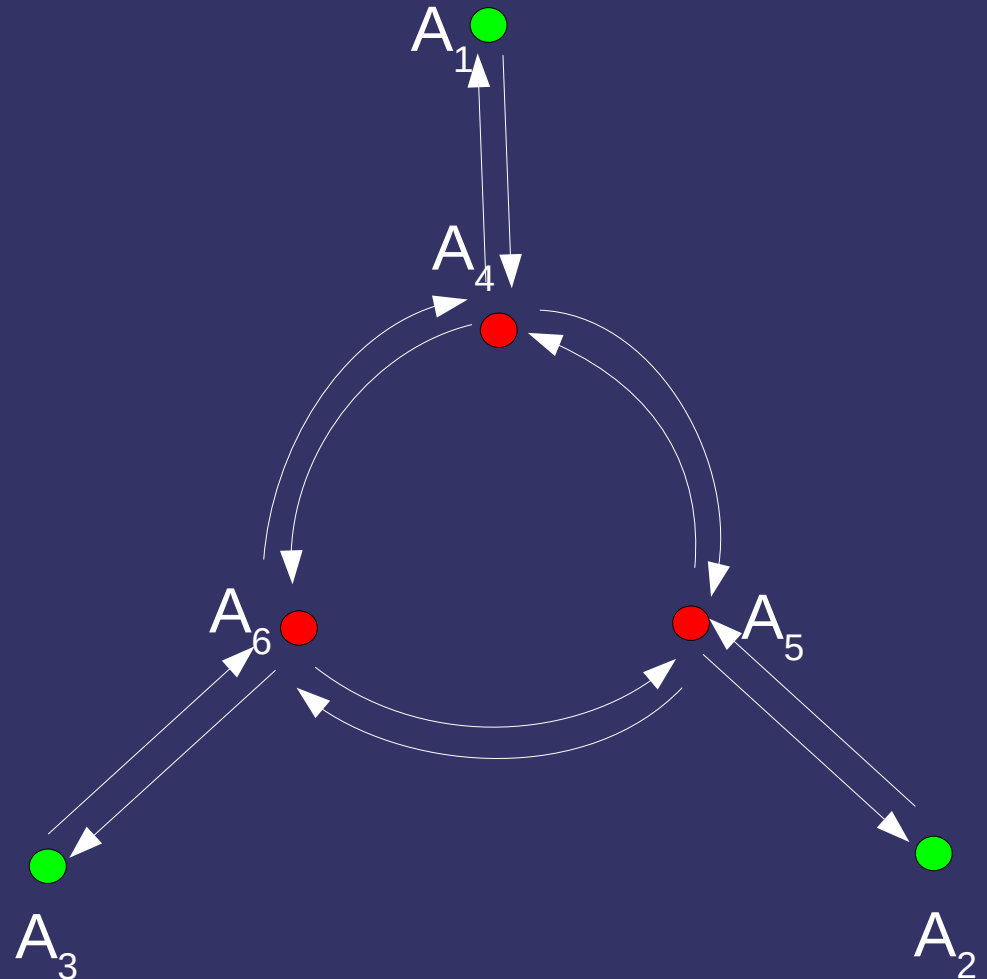
$A_2: (w2) \Rightarrow b2$

$A_3: (w3) \Rightarrow b3$

$A_4: A_2, A_3 \rightarrow \neg b1$

$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$



Why Restricted Rebut

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

$A_2: (w2) \Rightarrow b2$

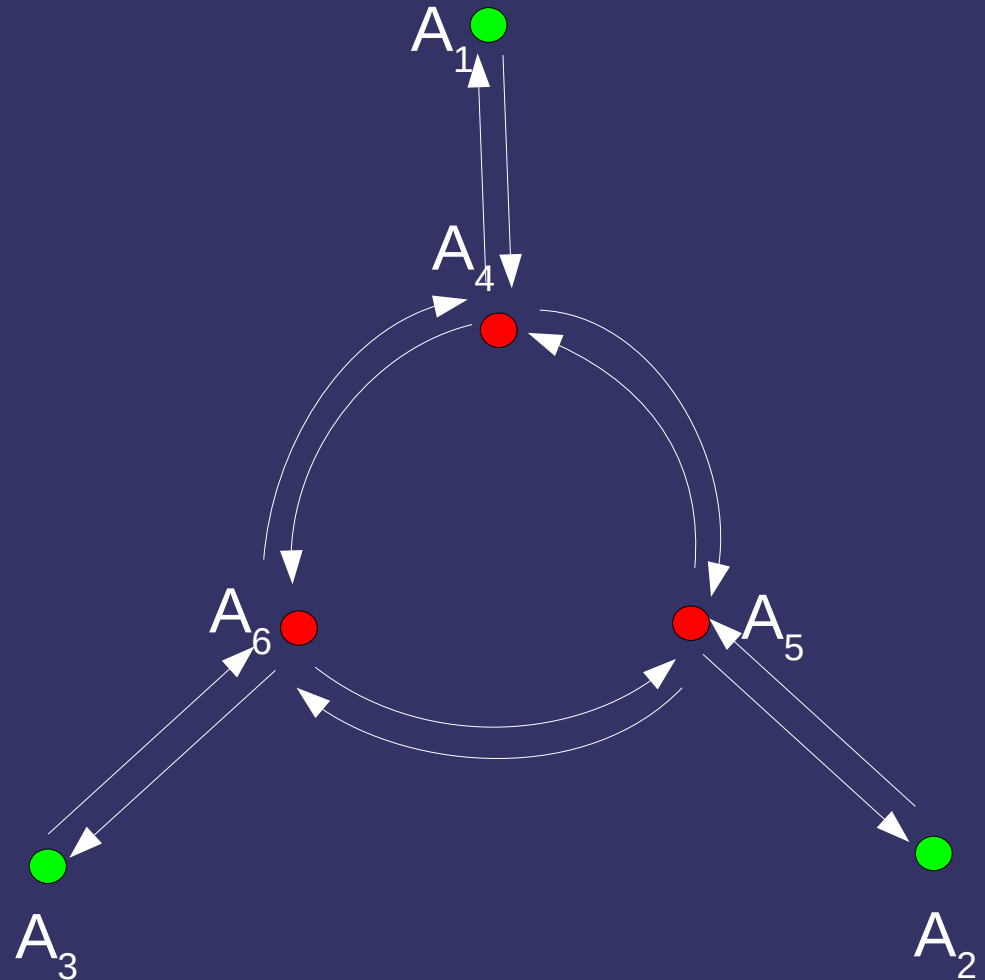
$A_3: (w3) \Rightarrow b3$

$A_4: A_2, A_3 \rightarrow \neg b1$

$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$

$b1 \ b2 \ b3 \quad \neg b1 \ \neg b2 \ \neg b3$



Why Restricted Rebut

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

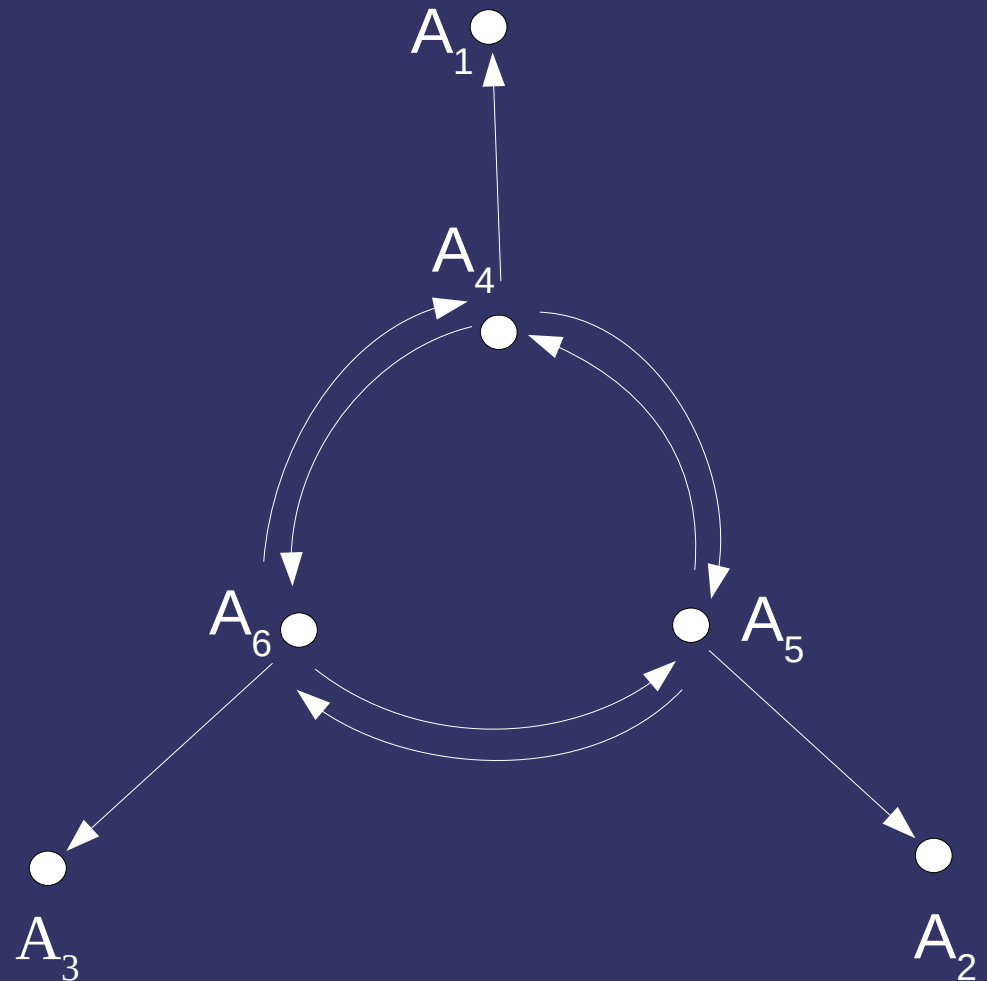
$A_2: (w2) \Rightarrow b2$

$A_3: (w3) \Rightarrow b3$

$A_4: A_2, A_3 \rightarrow \neg b1$

$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$



Why Admissibility

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

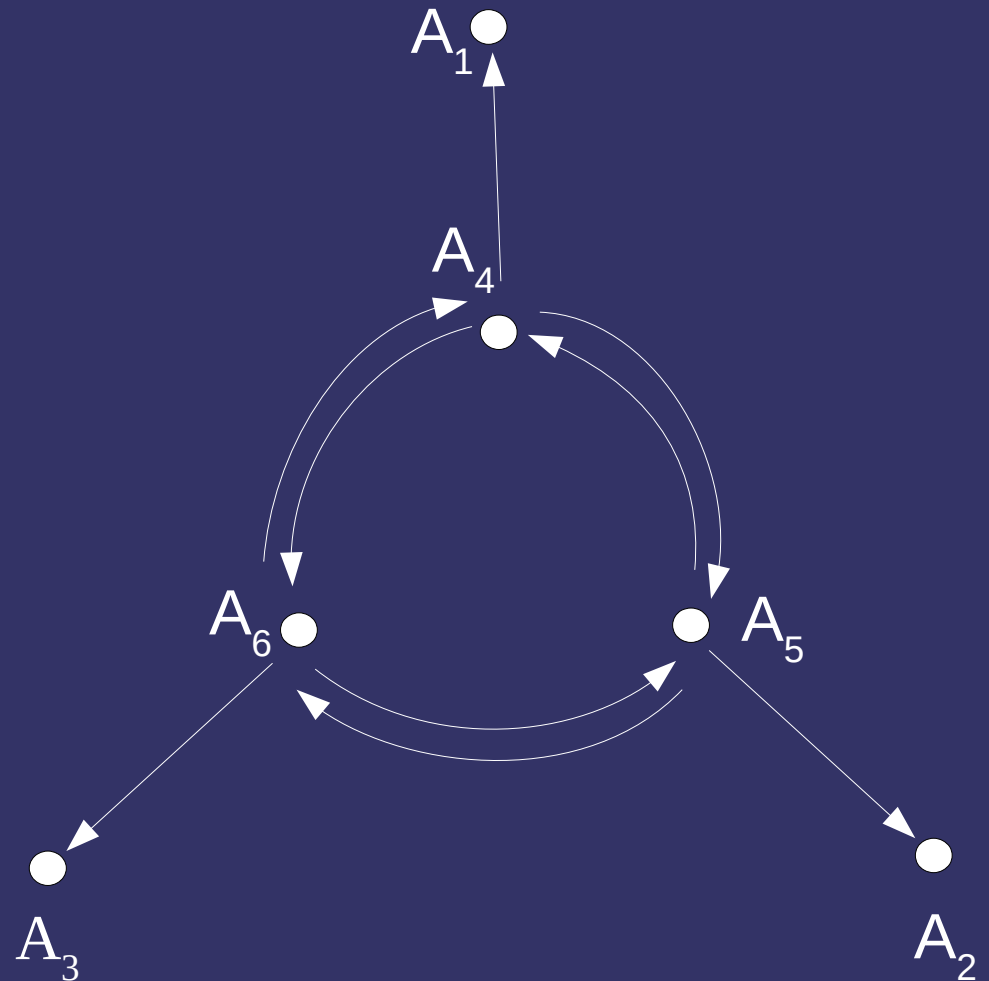
$A_2: (w2) \Rightarrow b2$

$A_3: (w3) \Rightarrow b3$

$A_4: A_2, A_3 \rightarrow \neg b1$

$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$



Why Admissibility

$S = \{ w1; w2; w3; b2, b3 \rightarrow \neg b1; b1, b3 \rightarrow \neg b2; b1, b2 \rightarrow \neg b3 \}$

$D = \{ w1 \Rightarrow b1; w2 \Rightarrow b2; w3 \Rightarrow b3 \}$

$A_1: (w1) \Rightarrow b1$

$A_2: (w2) \Rightarrow b2$

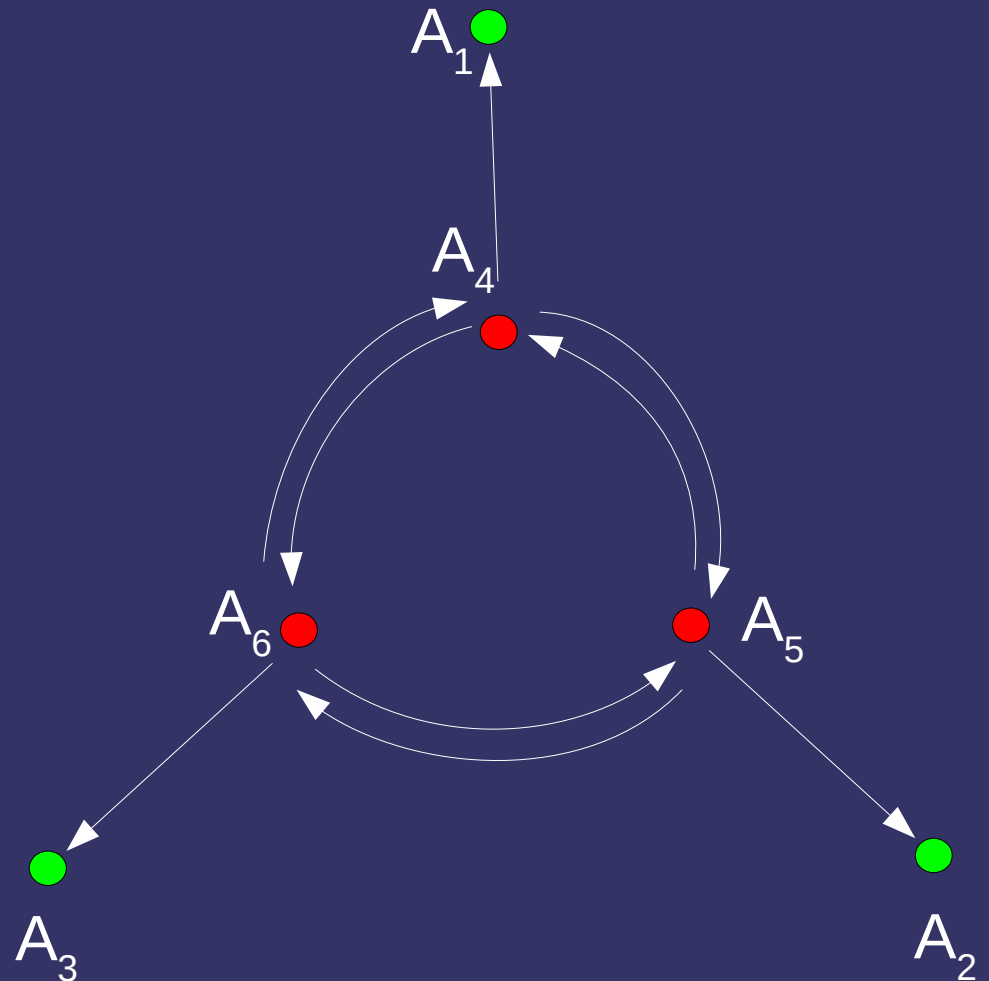
$A_3: (w3) \Rightarrow b3$

$A_4: A_2, A_3 \rightarrow \neg b1$

$A_5: A_1, A_3 \rightarrow \neg b2$

$A_6: A_1, A_2 \rightarrow \neg b3$

$b1 \ b2 \ b3 \quad \neg b1 \ \neg b2 \ \neg b3$



Research Challenge: finding the magic combinations

extensions (labellings)
of conclusions

↑ (3) *determining status of conclusions*

extensions (labellings)
of arguments

↑ (2) *applying argumentation semantics*

argumentation
framework

↑ (1) *argument (+attack) construction*

knowledge
base

Open Research Questions:

- 1) How to satisfy crash resistance when strict rules are generated by classical logic and defeasible rules have different strength?
- 2) How to satisfy closure and consistency when applying unrestricted rebut and defeasible rules have different strength?

Further Reading:

M.W.A. Caminada

Rationality Postulates: applying argumentation theory for non-monotonic reasoning
(Handbook of Formal Argumentation)

Recent Developments: *Heyninck & Straßer IJCAI17 / AAMAS19*

$A < B$ iff $\text{DefRules}(A) \neq \emptyset$ and
 $\forall d_B \in \min(\text{DefRules}(B)) \exists d_A \in \text{DefRules}(A): d_A < d_B$

Generalized Rebut:

$A \text{ GeRe } B$ iff

$\text{Conc}(A) = \neg b_1 \vee \dots \vee \neg b_n$ ($n \geq 1$) and each b_i occurs in B

Example: $\Rightarrow \neg b \vee \neg d$ rebuts (GeRe) $((\Rightarrow b) \Rightarrow c) \Rightarrow d$

A defeats B iff $A \text{ GeRe } B$ and $A \not< B$

This approach satisfies all rationality postulates (direct/indirect consistency, closure, crash-resistance, non-interference) but doesn't (yet) support undercutting (rebut only)

Argumentation Research: the Good, the Bad and the Ugly

The Good

research on how to to meaningfully draw conclusions based on (sufficiently rich) arguments and how to explain it

Argumentation Research: the Good, the Bad and the Ugly

The Bad

research that only provides an abstraction
without specifying what would be the full theory

always ask:

*“What is it that your abstract theory
provides an abstraction of”*

Argumentation Research: the Good, the Bad and the Ugly

The Ugly

research that uses argumentation
for a purpose that could be done
in a much simpler way
(e.g. MCS and LP)

Argumentation versus Machine Learning Only

Why not use ML on a big corpus of reasoning cases?

- 1) because the corpus may contain flawed reasoning (e.g. biases or logical errors)*
- 2) because you'd need to have a huge corpus, which might need to be generated*
- 3) because you want to have explainability*

*idea: use argument mining
to obtain the argument schemes*

Research Challenges

- How to satisfy closure, consistency and crash-resistance under different settings?
- Does exposure to argument-based discussion increase the user's confidence in the system's inferences?
- What would the discussion look like if the moves are rules instead of arguments?

Further Reading

(on topics in this presentation)

- Argumentation semantics
 - Dung, AIJ 1995 (*landmark paper*)
 - Baroni, Caminada & Giacomin (HOFA 2018, Ch4)
 - Caminada & Dunne (Argument&Computation 2019)
- Argumentation discussion games
 - Caminada (HOFA 2018, Ch10)
- Instantiated argumentation & rationality postulates
 - Modgil & Prakken (HOFA 2018, Ch6)
 - Caminada (HOFA 2018, Ch15)
 - Heyninck & Straßer (IJCAI 2017 / AAMAS 2019)
- Warnings against pure abstract argumentation
 - Caminada & Wu (BNAIC 2011)
 - Prakken & de Winter (COMMA 2018)

Further Reading

(on topics not in this presentation)

- How argumentation captures other forms of NMR:
 - Default Logic:
Dung (AIJ 1995), Caminada et al (JLC 2012)
 - Logic Programming:
Dung (AIJ 1995), Caminada & Schulz (JAIR 2017)
 - Classical Logic and Maximal Consistent Sets:
Besnard & Hunter (HOFA 2018 Ch9)
- Argument Schemes:
 - Macagno et al (HOFA 2018 Ch11)
- Formal argumentation and human intuitions:
 - Yu, Xu & Liao (Studies in Logic, 2018)
 - Cramer & Guillaume (COMMA 2018 / JELIA 2019)

Further Reading

(on topics not in this presentation)

- Argument Mining
 - Cabrio & Villata (IJCAI 2018)
 - IJCAI 2019 tutorial Federico Cerutti (tomorrow)
- Argumentation implementations
 - Cerutti et al (HOFA 2018, Ch14)
 - Nofal et al (AIJ 2014)
 - ICCMA 2015/2017/2019
- Online demonstrators:
 - DISCO: <http://disco.cs.cf.ac.uk/>
 - TOAST: <http://toast.arg-tech.org/>

Handbook of Formal Argumentation



Editors: Baroni, Gabbay,
Giacomin & van der Torre

College Publications (2018)

1028 pages

\$33.75 / €30.16 / £27.55

More on Argumentation at IJCAI

- Tutorial Federico Cerutti
Argumentation and Machine Learning
Monday 8.30am – 12.30pm
- Technical session
Computational Models of Argument
Friday 9.30am – 10.30am